

# Grain growth in BaTiO<sub>3</sub> ceramics assisted by an intergranular glass film

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## Abstract

This research demonstrates that BaTiO<sub>3</sub> ceramics exhibit increased grain boundary mobility ( $M_b$ ) triggered by an inter-granular glass film (IGF) as previously demonstrated in polycrystalline Al<sub>2</sub>O<sub>3</sub> ceramics conversion to single-crystal sapphire upon annealing at high temperatures. These results suggest that secondary abnormal grain growth (SAGG) during sintering of BaTiO<sub>3</sub> ceramics at 1365 °C, a temperature above the eutectic points in the BaTiO<sub>3</sub>–SiO<sub>2</sub> and BaTiO<sub>3</sub>–TiO<sub>2</sub> systems, is another example of faster  $M_b$  caused by IGF. Higher  $M_b$  magnified through an interface glass film of several nanometers thickness facilitates a faster grain growth rate that produces exceedingly large grains of ~2.4 mm in size. The growth mechanism involving twin-plane re-entrant (TPRE) corners may not be the only route responsible for SAGG in BaTiO<sub>3</sub>, particularly when sintered at above eutectic temperatures. How this abnormal grain growth occurs through mechanisms involving liquid-phase-enhanced  $M_b$  and the {111} twins as a chemically induced growth fault is discussed.

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## 1. Introduction

Extraordinarily large grains of several centimeters in size were obtained [1–3] when nearly stoichiometric BaTiO<sub>3</sub> powder (i.e., slightly TiO<sub>2</sub>-excess of Ba/Ti=0.999) infiltrated with a slurry containing 1 mol% of SiO<sub>2</sub> and TiO<sub>2</sub> was sintered at 1350 °C for 8 h in air [1]. A similar discovery was made by Yamamoto et al. [4] several years earlier who also used slightly TiO<sub>2</sub>-excess powder in sintering. A route preparing BaTiO<sub>3</sub> single crystals through solid-state crystal growth from polycrystalline BaTiO<sub>3</sub> was suggested. Although the growth mechanism for BaTiO<sub>3</sub> was not addressed specifically [4], it was a similar process resembling the conversion of polycrystalline alumina into single-crystal sapphire [5–7] where a minute amount of liquid phase [7] may have played a decisive role. In order to differentiate from the conventional abnormal grain growth (AGG), this exceptional behavior observed [1–4] in BaTiO<sub>3</sub> was termed the secondary abnormal grain growth (SAGG). In contrast, conventional AGG leading to the microstructure of a bimodal grain size distribution [8] in

BaTiO<sub>3</sub> where large grains are usually lamellar in shape is referred to as the primary abnormal grain growth (PAGG).

Two key factors that catalyzed SAGG in BaTiO<sub>3</sub> were proposed [1–3]: (1) the presence of the {111} double-twin grains, and (2) infiltration with SiO<sub>2</sub> prior to sintering. However, they are mutually related because it was also suggested [1,2] that adding SiO<sub>2</sub> promotes the formation of the {111} double-twin grains. These twin grains then provide the twin-plane re-entrant edges (TPRE) or corners that facilitate perpetuated growth [9–11] of BaTiO<sub>3</sub> grains to enormous sizes [1–3]. The mechanism was often called TPRE [1–3]. The argument necessitates that TPRE edges, which are the sites enabling two-dimensional (2D) nucleation, are maintained throughout by heat treatment. The 2D nucleation on TPRE edges is kinetically favorable because it requires considerably less activation enthalpy ( $\Delta H_T$ , where the subscript T represents TPRE) than that on an atomically flat surface ( $\Delta H_F$ , the subscript F for flat grain surface). TPRE therefore unleashes a burst out of the nuclei and a growth rate surge leading to unusually large grains.

Munoz-Saldana et al. [12] reproduced SAGG in SiO<sub>2</sub>-infiltrated BaTiO<sub>3</sub> which was heat-treated at 1260 °C/10 h followed by rising to 1320 °C/5 min, but second phase

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BaTiSiO<sub>5</sub> derived from the BaTiO<sub>3</sub>–SiO<sub>2</sub> liquid eutectic formed at 1260 °C was detected. Double-twin grains although seen in the SiO<sub>2</sub>-penetrated region did not exhibit nucleation-favorable [9–11] TPPE corners.

We report on grain growth in BaTiO<sub>3</sub> ceramics sintered at 1215 °C, 1265 °C, and 1365 °C in air using both BaO-excess and TiO<sub>2</sub>-excess powders. The latter two temperatures are higher than the eutectic points in the BaTiO<sub>3</sub>–SiO<sub>2</sub> (at 1260 °C [12,13]) and BaTiO<sub>3</sub>–TiO<sub>2</sub> (at 1332 °C [14]) systems. Experimental results suggest that SAGG is promoted by greater boundary mobility enhanced by a thin liquid film at the interface of growing grains in initially TiO<sub>2</sub>-excess BaTiO<sub>3</sub>. The likelihood that this grain growth mechanism is induced chemically by the {111} growth twins whose boundary is a planar fault is also discussed.

