

# Raman spectral characterization of existing phases in the $\text{ZrO}_2\text{--Y}_2\text{O}_3\text{--Nb}_2\text{O}_5$ system

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## Abstract

Tetragonal zirconia polycrystals (TZPs) were prepared with additions of 5.31 mol%  $\text{Y}_2\text{O}_3$  plus up to 5 mol%  $\text{Nb}_2\text{O}_5$  and their existing phases were investigated by Raman spectroscopy and X-ray diffraction. The present study reveals that Raman spectroscopy can identify the existing phases of cubic (c)-, tetragonal (t)-, monoclinic (m)- $\text{ZrO}_2$ , and Y–Nb ordered phase. The phase stability of t- $\text{ZrO}_2$  may be governed by the competition between stable and transformable t-phase as a function of  $\text{Nb}_2\text{O}_5$  content. Raman spectra of TZPs exhibit a broad and diffuse peak at around  $770\text{ cm}^{-1}$  in contrast to the c-, t- and m-phases due to local ordering. The local environment of  $\text{Nb}^{5+}$  in this system is maintained throughout  $\text{Nb}_2\text{O}_5$  concentrations ( $0 < \text{Nb}_2\text{O}_5 \leq 5\text{ mol}\%$ ), indicating that the  $770\text{ cm}^{-1}$  mode is likely to be related to the stable t-phase. © 2001 Elsevier Science Ltd and Techna S.r.l. All rights reserved.

**Keywords:** Tetragonal zirconia polycrystal; Y–Nb ordering; Raman spectroscopy

## 1. Introduction

Tetragonal zirconia polycrystals (TZPs) have been focused on as the candidate material of choice for structural and bio-ceramic applications, because of their excellent mechanical properties, hydrothermal phase stability, and biocompatibility [1–3]. Our previous work indicated that the stable TZPs exist in the composition region with 14–15 mol%  $\text{YNbO}_4$  in the  $\text{ZrO}_2\text{--YNbO}_4$  quasibinary system and within the certain triangular compositional boundary in the  $\text{ZrO}_2\text{--Y}_2\text{O}_3\text{--Nb}_2\text{O}_5$  system [1].

In the  $\text{ZrO}_2\text{--Y}_2\text{O}_3\text{--Nb}_2\text{O}_5$  system, as the  $\text{Nb}_2\text{O}_5$  content increased up to 1.5 mol%, the rate of low-temperature degradation (LTD) rose due to the increase in the  $c/a$  axial ratio (tetragonality) of the t- $\text{ZrO}_2$  solid solution, associated with the internal strain, as a result of annihilation of oxygen vacancies introduced by  $\text{Y}^{3+}$  [4–6]. On the other hand, TZPs, having a composition

of 90.24 mol%  $\text{ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ; 4.45 mol%  $\text{Nb}_2\text{O}_5$  (5.31Y–TZP), showed excellent phase stability and fracture toughness due to local Y–Nb dopant ordering in t- $\text{ZrO}_2$  into a scheelite-like arrangement, which resulted in a relief of the internal strain in the t- $\text{ZrO}_2$  lattice [1,5–8]. In the ordered structure, the smaller cation  $\text{Nb}^{5+}$  adopts a four-fold coordination leaving eight-fold coordination to  $\text{Y}^{3+}$ , determined by the observation of X-ray absorption spectroscopy [7].

However, although it appears that another factor must be related to the aging behavior in these TZPs, no systematic study for the effect of  $\text{Nb}_2\text{O}_5$  alloying to 5.31 mol%  $\text{Y}_2\text{O}_3\text{--TZP}$  on aging-induced degradation has been attempted over the composition range of  $\text{Nb}_2\text{O}_5$ , 0–5 mol%. For such purposes, detailed studies such as dependence of  $\text{Nb}_2\text{O}_5$  alloying on existing phases were carried out by using Raman spectroscopy.

## 2. Experimental procedure

The powder preparation procedure of Y–TZP doped with  $\text{Nb}_2\text{O}_5$  was reported elsewhere [1]. The powders

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having a composition of  $(94.69-x)$  mol%  $\text{ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ;  $x$  mol%  $\text{Nb}_2\text{O}_5$  ( $x=0, 1, 2, 3, 4$ , and 5) were chosen for this study because TZP, having a composition of 90.24 mol%  $\text{ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ; 4.45 mol%  $\text{Nb}_2\text{O}_5$ , showed excellent phase stability.

The powders were isostatically pressed at 140 MPa into pellets and then sintered for 1 h at 1550°C with a heating rate of 6°C/min from room temperature to 900°C and 3°C/min up to the sintering temperature and then furnace cooled to room temperature. A typical dimension of the sintered specimens were 18 mm in diameter and 2.0 mm in thickness. The sintered density was measured by the Archimedes method, using distilled water as the immersion medium. The average grain size was measured from scanning electron micrographs by the linear intercept method with the use of a correction factor of 1.56 after Mendelson [9].

