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Photocatalytic activity under visible light of Fe-doped CeO₂ nanoparticles synthesized by flame spray pyrolysis

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Abstract

 CeO_2 nanoparticles (undoped and Fe-doped) were synthesised using flame spray pyrolysis with varying Fe-dopant concentrations. X-ray diffraction analysis revealed the absence of any impurity phases in all samples. BET (Brunauer, Emmett and Teller) tests showed that the average sizes of undoped and Fe-doped CeO_2 particles were 6.39 and 5.94 nm, respectively. Specific surface area of the particles increased with increasing Fe-dopant concentration. High resolution transmission electron microscopy (HRTEM) revealed that the nanoparticles were either spherical or equiaxed in shape. UV–vis spectroscopy showed a shift of the adsorption edge towards longer wavelengths along with a decrease in the optical indirect band gap from 3.18 to 2.90 eV for undoped particles and 2 mol% Fe-doped particles. In terms of photocatalytic performance, Fe-doped CeO_2 nanoparticles were responsible for an increased degradation of the carbon from formic and oxalic acids. Furthermore, the photocatalytic efficiency was $\sim 100\%$ when 2 mol% Fe-doped CeO_2 particles were used for testing.

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1. Introduction

There have been an increasing experimental focus on characterising cerium dioxide (ceria, CeO₂) which has been identified to possess a unique photocatalytic activity, in addition to high chemical stability, and low biological toxicity. CeO₂ has been used for a wide range of applications, including solar cells, for water purification [1], gas sensors [2,3], and as polishing agents [4]. Furthermore, compared to other metal oxides such as TiO₂, ZnO, and Al₂O₃, CeO₂ has no deleterious effect on human cells [5,6], and therefore use of ceria for photocatalytic applications such as water purification and food packaging will pose minimal risk for

CeO₂ is a large band gap semiconductor with an optical indirect band gap of 3.20 eV [7], which limits its application to within the ultraviolet (UV) radiation range. In order to reduce the band gap and to enhance the photoactivity of CeO₂, transition metals ions of variable valency have been introduced into the CeO₂ lattice viz., iron (Fe) [8], copper (Cu) [9], nickel (Ni) [10], manganese (Mn) [11], cobalt (Co) [12] and silver (Ag) [13]. Of these ions, iron is considered to be one of the most promising candidate, since Fe³⁺ can easily substitute for Ce-ions or enter the interstices of the crystal lattice of CeO₂ [14], leading to the creation of donor or accepter levels between the valence and conduction bands [15].

Several techniques have been used to prepare CeO₂ nanoparticles, including hydrothermal synthesis [16], homogeneous precipitation [17], sonochemical synthesis

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humans. On the other hand, ceria is slightly more expensive, and it is also hygroscopic in nature.

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[18], and flame spray pyrolysis (FSP) [19]. The latter is an attractive, versatile, and practical method to prepare CeO₂ nanoparticles due to several advantages such as low cost, simplicity of operation and experimental setup, capacity for mass production, ease of doping, reproducibility, and rapid particle growth.

Thus, it is clear that the preparation and use of CeO_2 nanopaticles doped with Fe by flame spray pyrolysis would be advantageous; moreover, there is a potential for improving the photocatalytic performance of the material. Therefore, the present work aims: (1) to synthesise CeO_2 nanoparticles doped with Fe using flame spray pyrolysis, and (2) to analyse these particles in terms of their mineralogical and morphological characteristics, and photocatalytic performance.

2. Experimental procedure

2.1. Synthesis of CeO_2 nanoparticles

Cerium nitrate-hexahydrate (Ce(NO₃)₃ · 6H₂O, Sigma-Aldrich, 99.99%) and iron acetyl-acetonate (Fe(C₅H₇O₂)₃, Sigma-Aldrich, 97%) were used as the sources of cerium and iron, respectively. The precursors were prepared by dissolving cerium nitrate-hexahydrate in ethanol solution (Scharlau, 99.9%) at 0.5 M Ce concentration. The Fe-dopant concentrations used were 0.25, 0.50, 0.75, 1.00, 1.50, and 2.00 mol%. During the synthesis process, the precursor was fed into a FSP reactor using a syringe pump at a feed rate of 5 mL/min and the dispersion rate of O₂ was fixed at 5 L/min. The flow rates of combustion gases were fixed at 1.19 and 2.46 L/min for methane and O₂, respectively. The pressure at the nozzle tip was set at 1.5 bars. Finally, the synthesised nanoparticles were collected on a glass microfiber with the aid of a vacuum pump.