## 2. Experimental procedure

Commercial BaTiO<sub>3</sub> powders (Ticon™ HPB®, Ferro Electronic Material Systems, Penn Yan, NY, USA) prepared via an advanced oxalate route according to the manufacturer, of TiO<sub>2</sub>-excess (of Ba/Ti=0.9889, Lot no. 738,  $D_{50}$ =300 nm) and BaO-excess (of Ba/Ti=1.0007, Lot no. EXP4763,  $D_{50}$ =256 nm) compositions were used in this study. The major impurities are SiO<sub>2</sub>, SrO, MgO, CaO, Fe<sub>2</sub>O<sub>3</sub>, Na<sub>2</sub>O, and K<sub>2</sub>O. SiO<sub>2</sub> is most relevant to the present study, which amounts to ~121 ppm (wt.) and ~60 ppm (wt.) in the TiO<sub>2</sub>-excess and BaO-excess powder, respectively.

The powders were ball-milled using Y<sub>2</sub>O<sub>3</sub>-stabilized ZrO<sub>2</sub> balls with alcohol in a polyurethane jar to break up agglomerates before passing through a 125 µm sieve to remove the remaining large ones. A suitable quantity of powders was die-pressed at 100 MPa into disks of 10 mm diameter and ~2 mm thickness using a WC-inserted steel die and punch to make single-layer samples. Double-layer samples consist of BaO-excess single-layer disc on the top with TiO<sub>2</sub>-excess single-layer disc beneath it. They were prepared using single-layer discs pre-pressed at 5 MPa before stacking one on top of the other and pressing again at 100 MPa. Samples were packed with either TiO<sub>2</sub>-excess or BaO-excess powder, and made to sit in a high-purity Al<sub>2</sub>O<sub>3</sub> crucible for sintering at desired temperatures in air using 5 °C/min heating rate before being furnace-cooled to room temperature.

Sintered samples were polished successively using diamond-lapping films, and completed with DuPont™ Syton™ to obtain ~30 nm surface roughness. Polished sections were chemical-etched in a 70% HCl solution added with a few drops of HF to delineate the grain boundaries and ferroelectric domains. Sintered microstructure was examined using reflected light optical microscopy (OM, Nikon, AVK-C2, Tokyo, Japan), scanning electron microscopy (SEM, JEOL™ SEM-6330, Tokyo, Japan) operating at 20 kV, and transmission electron microscopy (TEM, JEOL™ AEM-3010) operating at 300 kV. Both SEM and TEM are equipped with energy-dispersive spectroscopy (EDS, Link Systems, Oxford Instruments, Oxford, UK) for micro-chemical analysis. The average grain size was determined using Optimas® (v6.1,

Optimas Co., 1987). A focused ion beam (FIB) instrument (SMI-3050, Seiko, Tokyo, Japan) was used for preparing thin foils because specific locations in samples were required for close examination under TEM.

## 3. Results

### 3.1. TiO<sub>2</sub>-excess samples sintered at 1215 °C and 1265 °C

Fig. 1(a) shows the SEM secondary electron image (SEI) that reveals [8] how PAGG occurs during TiO<sub>2</sub>-excess powder sintering at 1215 °C. Small grains coarsened to particle chains [15] through neck formation are dispersed in a matrix of lamellar {111} twin grains grown from ~10 µm to large sizes of ~15–20 µm by Ostwald ripening when sintering was extended from 20 h to 55 h, 100 h (Fig. 1(a)), and to 300 h [8]. It represents how the microstructure of TiO<sub>2</sub>-excess powder sintered at < 1260 °C, the lowest eutectic temperature of 1260 °C [12,13] in the BaTiO<sub>3</sub>–SiO<sub>2</sub> system was developed, knowing that SiO<sub>2</sub> is an inevitable trace impurity in the initial powder. After annealing for 100 h, lamellar grains coarsened at the expense of small grains and evolved into a skeletal microstructure [8] resembling a house of cards. An intergranular (or interface) glass film (IGF) of ~1.2 nm, which is liquid at the sintering temperature, determining using Digital Micrograph™ (v3.7.4, 1996, Gatan™, Pleasanton, CA, USA),

