

# Kinetics of growth of superhard boride layers during solid state diffusion of boron into titanium

B. Sarma\*, N.M. Tikekar, K.S. Ravi Chandran

*Department of Metallurgical Engineering, 135 South 1460 East Room 412, The University of Utah, Salt Lake City, UT 84112, USA*

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## Abstract

Solid state boriding of titanium is a very effective and inexpensive way to create surface layers that can impart high hardness and wear resistance. In this work, the growth kinetics of hard titanium boride layers created by the solid-state boron (B) diffusion through titanium (Ti) surface at various temperatures has been determined. The hard boride layers comprised of a monolithic titanium diboride ( $\text{TiB}_2$ ) layer at the top and a titanium boride (TiB) sub-layer that mostly consisted of TiB whiskers with high aspect-ratio growing normal to the surface. The structure and the crystallography of the layers were also confirmed by X-ray diffraction. Experimental results show that the growth rates of the  $\text{TiB}_2$  as well as the composite ( $\text{TiB}_2 + \text{TiB}$ ) coating layers follow the parabolic kinetics. It is shown that the thickness development as a function of time can be predicted reasonably accurately, using the error function solutions for the two simultaneously growing boride layers developed in our previous work. The maximum degree of growth as dictated by the diffusivity of B in the boride phases was achieved using a solid state B powder pack in an ambient furnace atmosphere.

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**Keywords:** Titanium boride; Diffusion; Whiskers; Kinetics

## 1. Introduction

It is well known that titanium (Ti) in heavy duty tribological and contact conditions suffers from high volumetric wear, galling, and seizure of surfaces. To mitigate these, surface hardening techniques such as the nitriding [1,2] or oxidizing [3–5] of titanium surfaces were pursued. A good review of the developments until the 1990s can be found in Ref. [5]. Nitriding increases the surface hardness of Ti to about 9–12 GPa (Vicker's hardness (Hv)) [6,7] with a moderate increase in wear resistance [8,9]. This is attributed to the dispersion of TiN and  $\text{Ti}_2\text{N}$  phases in the subsurface region to a depth of about 10–25  $\mu\text{m}$ . In oxygen-based surface hardening, oxygen enrichment leads to a surface hardness of about 5–12 GPa Hv [10,11], and has been found to improve the abrasive wear and/or scratch resistance. However, the use of these hardening techniques is limited for various reasons. This is partly due to the fact that the surface hardness levels

attainable by nitriding or oxidizing are, at best, about 10–12 GPa which is comparable to that obtained in surface hardened steels or unhardened tool steels. Additional issues such as the poor underlying support of the substrate beneath the titanium nitride layers [9] and the possible embrittlement of titanium substrate due to the presence of nitrogen or oxygen as interstitials also pose some intrinsic limitations.

Borides of titanium have a much higher hardness and wear resistance [12,13]. In our past research [14–16] the feasibility of solid state diffusion of boron into titanium to create hard ( $> 15$  GPa) and wear resistant surface layers up to depths of about 50  $\mu\text{m}$  was demonstrated. The diffusion leads to two layers of borides, with the top layer being titanium diboride ( $\text{TiB}_2$ ) and the second layer being titanium boride (TiB). The  $\text{TiB}_2$  grows as solid monolithic layer while the TiB below it predominantly grows as pristine whiskers, generally perpendicular to the surface. These hard dual layers provide a unique surface-modified structure that builds high surface hardness and wear resistance—the  $\text{TiB}_2$  layer provides surface hardness levels in excess of 30 GPa Hv and the TiB whiskers, in addition

\*Corresponding author. Tel.: +1 801 682 0619.

E-mail address: [biplabsarma@gmail.com](mailto:biplabsarma@gmail.com) (B. Sarma).

to having high hardness ( $> 15$  GPa Hv), anchor the coating into the substrate, which is very desirable for coating durability. In fact, it has been shown recently [17,18] that 6.35 mm dia. Ti balls borided with such a dual layer coating (for ball bearings) have superior wear resistance (about  $40\times$  better) than fully alumina balls when abraded against alumina disk.

There are a few studies of boride layer growth on titanium [13,19–22], but none address the detailed kinetics and explain the growth mechanisms. The earliest work in the area of titanium boriding was performed by Krzyminski and Kunst [13] and Chatterjee-Fischer and Schaab [19]. These studies showed that boride layer growth by the diffusion from solid B media is possible when boriding is performed in a controlled atmosphere with a reduced oxygen partial pressure. A more recent work [21] also confirmed the key finding of Krzyminski and Kunst that at a reduced oxygen partial pressure (1 Pa), the reaction activity is the highest for boriding.

The primary objective of this work is to fully establish the kinetics of the growth of titanium boride layers as a function of boriding temperature in the  $\alpha$  and  $\beta$  phase fields of Ti. The structure and the growth kinetics of the boride layers formed at temperatures above and below the beta transus ( $\beta$ -transus) temperature of Ti and the mathematical framework to predict the kinetics are very important both from fundamental and application points of view. More importantly, the emphasis of this study is on solid state boron diffusion process in a regular furnace atmosphere as opposed to the controlled atmosphere that was used in the studies mentioned above. The additional

objective is to show that error function solutions based on Fick's second law, developed for the two simultaneously growing layers, predict the layer growth kinetics quite well.

## 2. Experimental procedure

Commercially pure titanium (CP-Ti, Grade 2, composition in wt%: 0.3 Fe, 0.25 O, 0.1 C, 0.03 N, 0.015 H and 0.3 max. of other elements) samples ( $30\text{ mm} \times 14\text{ mm} \times 6\text{ mm}$ ) were polished to 800 grit surface finish. A boriding powder mixture comprising a B source (amorphous boron, Composition in wt%: 95–97 B, 0.89 Mg, 0.12 water soluble B, particle size FN 0.694, from SB Boron Corporation, Bellwood, IL), a transport medium (99% pure anhydrous sodium tetraborate from Alfa Aesar Inc.) and carbon activator (99.5% pure from Alfa Aesar Inc.) was prepared by ball milling the powders for about 16 h. The mixture was tightly packed in a crucible ensuring a sufficiently thick ( $> 1''$ ) pack all around the sample. Boron diffusion experiments were conducted by heating (rate:  $10^\circ\text{C}/\text{min}$ ) the pack to temperatures in the range  $850$ – $1050^\circ\text{C}$  for periods up to 24 h in an ambient furnace atmosphere. After the treatment, the formation of different phases on the borided samples was identified using SIEMENS D5000 diffractometer with copper  $K_\alpha$  radiation. The diffraction tests were done by  $\theta$  to  $\theta$  scan from  $20^\circ$  to  $100^\circ$ . The samples were then sectioned, metallographically polished and etched. Boride layer structure was examined using scanning electron microscopy (SEM). Thicknesses of  $\text{TiB}_2$  layer and the composite ( $\text{TiB}_2 + \text{TiB}$  whisker) coating layer