2.2. Characterisation

The mineralogy of the nanoparticles was analysed using X-ray diffraction (XRD; Philips X'pert MPD; CuKα radiation; 45 kV; 40 mA; step size 0.02° 2θ; scanning speed $5.5^{\circ} 2\theta$ /min; aluminium sample holder). The mean particle size and specific surface area (SSA) were evaluated using the Brunauer, Emmett, and Teller (BET) nitrogen adsorption method (Quantachrome Autosorp 1 MP; 0.25 g sample; 1 h at 150 °C degassing). High resolution transmission electron microscopy (HRTEM, JEOL JEM-2010; 200 kV accelerating voltage) was used to determine the particle size distribution and particle morphology of the synthesised particles. The amount of dopant present in the synthesised particles was confirmed using energydispersive X-ray spectroscopy (EDS; JEOL JSM-6335F; 15 kV accelerating voltage). The reflectance of nanoparticles (mounted in the recess of a standard aluminium sample support) was obtained using a UV-vis spectrophotometer equipped with an integrating sphere detector (Perkin Elmer Lambda 950, 300-800 nm, monochromatic,

400 nm/min, step size 1 nm). The absorbance spectra were used to calculate the optical indirect band gap using the Schuster–Kubelka–Munk equation [20,21].

2.3. Photocatalytic activity

The photocatalytic performances of nanoparticles were assessed in terms of the decomposition of both formic acid (HCOOH) and oxalic acid (COOH)₂ in a spiral reactor under UV irradiation from a fluorescent lamp (Sylvania fluorescent lamp, 18 W) filtered with a Rosco® E-colour UV filter, as shown in Fig. 1. The radiation was filtered using a double layer of UV cut-off filter (Rosco E-Colour, 360–400 nm).

The spiral reactor conduit included a borosilicate glass tube of dimensions 5 mm OD and 3 mm ID, which was formed into a coil of 50 mm OD and 700 mm length. The light source (30 mm diameter, 700 mm length) was centred within the coil. This assembly was wrapped with an outer layer of aluminium foil as a light shield. The solution was circulated continuously through the conduit using a peristaltic pump (Masterflex Model 7553-79; 7.0 mL/min) with silicone tubing. These conditions resulted in an operating temperature of the recirculating solution of $\sim\!28\,^{\circ}\mathrm{C}.$

Nanoparticles were suspended in a solution of 50 mL ethanol, and then dispersed into a vibra-cell sonicator (Sonics *VCX* 750) for 20 min. The suspension then was loaded into a spiral photoreactor. Oxalic acid or formic acid equivalent to 500 µg carbon was injected into the photocatalytic suspension through the inlet port. The photocatalytic efficiency was determined based on the carbon dioxide (CO₂) generation rate using a conductivity metre (Eutech Instrument *Cyberscan PC* 5500/5000). The overall organic compound degradation process can be summarised in terms following equations [22]:

Oxalic acid:
$$(COOH)_2 + 2OH \cdot \longrightarrow 2CO_2 + 2H_2O$$
 (1)

Formic acid:
$$HCOOH + 2OH \cdot \longrightarrow CO_2 + 2H_2O$$
 (2)

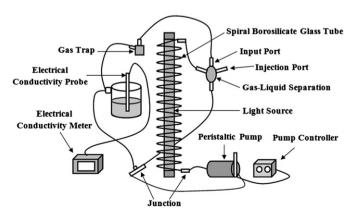


Fig. 1. Schematic of the photocatalytic activity test system.

3. Results and discussion

The XRD patterns shown in Fig. 2 indicate that cerium dioxide with cubic fluorite structure is the only crystalline phase present in both undoped and Fe-doped CeO₂ nanoparticle samples. Potential impurity phases such as Fe₂O₃, FeCeO₃, and FeCe₂O₄ were not observed. Moreover, the peak intensity of (111) plane was seen to decrease with increasing Fe-dopant concentration. This implies that the increasing incorporation of Fe ions into the CeO₂ lattice tends to lower the crystallinity of the latter due to introduction of anharmonicities in the lattice by the foreign cation. The crystallite sizes of the nanoparticles were determined using Scherrer's equation [23] and the values are presented in Table 1. From the table, it is seen that the crystallite sizes decreased with increasing Fedopant concentrations.

The increase in the dopant concentration was observed to lower the crystallite size in addition to decreasing the crystallinity of the nanoparticles (as seen from the decreasing crystallite sizes in Table 1). Moreover, it can be noted that doping CeO₂ with Fe³⁺ can hinder the grain growth as well, and this supports the observance of decreasing crystallite sizes [24,25].