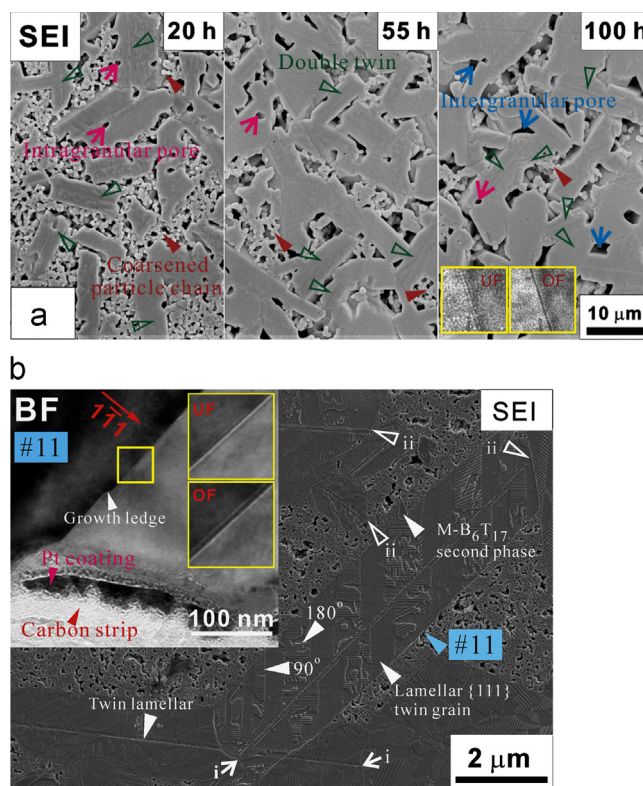


Fig. 1. Sintered microstructure of TiO<sub>2</sub>-excess powder: (a) PAGG from 1215 °C/10 h, 55 h, and 100 h (courtesy of Dr. Ming-Hong Lin), and an IGF ~1.2 nm was detected and shown in the inset, (b) PAGG from 1265 °C/20 h (SEM-SEI) where an IGF of ~0.9 nm exists between lamellar grains and the matrix shown in the inset (UF: under focus, OF: over focus, TEM-BF image).



was detected in foil #1, as shown in the inset of SEI for the 100 h samples. Microstructure features of AGG are represented by some residual pores entrapped in the grain interior, producing the distinct grain sizes (Fig. 1(a)). Although double-twins in a considerable quantity (indicated in Fig. 2(a)) are identified, no SAGG occurs. Even after prolonged sintering for 300 h [8], skeletal microstructure of double-twins and residual pores persisted.

Sintering at 1265 °C/20 h results in a bimodal grain size distribution (Fig. 1(b)) representing PAGG. This is typical of TiO<sub>2</sub>-excess powder sintered at temperatures slightly higher than the lowest eutectic point of ~1260 °C [12,13]. Suggestion is that the liquid eutectic involves in developing the microstructure feature. It contains mostly the characteristic {111} double-twin grains grown to the lamellar shape of high-aspect ratio that are scattered in a low sintered density matrix. These twin grains very scarcely contain residual pores. Only occasionally are the TPRES edges (indicated as (i) in Fig. 1(b)) from double-twinned grains thought to sustain perpetual growth

[9–11] observed. Other twin lamellae have grown to ridges [9–11], or impinged mutually where the TPRES corners [1–3] were lost (indicated by (ii)).

The 90 ° and 180 ° ferroelectric domains (as indicated) are characterized by herring-bone and water-mark patterns, respectively; observed in the lamellar grains are the representative features of tetragonal-BaTiO<sub>3</sub> ceramic [16]. Second phase monoclinic-Ba<sub>6</sub>Ti<sub>17</sub>O<sub>40</sub> can easily be identified by its dark contrast under SEM-SEI, which is formed when excess TiO<sub>2</sub> reacts with BaTiO<sub>3</sub> in solid-state [14]. Residual pores are found predominantly in areas among twin lamellae (Fig. 1(b)) where the microstructure is represented by neck formation and grain coarsening into particle chains [15].

The bimodal microstructure shown in Fig. 1(a) and (b) is often addressed in the literature as PAGG; the densification of both samples is enhanced by eutectic liquids formed at ≤1265 °C. An IGF of ~0.9 nm thickness is determined adopting the Fresnel under-focus (UF) and over-focus (OF) imaging technique [17], as shown in the inset of Fig. 1(b).

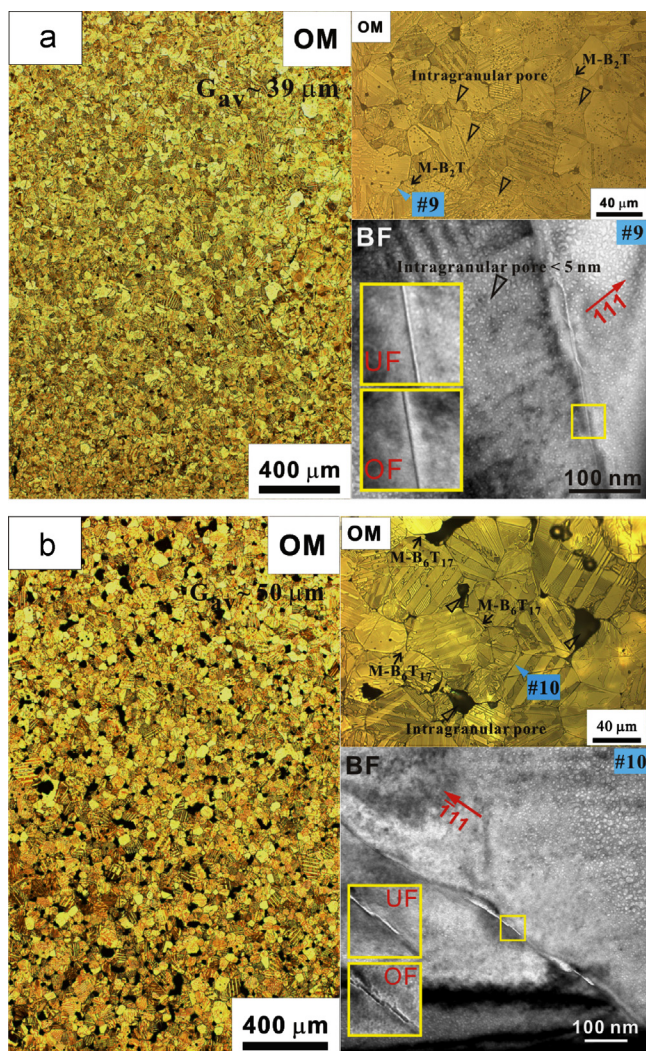


Fig. 2. Reflected light OM microstructure of (a) BaO-excess, (b) TiO<sub>2</sub>-excess single-layer samples sintered at 1365 °C/20 h in air, with higher magnifications shown in the inset. Respectively.