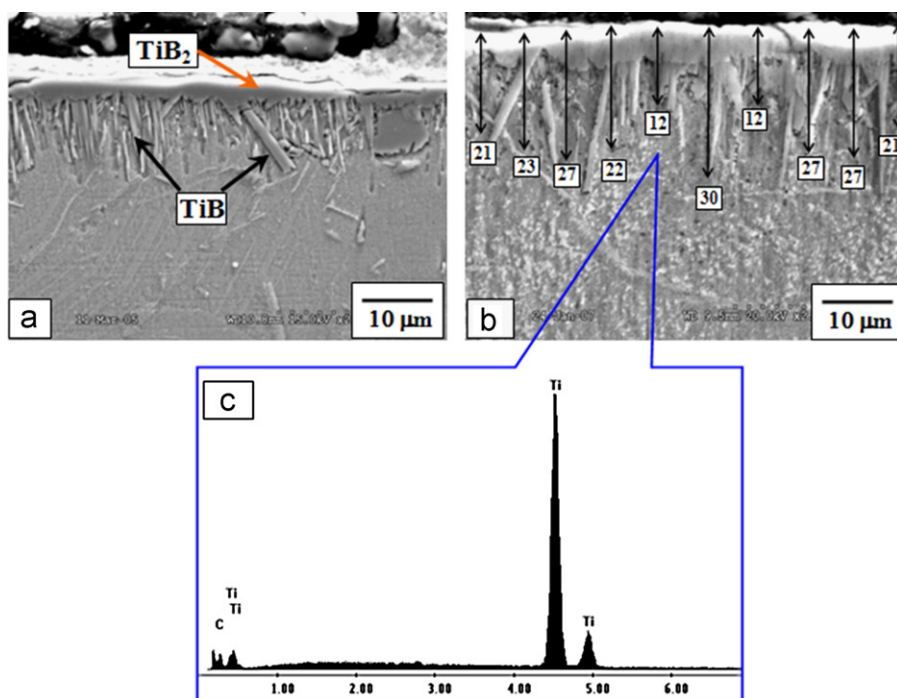


Fig. 1. SEM micrographs of coating structure in CP-Ti borided at  $850^\circ\text{C}$  for (a) 3 h and (d) 24 h, the vertical arrows in (b) and the numbers in boxes indicate the total coating thickness at equally spaced locations (c) the EDX profile of the Ti substrate in between  $\text{TiB}$  whiskers.

were determined from SEM micrographs on the basis of averages of measurements at ten equally spaced locations, as illustrated in Fig. 1(b). This involved measuring the distance of the farthest location of the tip of the intercepted TiB whisker, from the specimen edge, at ten equally spaced locations. For each boriding condition, such measurements were made on three different micrographs and the averages and the standard deviations of these measurements were determined. The TiB<sub>2</sub> grew as a continuous monolithic layer—its thickness could be readily measured at ten equally spaced locations on multiple SEM micrographs.

### 3. Results and discussion

#### 3.1. Structure of boride layers

The average coating thicknesses and standard deviations for the TiB<sub>2</sub> and the composite (TiB<sub>2</sub>+TiB) coating layers are given in Table 1 for different treatment temperatures and times. Microstructures of the dual layer coatings obtained after boriding at 850 °C for 3 h and 24 h are shown in Fig. 1(a and b). A continuous and thin outer layer of TiB<sub>2</sub>, followed by TiB whiskers penetrating normally into the substrate can be seen. Even though the outer TiB<sub>2</sub> layer constituted only a small fraction of the total coating thickness (Table 1), it was almost completely continuous in all the treatments. The thickness of the TiB<sub>2</sub> layer increased from 1.5 µm at 3 h to 3.9 µm at 24 h. The TiB layer is made of extremely fine TiB whiskers that have needle-like morphology with thicknesses in the range of 10–100 nm. The presence of some isolated ends of TiB whiskers located far inside the substrate can be seen in the 3 h treatment (Fig. 1a)—these seem to be the ends of TiB whiskers that originated from somewhere behind the plane of polishing. The outlines of TiB whiskers were found to be quite well defined and they were found to be thicker after longer treatment times compared to that seen in shorter treatment times. It is evident from the micrographs that, like TiB<sub>2</sub>, the TiB phase does not grow as a monolithic layer. Hence, when we refer to the “TiB layer” it is implied that it is a layer of TiB whiskers with Ti located in between. The EDX profile of the substrate in between the TiB whiskers confirms the presence of Ti only as shown in Fig. 1c.

The structures of boride layers after 950 °C treatment for 3 h and 24 h are shown in Fig. 2(a and b). A continuous TiB<sub>2</sub> layer followed by TiB whiskers penetrating into the CP-Ti substrate, similar to that at 850 °C, can be seen. The TiB<sub>2</sub> layer is slightly thicker and the TiB whiskers seem to penetrate deeper into the substrate, compared to that at 850 °C. Both the TiB<sub>2</sub> and TiB layer thicknesses increased by a factor  $\geq 2$ , on going from 3 to 24 h. Micrographs of samples borided at 1050 °C (this temperature is well into the  $\beta$ -phase field of titanium) for 3 h and 24 h are presented in Fig. 3(a and b). Due to the high temperature diffusion treatment, a thicker TiB<sub>2</sub> layer

Table 1  
Averages thickness values of TiB<sub>2</sub>, TiB and the composite (TiB<sub>2</sub>+TiB) coating layers, determined for different B diffusion temperatures and times.

Time (h)	850 °C				950 °C				1050 °C			
	TiB <sub>2</sub> (µm)	TiB <sub>2</sub> (µm)	Total (µm)	TiB (µm)	TiB <sub>2</sub> (µm)	Total (µm)	TiB (µm)	TiB <sub>2</sub> (µm)	Total (µm)	TiB (µm)	TiB <sub>2</sub> (µm)	Total (µm)
0.083	13	0.5 ± 0.1	13.5 ± 3.0	15	1 ± 0.1	16 ± 2.5	15	1.5 ± 0.1	16.5 ± 1.9	15	1.5 ± 0.1	16.5 ± 1.9
3	21.5	1.5 ± 0.1	23 ± 3.2	22.8	3.2 ± 0.3	26 ± 2.7	26	5 ± 0.3	31 ± 2.5	26	5 ± 0.3	31 ± 2.5
6	21.3	2.7 ± 0.2	24 ± 3.5	24.2	4.8 ± 0.2	29 ± 3.2	27	10 ± 0.7	37 ± 3.4	27	10 ± 0.7	37 ± 3.4
12	21.8	3.2 ± 0.2	25 ± 4.2	28.6	5.4 ± 0.3	34 ± 3.3	29	12 ± 0.9	41 ± 3.6	29	12 ± 0.9	41 ± 3.6
18	22.7	3.3 ± 0.3	26 ± 5.4	39.3	5.7 ± 0.3	45 ± 4.4	35	15 ± 0.9	50 ± 5.7	35	15 ± 0.9	50 ± 5.7
24	24.1	3.9 ± 0.3	28 ± 6.3	40.6	6.4 ± 0.4	47 ± 5.4	37	17 ± 1.0	54 ± 5.9	37	17 ± 1.0	54 ± 5.9

\*TiB coating thickness was determined by subtracting the average thickness of TiB<sub>2</sub> layer from the average total coating thickness, hence there is no S.D. for these data.