The specific surface area (SSA) of CeO₂ nanoparticles was found to increase with increasing Fe-dopant concentrations as shown in both Fig. 3 and Table 1. This supports the data on the crystallite sizes of the nanoparticles such

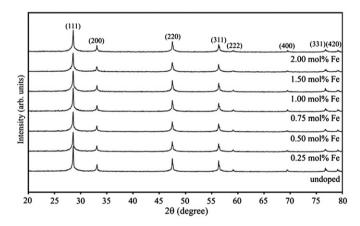


Fig. 2. X-ray diffraction (XRD) patterns of CeO₂ nanoparticles as a function of dopant concentration.

that seen that small particle sizes have greater surface areas.

The BET equivalent particle size was determined using the following equation [26]:

$$d_{\rm BET} = \frac{6}{\rho_{\rm CeO_2} \times \rm SSA} \tag{3}$$

where $d_{\rm BET}$ is the mean BET diameter, $\rho_{\rm CeO_2}$ is the bulk density of CeO₂ (≈ 7.215 g/cm³) [27] and SSA is the Specific surface area

The particle size of CeO₂ is shown in Table 1. In general, the crystallite size is not equal to the actual particle size due to agglomeration effects in the latter [28]. However, these results show that particle sizes are very close in value to the crystallite sizes; and this clearly indicates that the particles synthesised are single crystals [29].

Fig. 4 shows the high resolution transmission electron microscopy (HRTEM) images of Fe-doped CeO₂. The images clearly demonstrate that undoped and Fe-doped CeO₂ nanoparticles are spherical or equiaxed in shape. The distribution of particle diameters calculated from HRTEM micrographs has been found to be in the range of 6.25–10 nm for undoped CeO₂ and 5.00–6.25 nm for 2 mol% Fe-doped CeO₂. These results support the crystallite size measurements and BET results which showed that increasing Fe-dopant concentrations result in a lowering of the particle sizes of CeO₂.

Semi-quantitative elemental analysis of the Ce, O, and Fe concentrations were carried out using energy dispersive

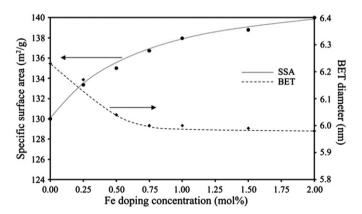


Fig. 3. Variation in the specific surface area (SSA) and BET particle size of CeO₂ nanoparticles as a function of the dopant concentration.

Table 1 Summary of analytical data.

Parameters	Dopant concentration (mol% Fe)						
	0.00	0.25	0.50	0.75	1.00	1.50	2.00
Crystallite size (nm)	7.15	6.70	6.65	6.60	6.41	6.31	6.22
Particle size (BET diameter, nm)	6.39	6.23	6.16	6.08	6.02	5.99	5.94
Particle size (TEM, nm)	6.25-10.00	7.50-9.50	6.50-9.00	6.50-9.00	5.00-6.25	5.00-6.25	5.00-6.25
Specific surface area (SSA, m ² /g)	130.00	133.38	135.00	136.73	137.97	138.80	140.00
Fe concentration(at%)	0.00	0.19	0.36	0.63	0.96	1.38	1.73
Energy band gap (eV)	3.18	3.13	3.10	3.06	3.00	2.98	2.90

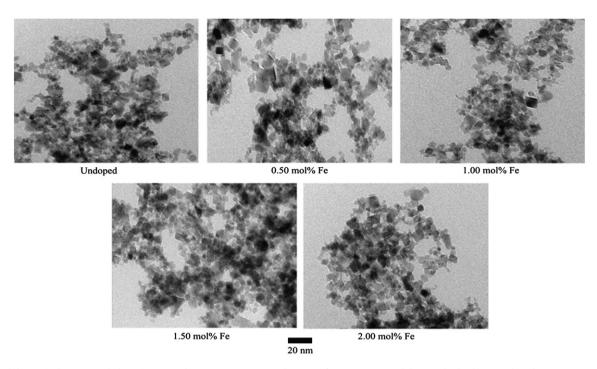


Fig. 4. High resolution transmission electron microscopy (HRTEM) images of CeO₂ nanoparticles synthesised at varying dopant concentrations.

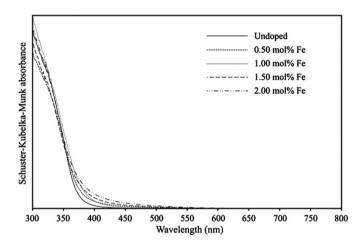
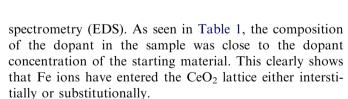


Fig. 5. Schuster–Kubelka–Munk absorbance plot of CeO₂ nanoparticles as a function of dopant concentration.