### 3.2. Embedded single-layer samples sintered at 1365 °C

When samples were sintered at 1365 °C/20 h, higher than the lowest eutectic of 1332 °C in the BaTiO<sub>3</sub>–TiO<sub>2</sub> pseudo-binary system [14], the resultant microstructures of non-stoichiometric compositions (Fig. 2(a) for BaO-excess sample and Fig. 2(b) for TiO<sub>2</sub>-excess sample) do not differ significantly. The fact that both samples are characterized by polygonal grains with rounded corners suggests a liquid-phase sintering mechanism. Monoclinic-Ba<sub>2</sub>TiO<sub>5</sub> (B<sub>2</sub>T) and monoclinic-Ba<sub>6</sub>Ti<sub>17</sub>O<sub>40</sub> (B<sub>6</sub>T<sub>17</sub>) second phases are detected by X-ray diffractometry (patterns not shown) in two single-layer samples. TiO<sub>2</sub>-excess sample (Fig. 2(b)) has a larger average grain size of  $G_{av}=50\ \mu\text{m}$  compared to  $G_{av}=39\ \mu\text{m}$  of BaO-excess sample (Fig. 2(a)), although the latter of lower sintered density is apparent from the more extensive residual pores (Fig. 2(b)).

BaO-excess sample containing large grains with intragranular residual pores suggests AGG (Fig. 2(a)). On the other hand, for TiO<sub>2</sub>-excess sample it may be described as NGG (Fig. 2(b)) with residual pores still located at grain junctions, but in fact it consists of abnormal grains which have consumed the matrix grains and grown to larger sizes (~50 μm). Nevertheless, the grain size distribution of the two samples can be characterized by a normal distribution representing mono-modal in contrast to a bimodal in the solid-state sintered (Fig. 1(a)), or in liquid-assisted sintered (Fig. 1(b)) TiO<sub>2</sub>-excess samples. An IGF of ~1.3 nm (Fig. 2(a)) and ~2.8 nm thickness (Fig. 2(b)), correspondingly, was found to exist along grain boundaries from samples of both compositions.

A superfluous quantity of intra-granular pores of very small size, i.e. <5 nm, and irregular shape (not faceted [18]) is observed in both samples (foil #9 in Fig. 2(a) and #10 in Fig. 2(b)).



### 3.3. Two-layer samples embedded in BaO-excess powder sintered at 1365 °C

The cross-section microstructure of double-layer samples, embedded in BaO-excess powder and sintered at 1365 °C/1 h, is represented by Fig. 3; each layer at higher magnifications is shown in juxtaposition. Three regions across the sample thickness can immediately be discerned from the distinctive grain sizes. Surface region (region I) contains grains uniform in size ( $G_{av}=40\text{ }\mu\text{m}$ ) but smaller than those of region II; AGG is observed in both regions where intra-granular pores are discerned. Although region II contains grains grown to an average size  $G_{av}=294\text{ }\mu\text{m}$ , region III shows extensive coarsening with the relative density remaining at  $\rho_{rel}<80\%$  whose microstructure is characterized by ubiquitous necking with NGG where intragranular pores are rarely observed. Similar to Fig. 2(b), it may also be that they are AGG grains ( $\sim 20\text{ }\mu\text{m}$ ) which have grown at the expense of smaller matrix

grains. The microstructure resembles that observed in areas among the twin lamellae from samples of a similar composition but sintered at 1265 °C/20 h (Fig. 1(b)). Only region III not exhibiting the AGG characteristics may be described as NGG.

After prolonged sintering, the initially BaO-excess layer is similarly divided into two regions, region I and II (Fig. 4). The microstructure consists of polygonal grains after sintering was extended to 20 h. Regions made to FIB-foils are indicated in #'s corresponding to those in Table 1.