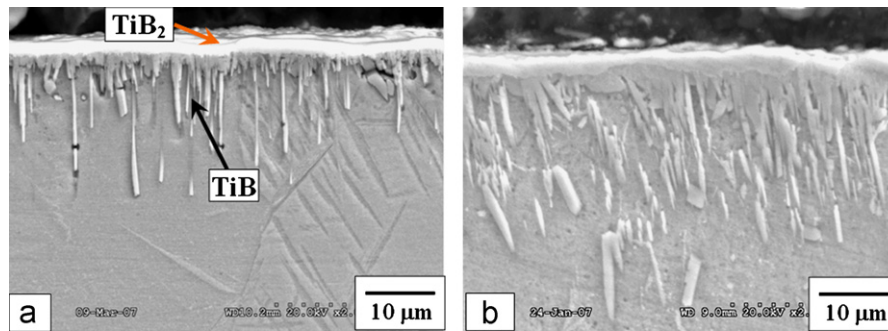


Fig. 2. SEM micrographs of coating structure in CP-Ti borided at 950 °C for (a) 3 h, and (b) 24 h.

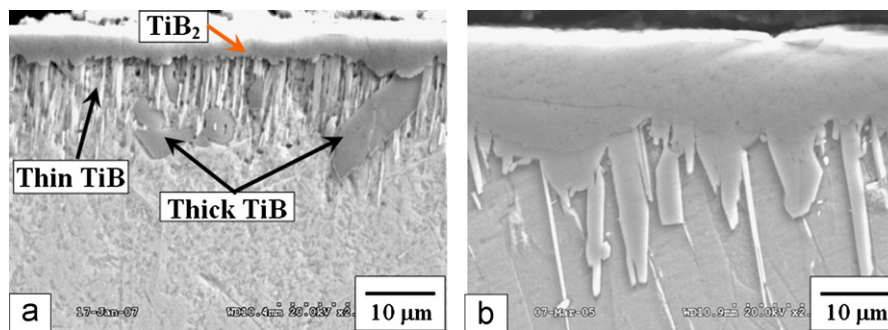


Fig. 3. SEM micrographs of coating structure in CP-Ti borided at 1050 °C for (a) 3 h, and (d) 24 hr.

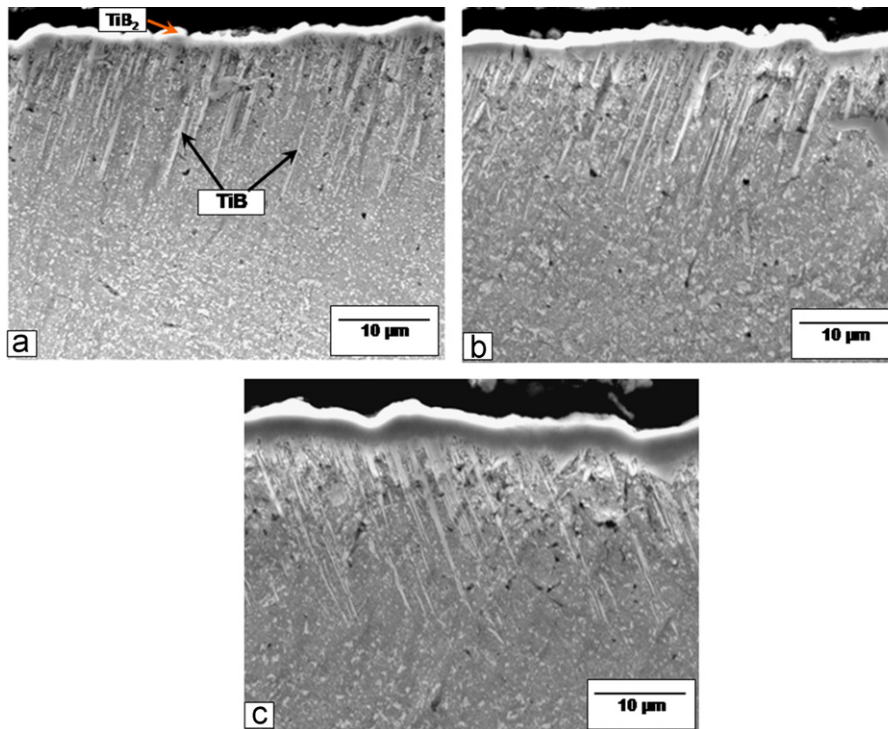


Fig. 4. SEM micrographs of CP-Ti samples borided for 5 min at different temperatures (a) 850 °C, (b) 950 °C and (c) 1050 °C.

was observed in all the samples. The TiB<sub>2</sub> thickness increased by a factor of 3 from 5 μm at 3 h to 17 μm at 24 h. (Table 1) indicating that the growth rate of TiB<sub>2</sub> layer is relatively faster than that observed at 850 and 950 °C.

Unlike the TiB whisker structure at 850 °C, the TiB whisker layer at 1050 °C seems to be actually made of two size groups: the individual nano-sized whiskers and a much thicker micron-sized TiB phases (Fig. 3a and b).