The strength of 5.31 mol%  $\text{Y}_2\text{O}_3$  stabilized TZP (5.31Y-TZP) ceramics doped with  $\text{Nb}_2\text{O}_5$  was evaluated by biaxial flexure testing [10]. Biaxial flexure disks were initially ground on both sides to a nominal thickness of 1.8 mm, polished to a 1  $\mu\text{m}$  diamond finish and then subsequently annealed for 1 h at 1200°C in air. The disks were placed on a test fixture consisting of a three-point support and a loading plunger having a flat central loading point,

and broken at a stress rate of 23 MPa  $\text{s}^{-1}$  (Instron 4465). The fracture toughness was determined by the indentation-strength method proposed by Chantikul et al. [11]. A Vickers indent of 490 N was placed on the center of the tensile face of five test specimens. A drop of silicon oil was applied to minimize the moisture assisted subcritical crack growth. The ratio of hardness to modulus ( $H/E$ ) was then determined by measuring Knoop indentation impression dimensions as reported by Marshall et al. [12]. The average strength data obtained from five specimens which fractured from the indented sites were used for the subsequent toughness determination.

The samples were aged for 500 h at 220°C in air and then the extent of LTD was estimated from the m- $\text{ZrO}_2$  fraction of the aged and the fractured specimens according to Garvie and Nicholson [13] using a X-ray diffractometer. For the determination of lattice parameter at room temperature, X-ray diffraction (XRD) data were obtained from the ground powders, mixed carefully with the silicon internal standard (SRM 640b, National Institute of Standards and Technology, Gaithersburg, MD), using an automated XRD (Philips, EA, Almelo, The Netherlands) with  $\text{CuK}\alpha$  radiation ( $\lambda(\text{CuK}\alpha_1)=0.154060$  nm (1.54060 Å)). A scan speed of 0.5°  $2\theta/\text{min}^{-1}$  was used in the  $2\theta$  range of 65 to 120°.

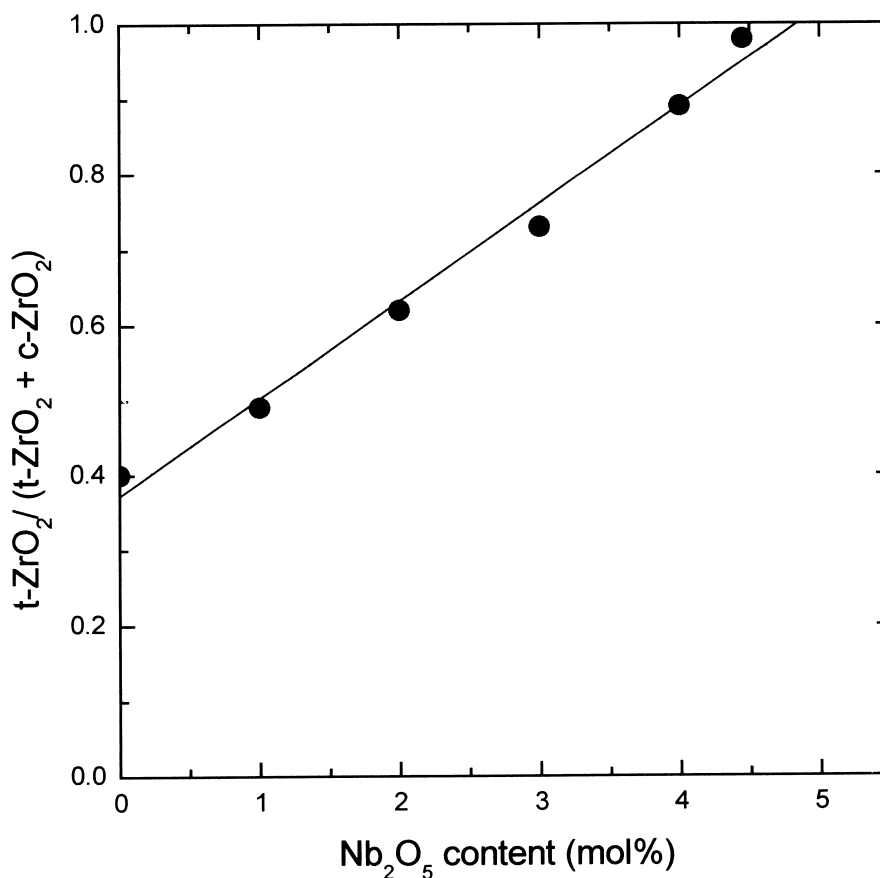


Fig. 1. Fraction of t- $\text{ZrO}_2$  of the sintered specimens having a composition of  $(94.69-x)$  mol%  $\text{ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ;  $x$  mol%  $\text{Nb}_2\text{O}_5$  ( $x=1-4.45$ ). The specimens were sintered for 1 h at 1550°C in air.

After  $k\alpha_2$  peak stripping, the peak position was determined by profile refinement using the built-in PC-APD program. Details of the lattice parameter refinement procedure have been described elsewhere [14].

Raman Spectra were obtained by a double monochromator (Model U1000, Jobin Yvon, Longjumeau, France) in a backscattering geometry. The spectra were excited with an argon ion laser that was operating at a wavelength ( $\lambda$ ) of 514.5 nm. Spectra of each specimen were taken over the range of 100–900  $\text{cm}^{-1}$ , scanning at a step size of 1.0  $\text{cm}^{-1}$  with an integration time constant of 1 s. The instrument was calibrated with the 520.9  $\text{cm}^{-1}$  Raman band of silicon wafer, and the error in determining the peak shifts was  $\pm 1 \text{ cm}^{-1}$ . The wavenumbers of the Raman bands were determined by the Lorentzian curve fitting of the spectra.