Grains in both region I and II contain intra-granular residual pores which is indicative of AGG, only that the average grain size differs significantly by  $G_{av}=42\text{ }\mu\text{m}$  in region I and  $G_{av}=263\text{ }\mu\text{m}$  in region II. Grains containing the {111} double-twin (as indicated) have a number frequency of  $\sim 53\%$  in region I where those within an area of  $\sim 1\times 1\text{ mm}^2$  were counted. Although residual pores entrapped in grain interior suggest that AGG has already begun, grains are still

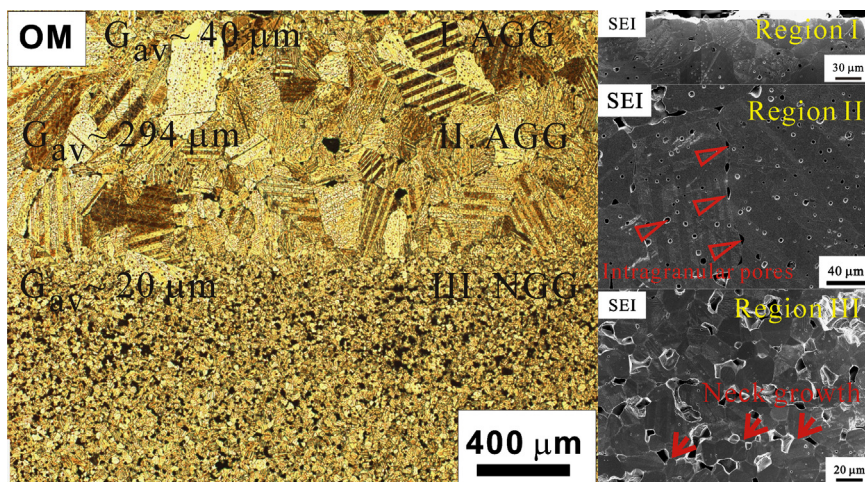


Fig. 3. Cross-section microstructure of two-layer sample sintered at 1365 °C/1 h. An overview reveals three regions of distinct grain sizes (reflected light OM), AGG in region I, and region II, and NGG and coarsened microstructure (SEM-SEI).

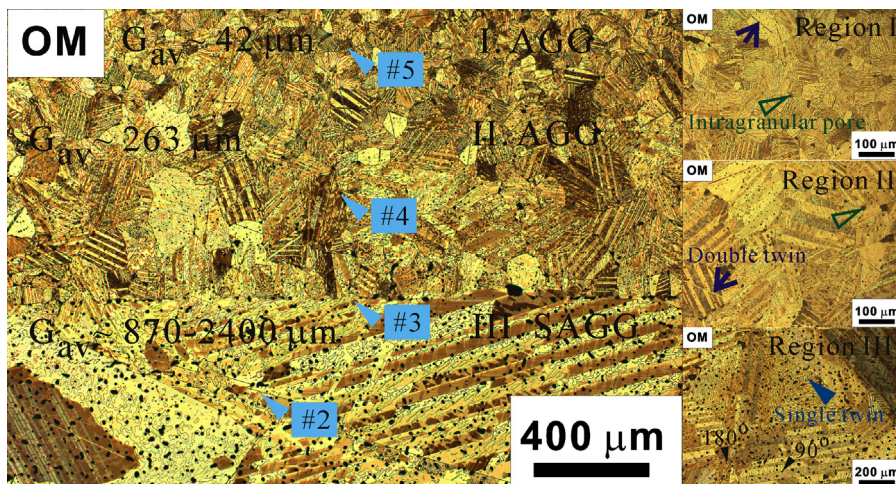


Fig. 4. Cross-section microstructure of two-layer sample embedded in BaO-excess powder and sintered at 1365 °C/20 h. An overview reveals three regions of distinct grain sizes with corresponding area at high magnifications showing AGG in region I, and region II, and SAGG in region III (reflected light OM).

Table 1  
Thickness of IGF and FIB-foil positions of the corresponding sample.

Foil#	1	2	3	4	5	6	7	8	9	10	11	12
Sintering conditions	1215 °C/100 h	1365 °C/100 h	1365 °C/20 h			1365 °C/20 h	1365 °C/20 h	1365 °C/20 h	1365 °C/20 h	1365 °C/20 h	1265 °C/20 h	
Ba/Ti ratio	0.9889	1.0007				0.9889	0.9889		1.0007	0.9889	0.9889	
Interface and grain boundary with $G_{av}$ ( $\mu\text{m}$ )	Bimodal	2400	AGG-SAGG	263	AGG-AGG	215	70	250	AGG-AGG of 40	NGG-NGG of 50	PAGG-NGG	TPRE
IGF (nm)	1.2	3.0	1.5	0.8	1.4	2.1	0.9	1.7	1.3	2.8	0.9	1.2
Boundary feature	Faceted	Faceted with glass pockets				Faceted	Faceted		Faceted with ledges		Faceted	
Sample type	Single-layer	Double layer	Double layer			Single-layer	Double layer	Double layer	Single-layer	Single-layer	Double layer	

rather uniform in size (Fig. 4) where the size distribution has not changed abruptly into a bimodal function.

Relative to those in region I, grains in region II have grown significantly. However, the number frequency of finding a {111} double-twinned grain at ~50% is almost the same. Ubiquitous residual pores are entrapped in grain interior, although some residual pores still remain located at triple grain junctions and along grain boundaries (as indicated in region II).

The microstructure of region III of the initially  $\text{TiO}_2$ -excess layer is represented very distinctly by extraordinarily large grains. They have grown to sizes between ~870 and 2400  $\mu\text{m}$  ( $G_{av}$ =1330  $\mu\text{m}$ ) where intra-granular residual pores are profuse. The number frequency of finding a {111} double-twinned grain decreases to ~33%. Abnormally large grains containing intra-granular residual pores are the characteristic SAGG microstructure. Nevertheless, SAGG grains are not restricted to growing from double-twins, and single-twin boundaries [12] are indicated.