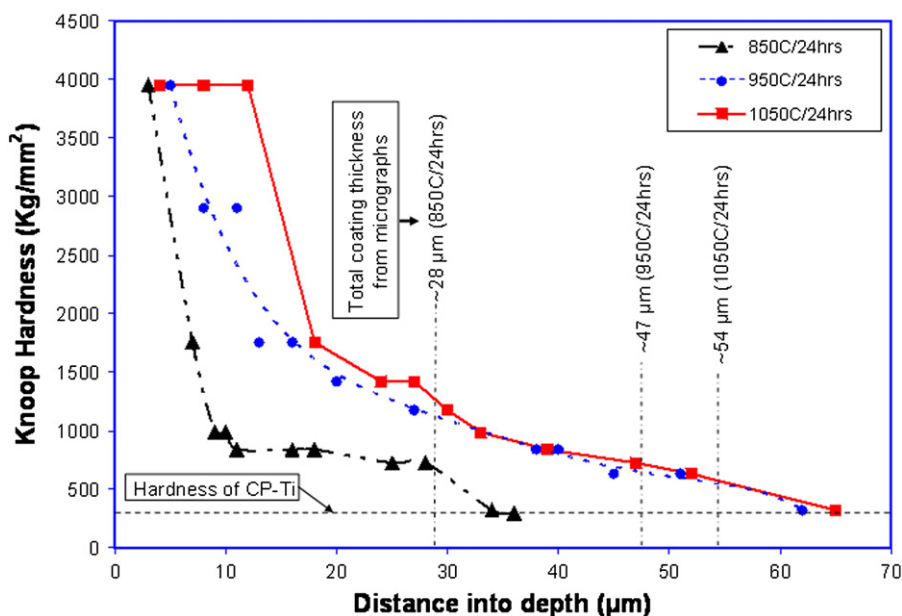


Fig. 5. Knoop hardness profile of the ( $\text{TiB}_2 + \text{TiB}$ ) boride layer formed at 850 °C, 950 °C and 1050 °C after 24 h of diffusion treatment time. The hardness of CP-Ti ( $\sim 300 \text{ kg/mm}^2$ ) is also shown for reference.

Nevertheless, the depth to which the TiB whiskers penetrated into the substrate increased with time.

The SEM micrographs of samples borided for 5 min at 850 °C, 950 °C and 1050 °C are shown in Fig. 4(a–c), respectively. Three important observations can be made from these micrographs and the data in Table 1, with respect to the nature of growth of individual layers and their relative dominance. First, based on the short term (5 min/0.083 h) layer thickness data, it is clear that a substantial growth of TiB whiskers occurs very early—it is likely that TiB formation actually started at relatively low temperatures, and that some pre-grown TiB existed even before reaching the isothermal treatment temperatures. This is evident from the fact that at 850 °C, the TiB growth after 5 min (13 µm) is more than that occurred between 3 h to 24 h (3 µm). Second observation is that there is not much growth of  $\text{TiB}_2$  during the short term (5 min) diffusion—most of the  $\text{TiB}_2$  growth actually occurred during the isothermal hold periods at the diffusion temperatures. Third observation is that the change in the TiB whisker layer thickness, on going from 5 min to 24 h diffusion, reaches a maximum at 950 °C—the changes in the TiB whisker layer thickness are  $\sim 11 \text{ µm}$ ,  $25 \text{ µm}$  and  $22 \text{ µm}$  for 850 °C, 950 °C and 1050 °C, respectively. Thus, it is clear that most of the increase in the total coating thickness is due to the increased contribution of TiB whisker layer at 950 °C and that of  $\text{TiB}_2$  layer at 1050 °C. The rates of growth of  $\text{TiB}_2$  and the composite ( $\text{TiB}_2 + \text{TiB}$ ) coating layers were found to follow the parabolic growth kinetics, but they were dependent on whether the treatment temperature was in  $\alpha$ -field or  $\beta$ -field or proximal to the  $\beta$ -transus—a more detailed account of the effects during diffusion near  $\beta$ -transus are presented elsewhere [23].

Knoop hardness profiles across the boride layers in samples borided at 850 °C, 950 °C and 1050 °C after 24 h of treatment times are shown in Fig. 5. The surface layers are hardened to a depth of about 30 µm in 850 °C/24 h sample and to about 60 µm in both 950 °C/24 h and 1050 °C/24 h samples, which are consistent with the SEM observations of the coating depths. The hardening depth is slightly higher than the actual depth of the layer despite the fact that the coating depth in the micrograph was measured as the farthest tip of the growing TiB whiskers. This suggests that the thickness measurements from the micrographs can be taken as the conservative coating thickness values and can be used for comparison with theory. The high hardness ( $> 3000 \text{ kg/mm}^2$ ) region near the surface corresponds to the thin layer of  $\text{TiB}_2$ . The sub-surface boride layer is actually a mixture of TiB whiskers and  $\text{TiB}_2$  monolith, or the transition region, which explains the steep decrease in hardness with distance into the substrate. The hardness of monolithic TiB is about  $2000 \text{ kg/mm}^2$ . The coating structures beyond the  $\text{TiB}_2$  are a mixture of TiB and Ti, with the volume fraction of TiB gradually decreasing with distance into the depth. The decreasing hardness profile in this region is consistent with the variations in TiB/Ti phase proportions in the sublayer.

The X-ray diffraction patterns for the boride layers are given in Fig. 6(a and b) for the 3 h and 24 h diffusion treatments at various temperatures. It can be observed that the borided layers consisted mostly of  $\text{TiB}_2$  and TiB compounds, with a clear dominance of  $\text{TiB}_2$  phase in the 1050 °C treatments. However, for 3 h, the 850 °C and the 950 °C treatments showed relatively higher concentrations of TiB whiskers. In particular, for the 24 h treatment, a relatively high concentration of TiB was found at 950 °C,