### 3. Results and discussion

The sintered specimens having a composition of  $(94.69-x) \text{ mol\% ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ;  $x \text{ mol\%}$

$\text{Nb}_2\text{O}_5$  ( $x=0-5$ ) are inhomogeneous due to the phase separation into t+c phases, as shown in Fig. 1. However, 5.31Y-TZP containing more than 4.6 mol%  $\text{Nb}_2\text{O}_5$  could not be fabricated because of the nearly complete transformation to the m- $\text{ZrO}_2$  phase during cooling below 500°C. 5.31Y-TZP is composed of 40% t-phase and 60% c-phase, but the extent of t-phase rises linearly with increasing the  $\text{Nb}_2\text{O}_5$  concentration, indicating that the c-phase becomes unstable and then decomposes into a t-phase. 5.31Y-TZPs doped with 4.45 to 4.6 mol%  $\text{Nb}_2\text{O}_5$  show only t-phase. Unlike  $\text{Y}^{3+}$  and  $\text{Zr}^{4+}$ ,  $\text{Nb}^{5+}$  is likely to occupy the four-fold coordination with oxygen ions due to the smaller ionic size of 0.074 nm [7], representing that the addition of  $\text{Nb}_2\text{O}_5$  into 5.31Y-TZP destabilizes the c-phase due to the increased tetragonality ( $c/a$  ratio) as shown in Fig. 1.

The lattice parameters of 5.31Y-TZP are plotted as a function of the  $\text{Nb}_2\text{O}_5$  concentration as shown in Fig. 2. In this system, it is believed that the lattice parameters should be constant regardless of the  $\text{Nb}_2\text{O}_5$  content because these compositions are positioned inside the two-phase region [1]. However, the lattice parameters

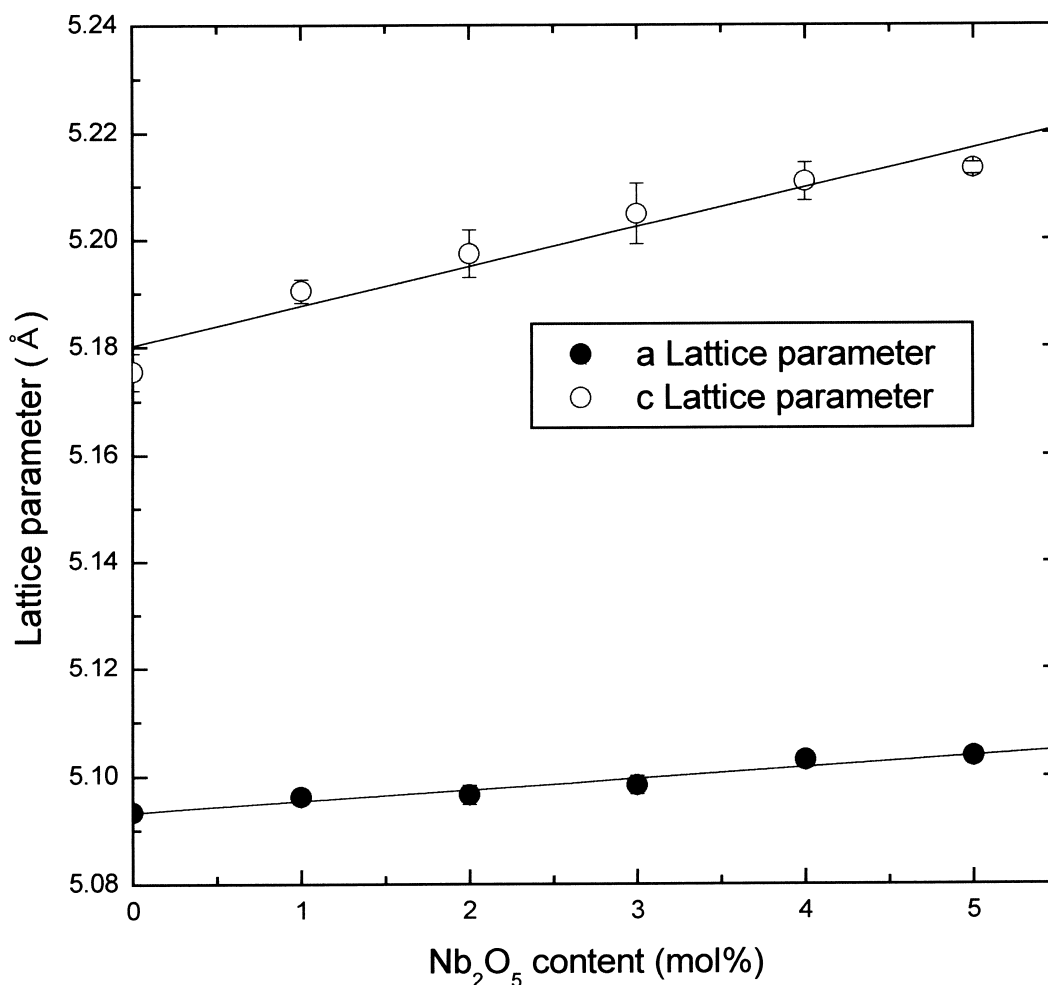


Fig. 2. Lattice parameters of 5.31 mol%  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  as a function of  $\text{Nb}_2\text{O}_5$  content.

increase linearly with an increase in  $\text{Nb}_2\text{O}_5$  content. Both lattice constants increase with the  $\text{Nb}_2\text{O}_5$  addition, but the effect of  $\text{Nb}_2\text{O}_5$  alloying on the c-axis lattice constants is more pronounced compared with the changes in the a-lattice parameter. This irrelevancy suggests that the stable t- $\text{ZrO}_2$  having a different crystal structure from the t- $\text{ZrO}_2$  existing in the  $\text{ZrO}_2\text{--Y}_2\text{O}_3$  system may start to form from the c-phase with an increase in  $\text{Nb}_2\text{O}_5$  content, however, the dissimilarity between two types of t- $\text{ZrO}_2$  solid solutions can not be discriminated by the XRD patterns.