The Ba/Ti ratios determined using EDS from an average of five grains from regions I, II and III in Fig. 4 are 1.4164: 1.4322: 1.4162. Due to the overlapped EDS energy lines of Ba ( $L\alpha$ =4.465 keV) and Ti ( $K\alpha$ =4.508 keV), the results show considerable discrepancies with Ba/Ti=1.0007 and 0.9889 of the initial powders. However, they also suggest that the composition is being homogenized between layers upon sintering.

### 3.4. Two-layer samples embedded in $\text{TiO}_2$ -excess powder sintered at 1365 °C

The sintered microstructure is divided into two layers with distinct grain sizes (Fig. 5), resembling Fig. 4, after sintering at 1365 °C/20 h. The BaO-excess layer-I reveals that double-twin grains do not necessarily lead to SAGG (as indicated), particularly when the re-entrant edges grow into ridges, as indicated. Further, not only are SAGG grains in the  $\text{TiO}_2$ -excess layer not as extensive as those shown in Fig. 4, but also large SAGG grains of e.g. ~1100  $\mu\text{m}$  in size (layer-II in Fig. 5) remain surrounded by smaller grains (~70–100  $\mu\text{m}$ ). Besides, SAGG grains containing single-twin are often detected, as indicated.

### 3.5. Inter-granular glassy films

All grain boundaries examined under TEM contain a thin IGF. The thicknesses from eleven positions are  $\leq 3.0$  nm, as shown in Table 1. No dependence of  $G_{av}$  and thickness was found immediately.

Four grain boundaries (#2–#5) from two-layer sample shown in Fig. 4 were made to thin foils using FIB. Only one boundary (foil #3) is shown representatively for OF and UF images. Bright-field (BF) image of IGF at AGG-SAGG boundary (foil #3, Fig. 6) connecting a series of glass pockets shows that it is of ~1.5 nm thickness, shown in the inset. The high-resolution image of foil #3 shown in the inset (Fig. 6) confirms the IGF thickness determined by the Fresnel



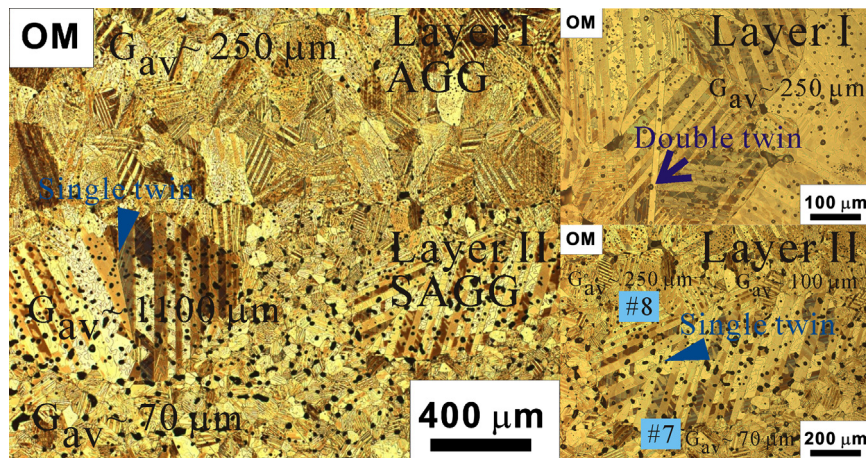


Fig. 5. Cross-section microstructure of two-layer sample embedded in  $\text{TiO}_2$ -excess powder and sintered at  $1365^\circ\text{C}/20\text{ h}$ . An overview suggests two regions of distinctive grain sizes with corresponding area at high magnifications of AGG in region I and region II, and SAGG in region II (reflected light OM).

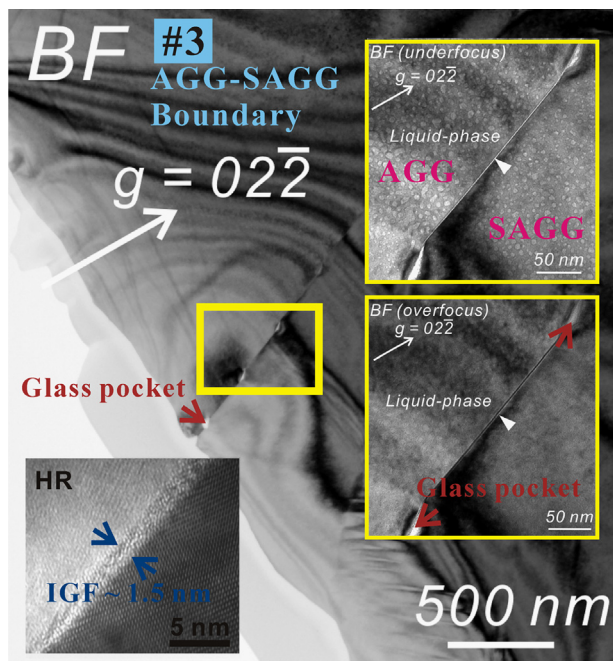


Fig. 6. IGF of  $\sim 1.5\text{ nm}$  thickness along AGG–SAGG interface (foil #3) (UF: under focus, OF: over focus, TEM-BF and high-resolution images). The locations of interfaces analyzed are indicated in Fig. 4.

technique [17]. And, IGF is  $\sim 3.0\text{ nm}$  thickness at boundary (foil #2) containing growth ledges between two SAGG grains. The wetting angle of  $\phi=0^\circ$  permits the eutectic liquid to penetrate into grain boundaries and spread over all grain surfaces.