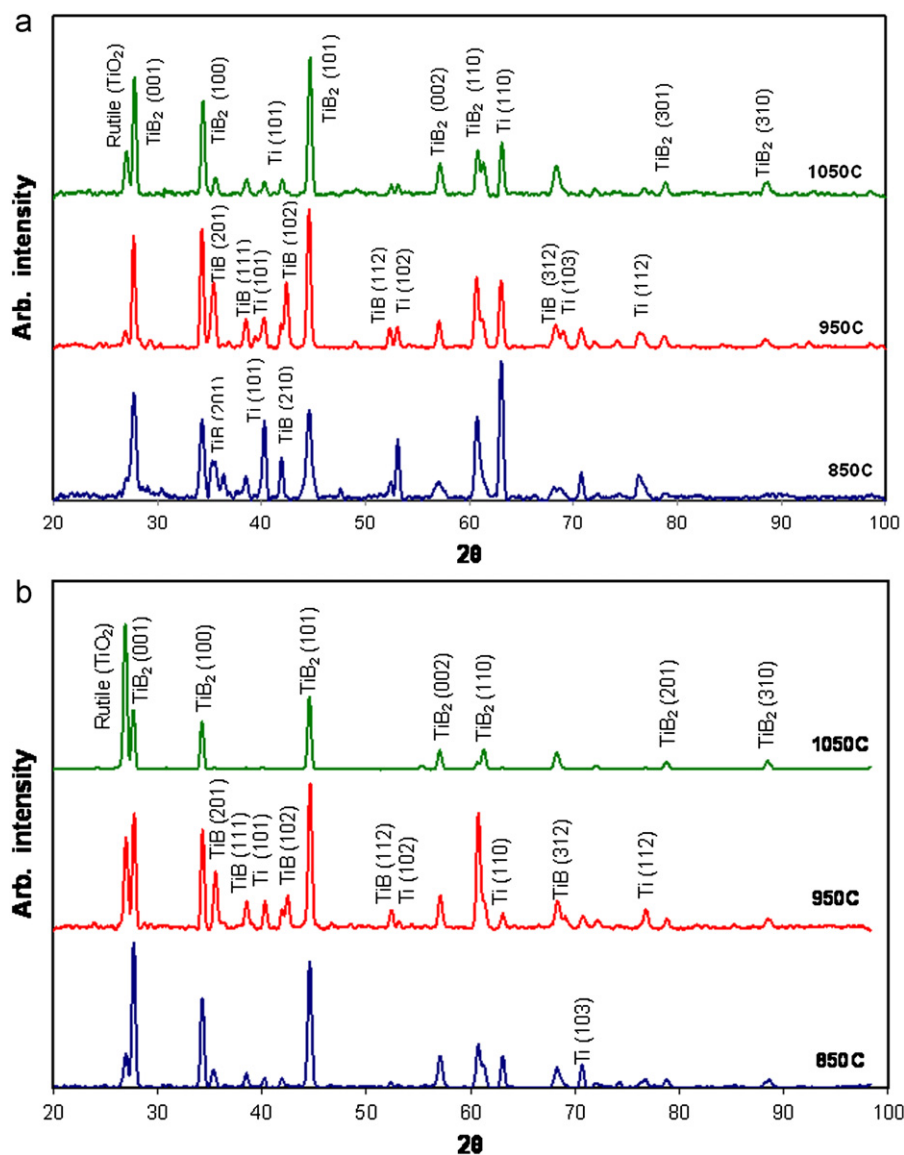


Fig. 6. X-ray diffraction profiles for the coatings borided at different temperatures for (a) 3 h and (b) 24 h.

Table 2  
Diffusivity data [29] used in the calculations of kinetics using error function solutions.

$T$ (°C)	Chemical diffusivity of B in $\text{TiB}_2$ ( $\text{m}^2/\text{s}$ )	Chemical diffusivity of B in TiB ( $\text{m}^2/\text{s}$ )
850	$1.34 \times 10^{-16}$	$6.13 \times 10^{-15}$
950	$6.92 \times 10^{-6}$	$3.25 \times 10^{-14}$
1050	$2.78 \times 10^{-15}$	$1.34 \times 10^{-13}$

compared to the other two temperatures. These observations are consistent with the SEM microstructures, in that, the 950 °C/24 h condition resulted in the highest TiB layer thickness. As reported in a recent study [21], the X-ray diffraction patterns also indicate the presence of rutile titanium oxide ( $\text{TiO}_2$ ) in the surface of all borided samples. However, the presence of this oxide layer could not be detected by SEM as the thickness of this layer is

apparently very small. It is to be noted that only one peak in the diffraction patterns could be assigned to  $\text{TiO}_2$ . There was no evidence of oxide phase within the boride layers. It is possible that the oxide layer had formed when the crucible was removed from the furnace after cooling to 500 °C after boriding. Further, as will be evident in the next section, the oxide layer does not appear to have influenced the growth kinetics.

### 3.2. Modeling of layer growth kinetics

Prior work on quantitative prediction of the growth of boride layers on Ti is quite limited. For the growth of multiple compound layers by diffusion, error-function based solutions [24,25] of Fick's second law can be used to predict the kinetics. The growth of FeB/Fe<sub>2</sub>B layers on Fe during boriding is somewhat similar to the growth of boride layers here. The kinetics of growth of FeB/Fe<sub>2</sub>B

layers have been predicted using the diffusivity of B alone [26–28] and assuming that the diffusion of metal component is negligible. In the present analysis, the chemical diffusivity values of B in TiB<sub>2</sub> and TiB (determined from the work of Fan et. al. [29]) were used (Table 2) to predict the growth of the two boride layers. In the Ti–B system, TiB<sub>2</sub> is a stoichiometric line compound and TiB has narrow stoichiometric range. Thus, in practice, diffusional growth of these compounds under B concentration gradient does not involve large concentration gradient within the phases. Nevertheless, the concentration difference between B/TiB<sub>2</sub>/TiB layers can be considered to represent the average compositional gradients in the phases.

In our recent publication [23], an effort was made to model the growth kinetics of boride layers on Ti using error function approach. However, the modeling aspects were pertaining to growth of layers at temperature close to the  $\alpha/\beta$  phase transition temperature in Ti (910 °C). As elucidated in the article, the growth behaviors of the layers near the transition temperature are quite different compared to when B diffusion experiments are performed away from it (in complete  $\alpha$  and  $\beta$  phase fields). Here, with the experimental results of boride layers at temperatures 850, 950 and 1050 °C, we would examine whether a similar theoretical model can also describe the growth kinetics of these layers at these temperatures. The detailed modeling procedure was explained in Ref. [23], however, the fundamental aspects as well as some key equations of the model are discussed in the following.

The development of the error function solutions will be illustrated on the basis of growth of TiB<sub>2</sub>/TiB whisker layer on titanium (Fig. 7(a)). Three interfaces exist in this system: the B–TiB<sub>2</sub> interface, TiB<sub>2</sub>–TiB interface and the TiB–Ti interface. The B concentration profiles across the layers are schematically shown in Fig. 7(b). The Fick's second law of diffusion, relating the changes in concentration of B with time and location is:

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2} \quad (1)$$

where  $D$  is the diffusion coefficient and  $C$  is the concentration. The development of error function solutions is based on the following assumptions: (i) the growth of the dual layer is controlled only by the diffusion of B and the diffusion of Ti in the opposite direction can be ignored [29], (ii) the diffusion coefficient of B is concentration independent, and (iii) the solubility of B in Ti-matrix is negligible [30]. The aforementioned assumptions are based on the prior works as described in Ref. [29]. It was suggested that the growth of the TiB<sub>2</sub> and the TiB are limited only by the sluggish diffusion of B through these layers. The kinetics of the interfacial reactions is much faster compared to that of the B diffusivities through these layers. On the other hand, the diffusivities of Ti in these phases are couple of orders of magnitude lower than that of B as it diffuses substitutionally. Hence, from the modeling perspective, the influence of Ti diffusion on the