The m- $\text{ZrO}_2$  content of the aged 5.31Y-TZP doped with  $\text{Nb}_2\text{O}_5$  was measured by using XRD. At low concentrations, 0–3 mol%, both destabilized t- $\text{ZrO}_2$  and c- $\text{ZrO}_2$  may transform to transformable (degradable) t- $\text{ZrO}_2$  with increasing the  $\text{Nb}_2\text{O}_5$  concentration, due to the annihilation of oxygen vacancies as a result of the substitution of  $\text{Nb}^{5+}$  for  $\text{Zr}^{4+}$ , as shown in Fig. 3. The degradable t- $\text{ZrO}_2$  in 5.31Y-TZP doped with 0–3 mol%  $\text{Nb}_2\text{O}_5$  can be easily distorted so that such a distortion raises the internal strain, which is prerequisite for the t $\rightarrow$ m phase transformation. From 3 mol%  $\text{Nb}_2\text{O}_5$ , the fraction of m- $\text{ZrO}_2$  starts to decrease abruptly and then

only t- $\text{ZrO}_2$  exists over the composition range of 4.45–4.6 mol%  $\text{Nb}_2\text{O}_5$ . The absence of LTD in 5.31Y-TZP doped with 4.45–4.6 mol%  $\text{Nb}_2\text{O}_5$  indicates that two types of t- $\text{ZrO}_2$  phases, a stable t- $\text{ZrO}_2$  in the system  $\text{ZrO}_2\text{--YNbO}_4$  and a degradable t- $\text{ZrO}_2$  in the system  $\text{ZrO}_2\text{--Y}_2\text{O}_3$ , may coexist, but the stable t- $\text{ZrO}_2$  phase hampers the t $\rightarrow$ m phase transformation of the degradable t-phase. That is, lattice relaxation of the degradable t- $\text{ZrO}_2$  is restrained significantly by the stable t-phase. It was reported by one of the authors that the stable t- $\text{ZrO}_2$ , which does not transform to m- $\text{ZrO}_2$  during low-temperature aging, exists due to local Y–Nb ordering in the composition region with 14–15 mol%  $\text{YNbO}_4$  in the  $\text{ZrO}_2\text{--YNbO}_4$  quasibinary system [1]. At 4.45 mol%  $\text{Nb}_2\text{O}_5$ ,  $\text{Nb}^{5+}$  necessary for the stability of t- $\text{ZrO}_2$  is dissipated by the proper substitution so that Y–Nb dopant ordering into a scheelite-like structure is achieved and the relaxation of the internal strain inherent in the t-lattice is accomplished. Beyond 4.6 mol%  $\text{Nb}_2\text{O}_5$ , the fraction of m- $\text{ZrO}_2$  starts to increase again, implying that the addition of excess  $\text{Nb}^{5+}$  into t- $\text{ZrO}_2$  increases the internal strain more significantly than TZPs doped with a small amount of  $\text{Nb}_2\text{O}_5$  (0–3 mol%).