The Schuster-Kubelka-Munk absorbance data were calculated from UV-vis reflection data using the following equation [20,21]

$$\frac{F(R_{\infty}) = (1 - R_{\infty})^2}{2R_{\infty}} \tag{4}$$

where $F(R_{\infty})$ is proportional to the absorption constant of the material at a particular wavelength R_{∞} is the reflectance of the sample (%)

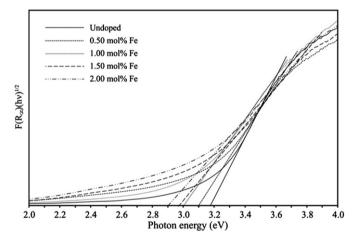


Fig. 6. Optical indirect band gaps of CeO₂ nanoparticles as a function of dopant concentrations.

The plot of $F(R_{\infty})$ vs. wavelength of CeO_2 nanoparticles is shown in Fig. 5. The spectra show that the adsorption edge shifted towards longer wavelengths (red-shift) with increasing Fe-dopant concentration. Fig. 6 shows the optical indirect band gaps of CeO_2 nanoparticles, and this figure suggests that an increase in the dopant concentration results in a lowering of the optical indirect band gap. The lowest band gap value is seen in the case of the 2.00 mol% Fe-doped CeO_2 nanoparticles.

The reason for the enhanced performance in the case of doped CeO_2 is due to the fact that the addition of Fe ions results in the formation of interstitial sites which in turn create new energy levels (impurity energy levels) between the valence and conduction bands [30]. The impurity energy levels allow for intrinsic band gap excitation under

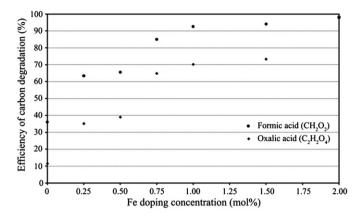


Fig. 7. Variation in the efficiency of formic and oxalic acid degradation by CeO_2 nanoparticles at varying dopant concentrations.

visible light region, and this implies that the higher energy state of 3d-electrons from Fe-cation dopants can be excited to the conduction band of CeO₂ [31], thereby enhancing its photocatalytic performance.

The photocatalytic efficiency of CeO₂ nanoparticles was calculated by measuring the CO₂ gas formed as a byproduct of formic or oxalic acid degradation. Fig. 7 shows the variation in the efficiency of CeO₂ nanoparticles as a function of the dopant concentration. From this figure, it is clearly seen that the efficiency of degradation of carbon is enhanced at increasing Fe-dopant concentrations.

Comparing the formulae for formic acid (HCOOH) and oxalic acid (COOH)₂, it is seen that the efficiency of carbon degradation in formic acid is greater than the case for oxalic acid at low Fe-dopant concentrations. However, at 2 mol% Fe, the efficiencies of acid degradation were similar i.e. $\sim 100\%$ for both acids. The reasons for this are due to the following: (1) the defects on the catalyst surface formed during synthesis can trap and prevent electron–hole recombination [32], thereby lowering recombination rates, (2) the increase in surface area can provide more sites for adsorption of organic atoms on the surface of the CeO₂ particles, and (3) decreasing optical indirect band gaps can enhance the light absorption of CeO₂ nanoparticles, and thereby enhance the photocatalytic performance leading to the degradation of organics.

4. Conclusions

The present work has successfully synthesised Fe-doped CeO₂ nanoparticles using the flame spray pyrolysis method. The CeO₂ nanoparticles produced were of cubic fluorite structure with no impurity phases present. The BET results showed that the CeO₂ particles sizes decreased from 6.39 nm (undoped) to 5.94 nm (2.00 mol% Fe-dopant). Moreover, the SSA increased with increasing Fe-dopant concentration. HRTEM analysis revealed that the nanoparticles were either spherical or equiaxed in appearance.

The shifting of the absorption edge in visible region towards longer wavelengths was found in the case of Fedoped CeO₂ nanoparticles, and this lowered the optical indirect band gap of CeO₂ nanoparticles from 3.18 eV (undoped) to 2.90 eV (2.00 mol% Fe-dopant). Under visible light irradiation, the efficiency of formic and oxalic acid degradations by Fe-doped CeO₂ nanoparticles was superior to that of undoped nanoparticles. Furthermore, the photocatalytic performance of 2 mol% Fe-doped CeO₂ nanoparticles resulted in almost complete degradation of both formic and oxalic acids.

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