Preparing FIB foils from TPRES edges was only successful after a few attempts. SEM indicating where the foil was made and TEM revealing the existence of IGF at the edges are shown in Fig. 7.

Numerous nano-scale intra-granular pores of  $< 5.0\text{ nm}$  size are again found in both grains across IGF in SAGG–SAGG and AGG–SAGG (Fig. 6) boundaries. This is strong evidence that residual pores were swept across by fast migrating

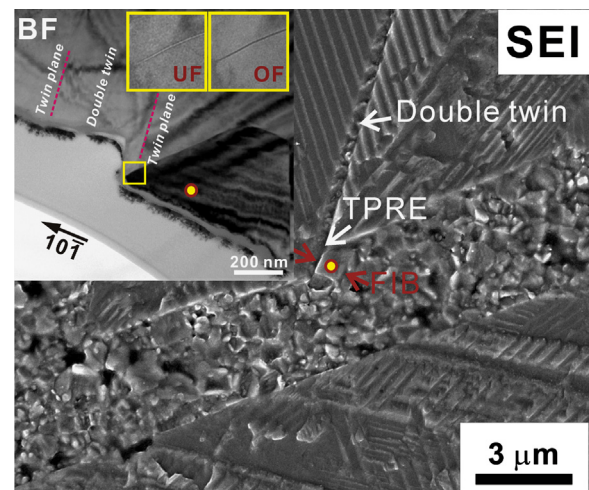


Fig. 7. Position of a TPRES edge shown indicated in SEM-SEI, and the presence of IGF at  $\sim 1.2\text{ nm}$  revealed by TEM-BF image (UF: under focus, OF: over focus).

boundaries containing liquids, a unique feature of AGG in ceramics. Growing  $\text{BaTiO}_3$  single crystals via the SAGG route would suffer a major setback in crystal's quality [4].

## 4. Discussion

### 4.1. TPRES mechanism

Previous reports [1–3,9,10] suggested that perpetuated growth via TPRES during SAGG relies on the availability of the re-entrant corners provided by the  $\{111\}$  double-twin lamellae. It was claimed that when single-twin crystals grow into ridges, [9–11] they become less favorable for 2D nucleation, and consequently GG stops. The present observation does not entirely support this view because SAGG still occurs with single-twin grains [12], e.g., Fig. 5, because  $\text{TiO}_2$ -excess samples although containing  $\{111\}$  double-twins did not develop to SAGG even after annealing for 100 h (Fig. 1(a)) and 300 h [8] at  $1215^\circ\text{C}$  ( $< 1260^\circ\text{C}$ ). TPRES assumed [20]

that nucleation is rate-controlled for grains growing from melts, [19,20] or vapor phase [20]. While in Ostwald ripening, as happens here, either interface reaction (i.e. solution or reprecipitation) or diffusion in liquid phase may have been the rate-controlling step.

The number frequency of {111} double-twins grains is reduced from 53%, 50% of the AGG layer to 33% of the SAGG layer (Fig. 4). This may have indicated that the {111} twins grew among themselves facilitating SAGG. On the other hand, SAGG did not occur in single-layer samples regardless of the composition (Fig. 2(a) and (b)), neither in region I nor in region II of BaO-excess layer, even if they contained a sufficient quantity of double-twin grains (Fig. 4). Therefore, SAGG grains containing {111} single twins [12] (Fig. 5) suggest that 2D nucleation through TPPE is not the only mechanism responsible for SAGG in BaTiO<sub>3</sub>. Examining TPPE edges from a double-twin lamellar grain corner, IGF (Fig. 7), serves as strong evidence that SAGG is encouraged by the presence of liquid phase.

#### 4.2. Boundary mobility

The present results suggest that similar to Al<sub>2</sub>O<sub>3</sub> [7,21], SAGG in BaTiO<sub>3</sub> is another convincing example of higher  $M_b$  magnified by a liquid grain boundary phase. Higher  $M_b$  facilitates faster GG rate and produces huge grains of ~2400  $\mu\text{m}$  (2.4 mm) size (Fig. 4).

When a liquid film is present in polycrystalline ceramics, the boundary mobility ( $M_b$ ) can be described [22] by

$$M_b = \frac{D_1 C_1 \Omega}{\omega kT} \quad (1)$$

where  $D_1$  is the diffusivity in liquid which is related to the viscosity ( $\eta$ ) and particle radius ( $R$ ) using the Stokes–Einstein equation  $D_1 = kT/6\pi R\eta$ ,  $C_1$  the solubility in liquid,  $\Omega$  the atomic volume,  $\omega$  the IGF thickness, and  $kT$  has its usual meaning.