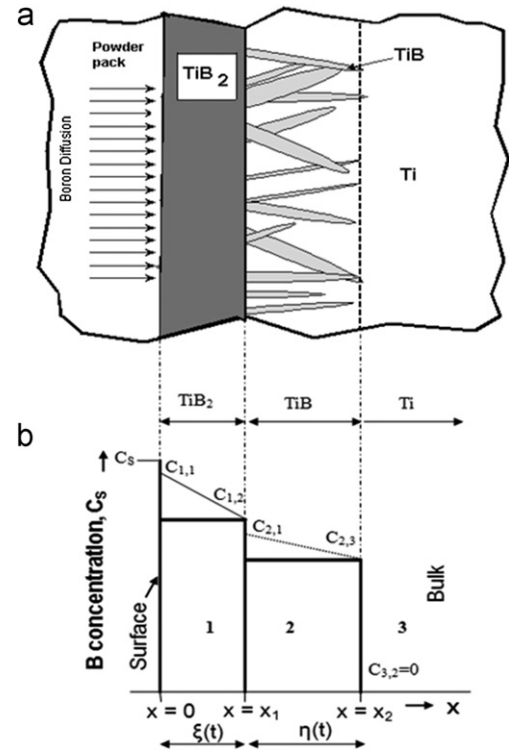


Fig. 7. (a) Schematic of growth of the TiB<sub>2</sub> layer and the TiB whisker layer (b) concentration profile of B across the layers.

boride layer growth can be neglected. The homogeneity range of the TiB<sub>2</sub> and the TiB layers are rather small ( $\sim 1$  at%) and are considered line compounds for all practical purposes. Therefore, it is reasonable to assume that the diffusion coefficient of B is independent of the concentrations in these layers.

With these assumptions, the initial and boundary conditions can be written as:

Initial conditions: ( $t=0$ ).

The effective weight fraction of B in the powder mixture is  $C_S$ , hence,<sup>1</sup>

$$C = C_S = 0.54 \text{ at } x = 0 \quad (2)$$

$$C \text{ (in TiB}_2\text{/TiB)} = 0 \text{ for } x > 0 \quad (3)$$

Boundary conditions: ( $t > 0$ ).

$$C = C_{1,1} = \text{upper limit of B concentration in TiB}_2 = 0.311 \quad (4)$$

$$C = C_{1,2} = \text{lower limit of B concentration in TiB}_2 = 0.301 \quad (5)$$

$$C = C_{2,1} = \text{upper limit of B concentration in TiB} = 0.185 \quad (6)$$

<sup>1</sup>In this model calculation, the B concentrations are taken as weight fractions in all phases. To maintain this consistency, the value of the surface B concentration ( $C_S$ ) was also considered in weight fraction of the powder mixture. Note that the powder mixture consists of a boron source, a transport medium and an activator.

$$C = C_{2,3} = \text{lower limit of B concentration in TiB} = 0.18 \quad (7)$$

$$C = C_{3,2} = \text{B concentration in Ti matrix} = 0 \quad (8)$$

The general solutions for B concentration in the boride layers and for that in Ti matrix which satisfy Eq. (1) are of the form [24,25]:

$$C_i(x, t) = A_i + B_i \operatorname{erf}\left(\frac{x}{2\sqrt{D_i t}}\right) \quad (9)$$

where  $C_i$  and  $D_i$  are the concentration and diffusivity of B in the respective phase (TiB<sub>2</sub>, TiB or Ti).  $A_i$  and  $B_i$  are the respective constants for each phase which need to be determined from the initial and boundary conditions. From Fig. 7(b), defining the time-independent interface boundary positions for TiB<sub>2</sub> and TiB in terms of dimensionless growth-rate parameters  $\xi$  and  $\eta$ , respectively, one can write [24]:

$$x_1 = 2\xi\sqrt{D_1 t} \quad (10)$$

$$x_2 = 2\eta\sqrt{D_2 t} \quad (11)$$

where  $x_1$  and  $x_2$  are the positions of TiB<sub>2</sub>/TiB and TiB/Ti interface boundaries, respectively.  $D_1$  and  $D_2$  are the respective diffusion coefficients of B in TiB<sub>2</sub> and TiB phases. Using Eqs. (10) and (11) and incorporating the initial and boundary conditions [(Eqs. (2)–(8) in Eq. (9)], the variations of concentrations of B in TiB<sub>2</sub> and TiB phases are given by:

$$C_{\text{TiB}_2}(x, t) = C_S - \left(\frac{C_S - C_{1,2}}{\operatorname{erf}\xi}\right) \operatorname{erf}\left(\frac{x}{2\sqrt{D_1 t}}\right) \quad (12)$$

$$C_{\text{TiB}}(x, t) = C_{2,1} - (C_{2,1} - C_{2,3}) \left(\frac{\operatorname{erf}\left(\frac{x}{2\sqrt{D_2 t}}\right) - \operatorname{erf}(\phi\xi)}{\operatorname{erf}\eta - \operatorname{erf}(\phi\xi)}\right) \quad (13)$$

where  $\phi = \sqrt{\frac{D_1}{D_2}}$

During the growth of the layers, simultaneous advancement of the TiB<sub>2</sub>/TiB and TiB/Ti interface boundaries at  $x_1$  and  $x_2$  in a small time step ( $dt$ ) will occur because of the accumulation of B atoms at those interfaces driven by the differences in B flux between TiB<sub>2</sub>, TiB and Ti phases. Hence, applying the rule of mass conservation at the TiB<sub>2</sub>/TiB and TiB/Ti interfaces, one can write [23]:

$$(C_{1,2} - C_{2,1}) \left(\frac{dx_1}{dt}\right) = -D_1 \left(\frac{\partial C_{\text{TiB}_2}}{\partial x}\right)_{x=x_1} + D_2 \left(\frac{\partial C_{\text{TiB}}}{\partial x}\right)_{x=x_1} \quad (14)$$

$$(C_{2,3} - C_{3,2}) \left(\frac{dx_2}{dt}\right) = -D_2 \left(\frac{\partial C_{\text{TiB}}}{\partial x}\right)_{x=x_2} \quad (15)$$

Differentiating Eqs. (10), (12), and (13) and incorporating in Eq. (14) yields:

$$\left(\frac{C_S - C_{1,2}}{\xi\sqrt{\pi}\operatorname{erf}\xi}\right) \exp(-\xi^2) - \frac{(C_{2,1} - C_{2,3})}{\xi\phi\sqrt{\pi}(\operatorname{erf}\eta - \operatorname{erf}(\phi\xi))} \exp(-\phi^2\xi^2) = (C_{1,2} - C_{2,1}) \quad (16)$$

Similarly, differentiating Eqs. (11) and (13) and incorporating in Eq. (15) yields:

$$\frac{(C_{2,1} - C_{2,3})}{\eta\sqrt{\pi}(\operatorname{erf}\eta - \operatorname{erf}(\phi\xi))} \exp(-\eta^2) = (C_{2,3} - C_{3,2}) \quad (17)$$

Eqs. (16) and (17) are non-linear and are to be solved for two unknown parameters,  $\xi$  and  $\eta$ , which are the growth parameters for the TiB<sub>2</sub> and TiB layer, respectively. These equations were solved simultaneously using MATLAB program and  $\xi$  and  $\eta$  were determined for the three treatment temperatures (850 °C, 950 °C and 1050 °C). From the growth parameters, the time-dependent layer thicknesses for the TiB<sub>2</sub> and TiB layers can be calculated using Eqs. (10) and (11), respectively.