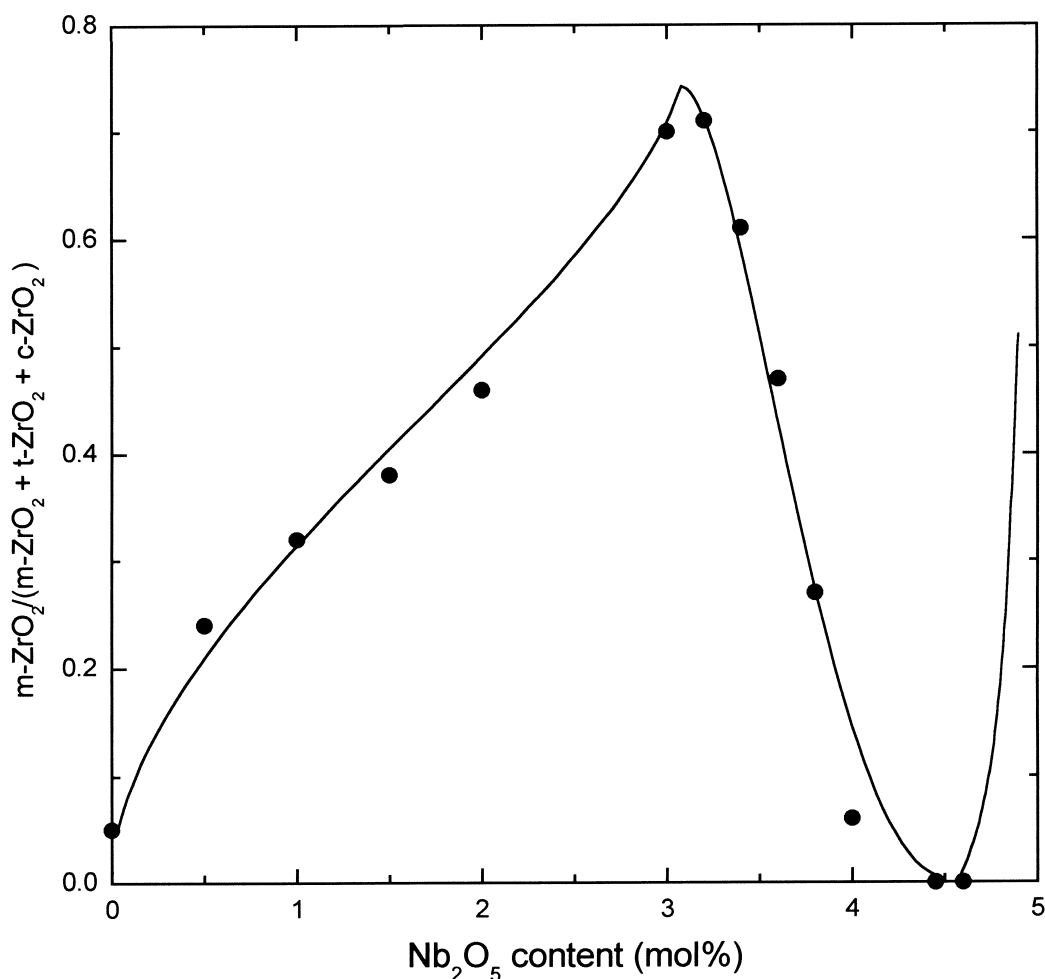


Fig. 3. m- $\text{ZrO}_2$  content of 5.31 mol%  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  containing different amounts of  $\text{Nb}_2\text{O}_5$  after aging for 500 h at 220°C in air.

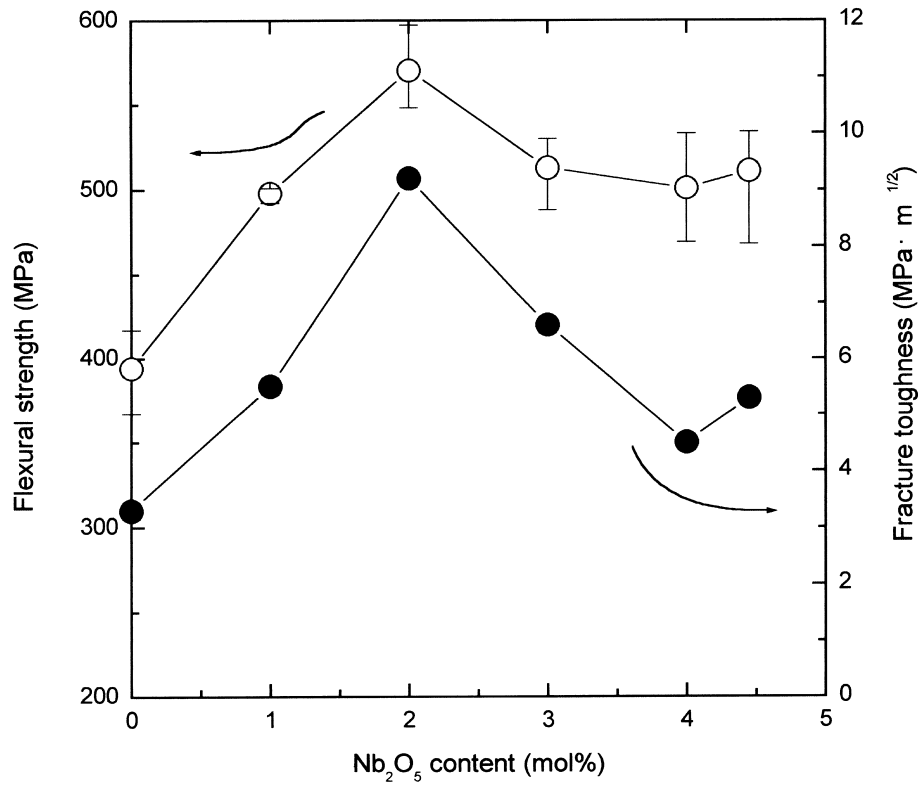


Fig. 4. Variation of biaxial strength and fracture toughness of 5.31 mol%  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  as a function of  $\text{Nb}_2\text{O}_5$  content.