An important aspect needs to be considered in comparing the predicted growth rates of the TiB<sub>2</sub> and TiB layers with the experimental data. Because B diffusion occurs during the heating of the samples (10 °C/min) from room temperature to the isothermal treatment temperatures as discussed earlier, there will be some pre-existing layer thickness that is not part of growth at the diffusion temperatures. Hence, this must be subtracted from the experimental data for a meaningful comparison with experiments. To determine the approximate amount of TiB<sub>2</sub>/TiB layer growth during the heat-up period, samples were borided for 5 min at 850 °C, 950 °C and 1050 °C using the same heating rates. The layer thicknesses obtained in these experiments are given in Table 1.

### 3.3. Comparison with experimental data

For the present calculations, the B diffusion coefficients were determined from the work of Fan et al. [29] and are reported in Table 2. The TiB layer growth is accelerated due to the fast diffusion of B in [0 1 0], and therefore, the estimated B diffusivity in TiB is specific to this direction. The diffusivities of Ti in TiB<sub>2</sub> and TiB are 10<sup>3</sup> to 10<sup>4</sup> times lower than that of B in these phases [29–31]. Hence the effect of Ti diffusion on layer growth can be neglected.

Fig. 8 shows the predicted TiB<sub>2</sub> thickness development as a function of time, compared against the experimental data. The experimental data have been corrected for the 5 min growths—the TiB<sub>2</sub> thicknesses, observed after 5 min at the respective temperatures, were deducted from the original thicknesses. A reasonable agreement between the predicted data and the experimental data at 850 °C and 1050 °C can be seen. In most cases, the predicted layer thicknesses of TiB<sub>2</sub> are within 10–20% of the experimental data. But the numerical predictions at 950 °C are slightly higher than the experimental trend. Especially for treatment times exceeding 6 h, the numerical predictions are 20–30% higher than the experimental values. Based on our recent research [23], it was also found that the TiB<sub>2</sub> layer recedes due to a complex mechanism involving enhanced anomalous diffusion in Ti near the  $\alpha/\beta$  phase transition temperature. The temperature region for such anomalous diffusion in Ti can extend up to 950 °C [32]. It is therefore suggested that the small difference (20–30%) between the predicted and the experimental TiB<sub>2</sub> layer thickness at



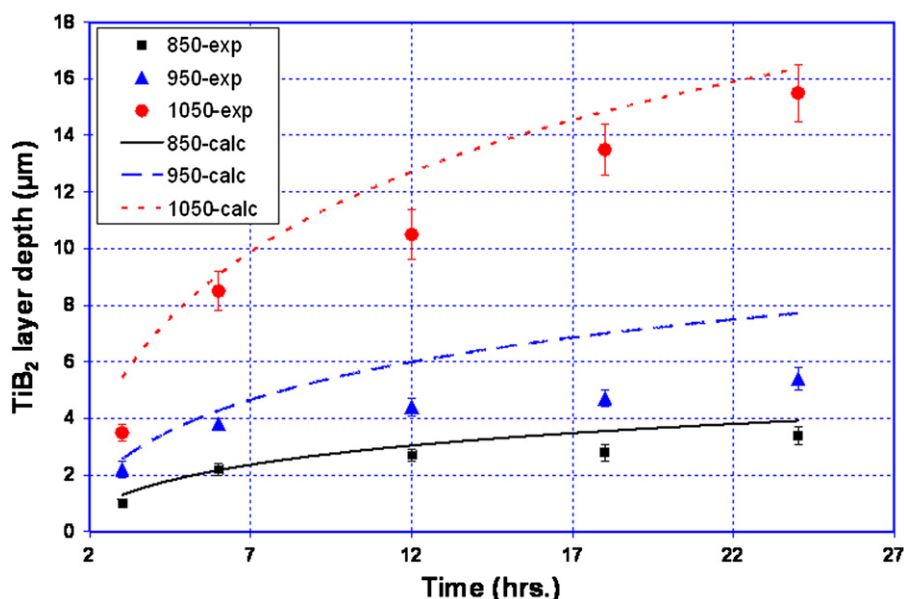


Fig. 8. Comparison of the predicted and the experimentally measured TiB<sub>2</sub> thicknesses, after correcting for the TiB<sub>2</sub> layer growth due to 5 min exposure.

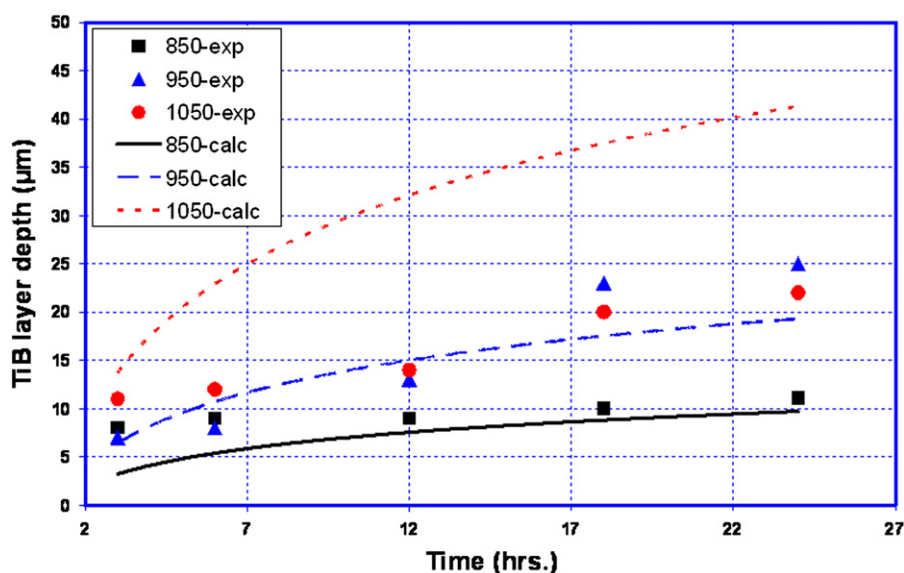


Fig. 9. Comparison of the predicted and the experimentally measured TiB coating layer thicknesses, after correcting for the TiB layer growth due to 5 min exposure.