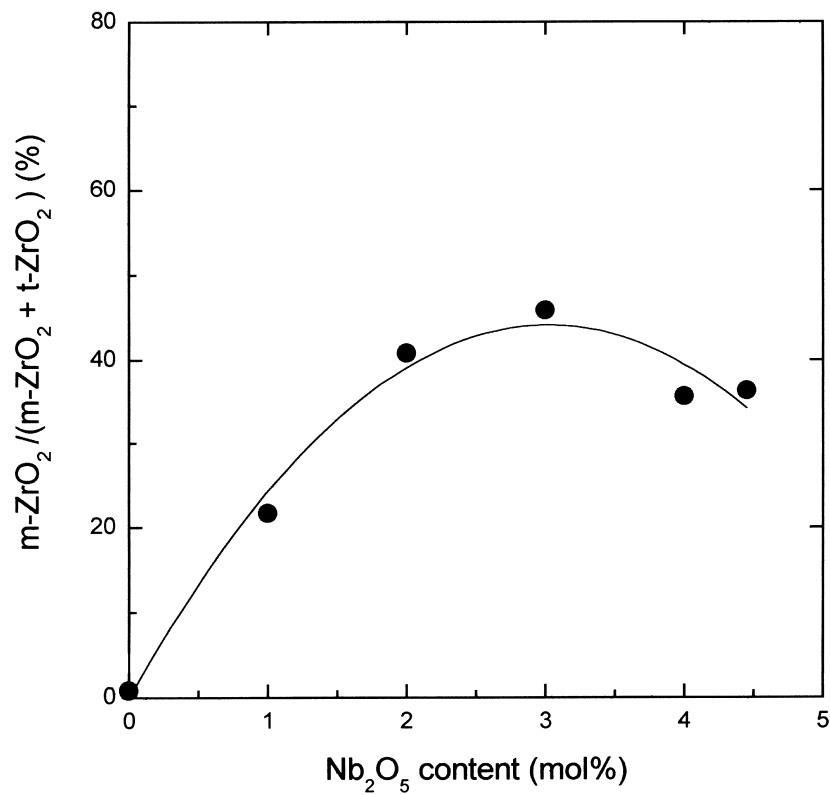


Fig. 5. m-ZrO<sub>2</sub> content on the fractured surfaces of 5.31 mol%  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  containing different amounts of  $\text{Nb}_2\text{O}_5$ .

Biaxial strength and fracture toughness were investigated and shown in Fig. 4. The initial increase of strength and fracture toughness probably stems from the fact that the stress-induced  $t \rightarrow m$  phase transformation becomes significant due to the overwhelming contribution to mechanical properties by the degradable  $t$ -ZrO<sub>2</sub> compared to the stable  $t$ -phase. From 2 mol% Nb<sub>2</sub>O<sub>5</sub>, both strength and fracture toughness start to decrease, implying that the Nb<sub>2</sub>O<sub>5</sub> content is just enough to form the tetrahedral bonds in the layer-like structure to relieve the internal strain, so that strength and toughness decrease as a result of lack of the stress-induced strengthening caused by the enhanced phase stability of the stable  $t$ -ZrO<sub>2</sub>. The fraction of  $m$ -ZrO<sub>2</sub> on the fractured surfaces of 5.31Y-TZPs increases to 46%

when the concentration increases to 3 mol% and then decreases slightly with increasing Nb<sub>2</sub>O<sub>5</sub>, as shown in Fig. 5. However, the fact that fracture toughness at 3 mol% Nb<sub>2</sub>O<sub>5</sub> is lower than that at 2 mol% Nb<sub>2</sub>O<sub>5</sub> implies the influence of increased phase stability on fracture toughness. The 46%  $m$ -ZrO<sub>2</sub> content that is related to the transformable  $t$ -phase does not increase with an increase in Nb<sub>2</sub>O<sub>5</sub>. Consequently, it is believed that most of  $t$ -ZrO<sub>2</sub> (4.45–4.6 mol% Nb<sub>2</sub>O<sub>5</sub>) may be present in the form of the stable  $t$ -ZrO<sub>2</sub> due to local Y–Nb ordering, which is a prerequisite for TZP phase stability.

The effect of Nb<sup>5+</sup> content on the Raman spectra of 5.31Y-TZP is shown in Fig. 6. The Nb doping shifts the Raman bands that are related with the stretching modes

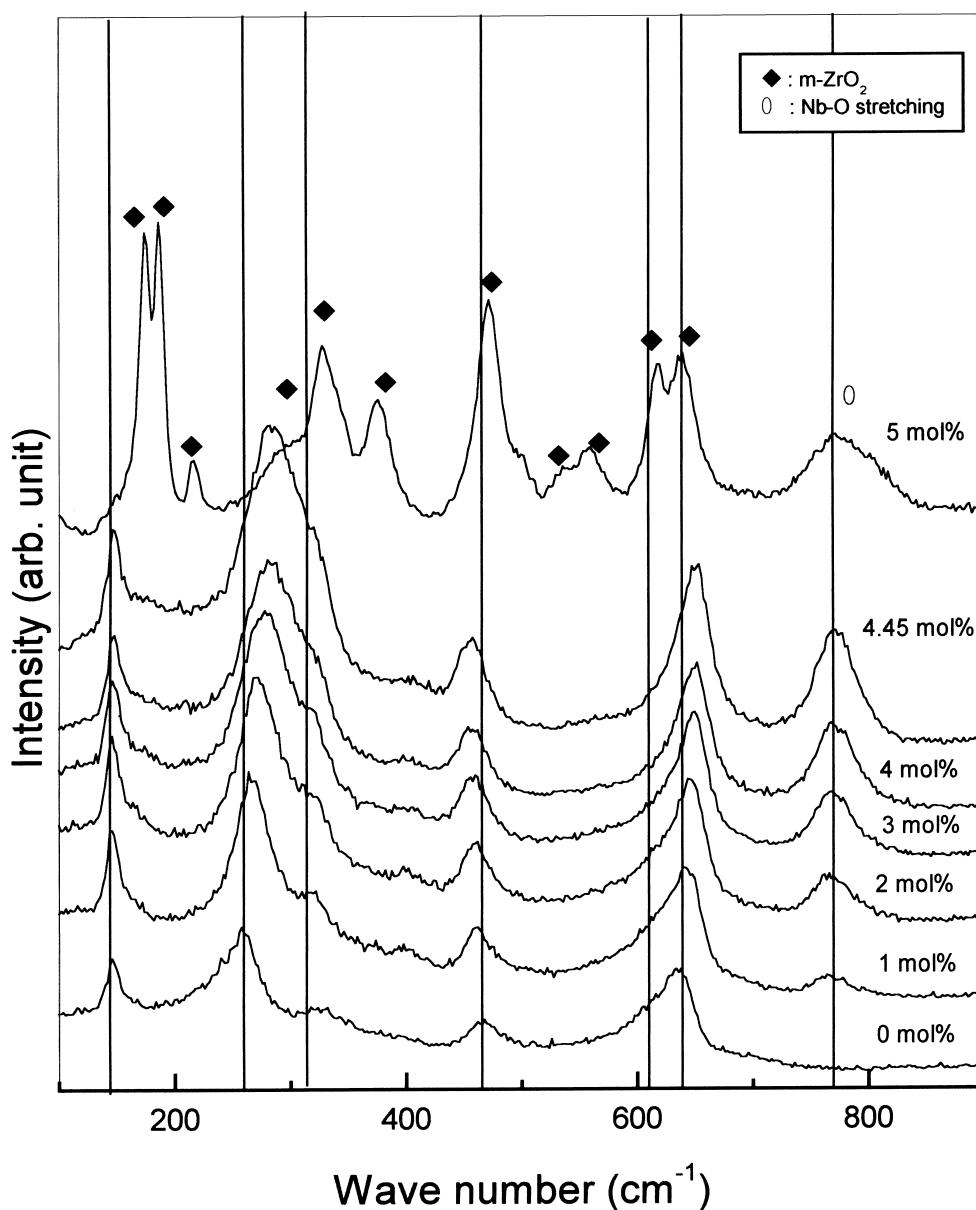


Fig. 6. Raman spectra of 5.31 mol% Y<sub>2</sub>O<sub>3</sub>-stabilized ZrO<sub>2</sub> containing different amounts of Nb<sub>2</sub>O<sub>5</sub>.

of  $\text{Zr-O}_{\text{II}}$  ( $260\text{ cm}^{-1}$ ) and  $\text{Zr-O}_{\text{I}}$  ( $640\text{ cm}^{-1}$ ) towards higher wavenumbers, which corresponds to the increase in zirconium–oxygen bond strength. The shift of Raman spectra indicates that a rather different local bonding environment with oxygens is formed due to the addition of  $\text{Nb}_2\text{O}_5$ . In addition to six Raman modes ( $147, 260, 321, 465, 609, 640\text{ cm}^{-1}$ ) in  $\text{t-ZrO}_2$ , an extra peak near  $770\text{ cm}^{-1}$  that is absent in  $5.31\text{Y-TZP}$  appears and the peak height of  $770\text{ cm}^{-1}$  increases linearly over the sum of peak height of  $260\text{ cm}^{-1}$  and  $640\text{ cm}^{-1}$  as the  $\text{Nb}_2\text{O}_5$  content increases. However, the peak height of  $770\text{ cm}^{-1}$  decreases as the  $\text{Nb}_2\text{O}_5$  content is above  $4.6\text{ mol}\%$ . Hardcastle and Wachs [15] reported that the bond lengths and stretching frequencies for the perfect  $\text{NbO}_4$  tetrahedron and the perfect  $\text{NbO}_6$  octahedron are estimated to be  $1.823\pm0.024\text{ \AA}$  and  $787\pm30\text{ cm}^{-1}$ ,  $1.977\pm0.024\text{ \AA}$  and  $586\pm30\text{ cm}^{-1}$ , respectively, under the assumption of the diatomic approximation and an anharmonic dependence between force constant and interatomic distance, and Raman band arising from symmetry related Nb–O modes always occur at low frequency below  $300\text{ cm}^{-1}$ . A relatively large diffuse

peak at around  $780\text{ cm}^{-1}$ , characterized by Raman spectroscopy, was reported as the defect-fluorite phase in the  $\text{Y}_2\text{O}_3\text{-Nb}_2\text{O}_5$  system [16]. It was argued that the diffuse Raman peaks were due to local ordering and a modulated structure through electron diffraction in the defect-fluorite solid solutions [16]. The Raman stretching frequency of the shortest Nb–O bond is observed only at  $770\text{ cm}^{-1}$  that is  $10$  and  $17\text{ cm}^{-1}$  lower than the value of  $780\text{ cm}^{-1}$  for the defect-fluorite phase and  $787\text{ cm}^{-1}$  for the ideal  $\text{NbO}_4$  tetrahedron, respectively. As a result, it is in good agreement with the local Y–Nb ordered phase and the tetrahedral closest packing of  $\text{O}^{2-}$  ions around a  $\text{Nb}^{5+}$  ion. Several researchers [7,15] proposed that the coordination of  $\text{Nb}^{5+}$  should be changed from four to six during the  $\text{t}\rightarrow\text{m}$  phase transformation, implying that the  $770\text{ cm}^{-1}$  band should be shifted to  $586\text{ cm}^{-1}$ . However, the  $586\text{ cm}^{-1}$  Raman band is not observed in the present study. Failure to observe the  $586\text{ cm}^{-1}$  band and the existence of the broad  $770\text{ cm}^{-1}$  band at this composition suggests that although there occurs severe distortion of the  $\text{NbO}_4$  tetrahedron because this phenomenon is commonly