950 °C, especially at longer boriding times, is due to the TiB<sub>2</sub> layer recession. This effect is absent at 850 °C and 1050 °C and this might explain the agreement of the experimental and the predicted data at these temperatures. It is also to be noted here that the reasonable agreement between the predicted and experimental values of TiB<sub>2</sub> layer thicknesses also negates any argument of oxidation during boriding. If the TiO<sub>2</sub> layer were to have formed and retarded the growth kinetics of the boride layers, the experimental TiB<sub>2</sub> layer thicknesses would have been much lower than the theoretically predicted values at all boriding temperatures. Hence, it appears to be reasonable to conclude that oxidation did not affect boride layer growth kinetics significantly.

Fig. 9 is the comparison of the experimentally measured TiB coating thicknesses (after deducting the TiB thicknesses due to 5 min exposure) and the predicted growth data. The predictions are in reasonable agreement with the experimental data at 850 °C and 950 °C. Most of the numerical data are in the range of 20–25% of that of the experimental values. However, there is a large discrepancy between the predicted and the experimental data at 1050 °C by about a factor of two. Actually, the experimental growth data at 1050 °C, being nearly similar to that at 950 °C, is itself quite unusual. This may be attributed to the thickening of TiB whiskers at high temperatures. While almost all of the TiB whiskers were

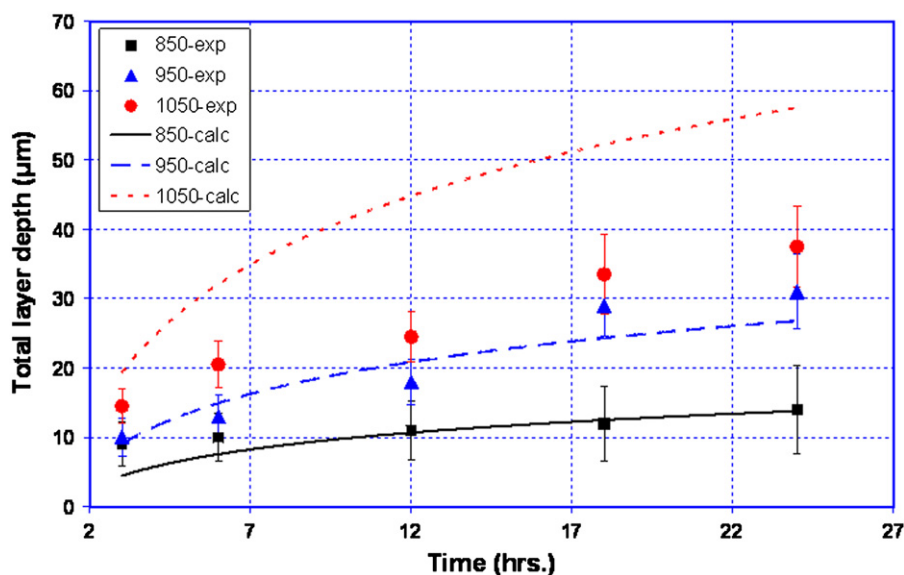


Fig. 10. Comparison of the predicted and the experimentally measured total ( $\text{TiB}_2 + \text{TiB}$ ) coating layer thicknesses, after correcting for the  $\text{TiB}_2$  and the  $\text{TiB}$  layer growth due to 5 min exposure.

relatively thin at 850 °C and 950 °C; at 1050 °C, many  $\text{TiB}$  whiskers in the layer were relatively thicker (Fig. 3). It was suggested earlier [33] that diffusion in the transverse direction of  $\text{TiB}$  whiskers is about 10 times slower than that in the  $[0\ 1\ 0]$  direction, which is the axial direction of whiskers. This means that the rates of thickening and lengthening will be about equal, when the whisker aspect ratio reaches 10. Above this aspect ratio, thickening of  $\text{TiB}$  whiskers provides a faster means of transporting B and reacting with Ti, as opposed to the axial transport and extension of growth along the  $\text{TiB}$  axial direction. Since the model predictions are based only on diffusivities for growth along the  $[0\ 1\ 0]$   $\text{TiB}$  direction, they should not agree with the experimental data of total layer thickness at 1050 °C, if  $\text{TiB}$  whiskers appear to be much thicker than those at lower temperatures. Fig. 3(a and b) indicate that this may be the case—a significant fraction of  $\text{TiB}$  is no longer whiskers and they appear to thicken due to increased B diffusion in the direction transverse to  $\text{TiB}$  whisker axis. Further study of  $\text{TiB}$  thickening will be performed in the future.

Fig. 10 shows the comparison of the total ( $\text{TiB}_2 + \text{TiB}$ ) layer thickness predictions with the experimental data. The predictions for the 850 °C and 950 °C are in reasonable agreement with the experimental data, while at 1050 °C; the predicted thicknesses are relatively higher. This difference arises from the  $\text{TiB}$  layer growth behavior as discussed above.

#### 4. Conclusions

1. Superhard, dual boride layers consisting of a monolithic  $\text{TiB}_2$  layer, followed by a  $\text{TiB}$  whisker layer are formed, with the  $\text{TiB}$  whiskers penetrating normally into the titanium surface during solid state diffusion of B.

2. The thickness of the  $\text{TiB}_2$  layer increases with time and temperature with a relatively higher  $\text{TiB}_2$  layer thicknesses resulting at diffusion temperatures in the  $\beta$ -phase field.
3. The growth rate and the maximum layer thickness attained for the  $\text{TiB}$  whisker layer seem to reach a maximum at 950 °C, which is the closest to the  $\beta$ -transus temperature (913 °C) of all the temperatures studied.
4. X-ray diffraction analysis confirmed the presence of both  $\text{TiB}_2$  and  $\text{TiB}$  layers in all samples irrespective of the boring time and temperature.
5. The total layer thickness is actually dominated by  $\text{TiB}$  whiskers at temperatures 850 °C and 950 °C, whereas at 1050 °C, the  $\text{TiB}_2$  layer becomes a significant fraction of the total layer thickness. This difference is attributed to the diffusivities of B in  $\text{TiB}$ –B transport in the  $\text{TiB}$  axial direction seems to be reduced when the  $\text{TiB}$  whiskers grow too long and this seems to lead to accumulation of B in  $\text{TiB}_2$ , resulting thicker  $\text{TiB}_2$  layer at high temperature.
6. The growth of  $\text{TiB}_2$  as well as that of total ( $\text{TiB}_2 + \text{TiB}$ ) layer was found to obey the parabolic kinetics. Error function solutions were developed based on Fick's second law to predict boride layers growth kinetics. A reasonable agreement between the predictions of these solutions with the experimental data was found in most cases with the exception of when  $\text{TiB}$  whiskers begin to thicken.

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