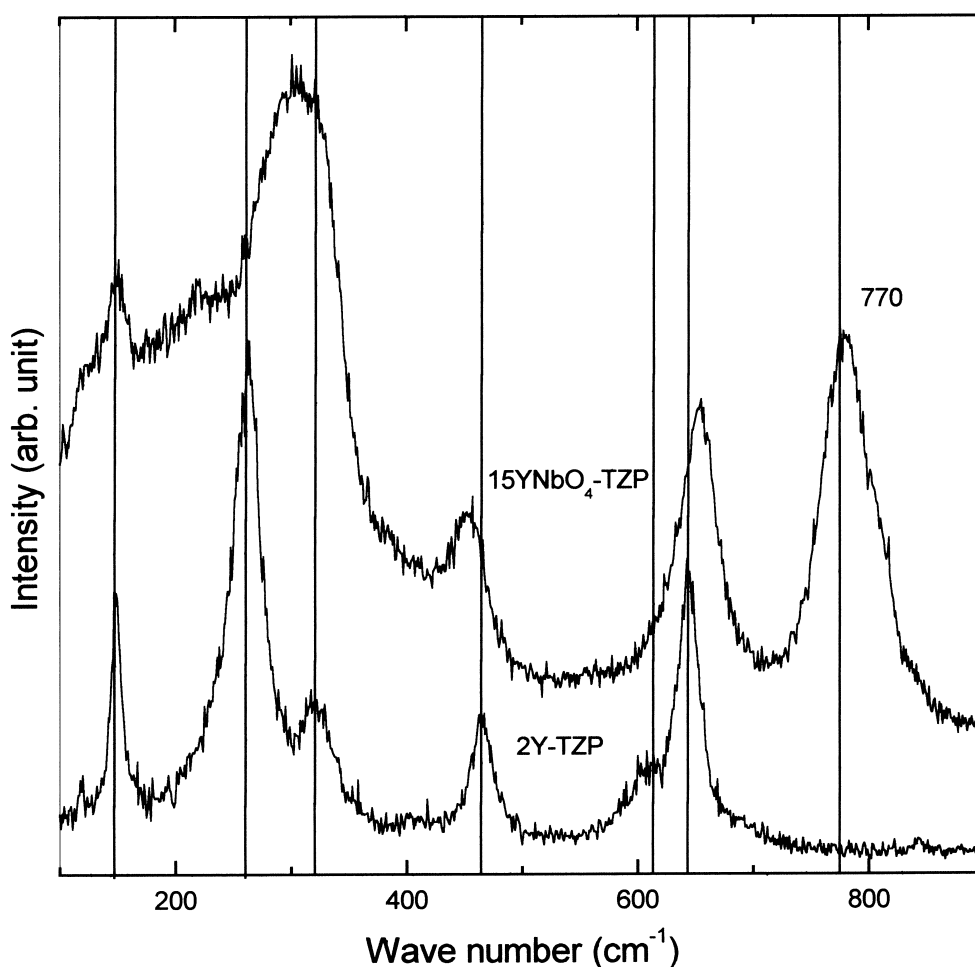


Fig. 7. Comparison of Raman spectra of  $2\text{ mol}\%$   $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  and  $15\text{ mol}\%$   $\text{YNbO}_4$ -stabilized  $\text{ZrO}_2$ .

Table 1

Existing phases of (94.69– $x$ ) mol%  $\text{ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ;  $x$  mol%  $\text{Nb}_2\text{O}_5$  samples sintered for 1 h at 1550°C in air. Resulting phases are characterized by Raman spectroscopy. C, T, Y, and M indicate cubic phase, tetragonal phase, defect-fluorite (Y–Nb ordered) phase, and monoclinic phase, respectively

$\text{Nb}_2\text{O}_5$ (mol%)	Resulting phases
0	C+T
1	C+T+Y
4.45	T+Y
4.6	T+Y
5	M+Y

observed when a disorder caused by the dopant addition is introduced into the crystal structure, the  $\text{NbO}_4$  tetrahedron is sustained throughout the  $\text{Nb}_2\text{O}_5$  concentration. Typical Raman spectra of 2 mol%  $\text{Y}_2\text{O}_3$ -stabilized TZP (2Y–TZP) and 15 mol%  $\text{YNbO}_4$ -stabilized TZP (15  $\text{YNbO}_4$ –TZP) are shown in Fig. 7. 2Y–TZP shows the typical six Raman modes which is unique for the fluorite structure, but the  $770\text{ cm}^{-1}$  band, which is absent in the binary system  $\text{Y}_2\text{O}_3$ – $\text{ZrO}_2$ , is observed in 15  $\text{YNbO}_4$ –TZP as expected. The existing phases in 5.31Y–TZP doped with  $\text{Nb}_2\text{O}_5$  characterized by Raman spectroscopy are summarized in Table 1. However, the fraction of the Y–Nb ordered phase could not be determined quantitatively in the present study.

#### 4. Conclusions

Raman spectroscopy can identify the existing phases of cubic (c)-, tetragonal (t)-, monoclinic (m)- $\text{ZrO}_2$ , and Y–Nb ordered phase in the ternary system (94.69– $x$ ) mol%  $\text{ZrO}_2$ ; 5.31 mol%  $\text{Y}_2\text{O}_3$ ;  $x$  mol%  $\text{Nb}_2\text{O}_5$  ( $x=0$ –5 mol%). The phase stability of t- $\text{ZrO}_2$  may be governed by the competition between stable and transformable t-phase as a function of  $\text{Nb}_2\text{O}_5$  content. Raman spectra of TZPs exhibit a broad and diffuse peak at around  $770\text{ cm}^{-1}$  in contrast to the c-, t- and m-phase due to local ordering, which is likely to be related to the stable t- $\text{ZrO}_2$ . Therefore, the phase stability of t- $\text{ZrO}_2$  in this system is attributed mainly to the  $\text{Nb}_2\text{O}_5$  content.

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