The existence of IGF along the AGG–SAGG grain boundary (foil #3 in Fig. 6) is strongly supportive to the suggestion that the fastest moving boundaries in polycrystalline Al<sub>2</sub>O<sub>3</sub> are impure and disordered [7,21]. According to Eq. (1), reducing IGF's thickness increases  $M_b$  direct-proportionally. However, IGF thicknesses detected from the interfaces ranging between ~0.9 and 3.0 nm (Table 1) do not differ significantly to completely justify the higher  $M_b$  (Eq. (1)) that leads to SAGG and extraordinarily large BaTiO<sub>3</sub> grains. Although IGF enhances  $M_b$ , it alone may not satisfactorily explain the SAGG in BaTiO<sub>3</sub>. Even the glass viscosity (Eq. (1)) depending on the IGF composition may account for changes in  $M_b$ , and other causes must be sought.

#### 4.3. Chemically induced grain growth via 2D faults

Anisotropic grain growth along directions parallel to the c-plane in ZnO ceramics is attributed [23] to the head-to-head inversion-domain boundaries (IDB) where the polar directions ( $\pm c$ ) have slower  $M_b$  than the non-polar directions. Similarly, the Ruddlesden–Popper (R–P) grains dispersed in the SrTiO<sub>3</sub>

matrix are also characterized by a lamellar shape extending parallel to the (001) plane [24]. The R–P phase containing an interleaved rock-salt SrO-layer may be seen as the crystallographic shear (CS) structure.

When IGF and its effects on  $M_b$  cannot be ruled out in these ceramics, anisotropically grown grains also commonly contain planar faults. The {111} growth twins in BaTiO<sub>3</sub> [25] as a 2D growth fault containing a 2H (hexagonal in Ramsdell's notation) stacking sequence [25], and oxygen vacancies [26] may serve equivalently to facilitate AGG and PAGG (Fig. 1(a) and (b)), although not SAGG. The suggestion is that crystallographic faults such as IDB, growth twins, and the CS structure have non-stoichiometric compositions [24,25] or stacking faults [25,27] that provide favorable growth sites at low sintering temperatures, e.g., 1215 °C (Fig. 1(a)) and 1265 °C (Fig. 1(b)) where eutectic liquids are not of significant amount to cover all grain boundaries. The AGG behavior may thus be termed as “chemically induced” planar growth. Nevertheless, grains [8] (Fig. 1(a)) did not coarsen into large sizes (Figs. 4 and 5) as in SAGG even after prolonged sintering for 100 h, and 300 h [8].

When sintering temperature is raised above 1265 °C (@1290 °C [28]), the characteristic {111} lamellar twin grains disappeared. That the {111} twin lamellae are altered into polygonal grains with the twinning retained is a common observation [28,29] in BaTiO<sub>3</sub> ceramics. It appears that the chemically induced growth mechanism is not conciliatory when the liquid phase is present. The AGG mechanism changes from that induced by growth faults (Fig. 1) to enhanced  $M_b$  by the liquid phase (Figs. 4 and 5) when liquid phase has a significant quantity, e.g.,  $T > 1265$  °C or with BaO-excess, that its effect on  $M_b$  becomes predominant. Examples of liquid-phase-enhanced growth in grains containing no crystallographic faults are indeed found in many other systems, e.g., MgAl<sub>2</sub>O<sub>4</sub> spinel [30], Al<sub>2</sub>O<sub>3</sub> [31], and Si<sub>3</sub>N<sub>4</sub> [32].

## 5. Conclusions

AGG including PAGG and SAGG in BaTiO<sub>3</sub> ceramics is examined in sintered BaTiO<sub>3</sub> ceramics via microscopic observation using OM, SEM and TEM.

TPPE may not be the only mechanism that leads to SAGG in BaTiO<sub>3</sub> ceramics. Similar to converting polycrystalline Al<sub>2</sub>O<sub>3</sub> into single-crystal sapphire, SAGG in BaTiO<sub>3</sub> through Ostwald ripening necessitates faster boundary mobility via IGF. The IGF between ~0.9 and 3.0 nm thickness significantly increases  $M_b$ . However, it alone cannot fully account for the grain growth rate that produces extraordinarily large grains. Although a synergistic effect combining narrow IGF with lower viscosity eutectic liquids, higher diffusivity and higher solubility in the liquid may all contribute to the mobility enhancement that facilitates SAGG, further studies are necessary.

An AGG mechanism involving chemically induced growth faults, i.e., the {111} growth twins, may also have a role in instigating PAGG, particularly at low-temperature sintering



when the liquid phase exists in small quantities. At higher sintering temperatures, e.g.,  $T > 1265\text{ }^{\circ}\text{C}$ , liquid-phase-enhanced  $M_b$  contributes more significantly to SAGG in BaTiO<sub>3</sub> ceramics. A sufficient quantity of BaO is necessary for the ternary eutectic reaction with trace impurity SiO<sub>2</sub> to catalyze SAGG. This additional BaO is supplied by embedding TiO<sub>2</sub>-excess BaTiO<sub>3</sub> samples in BaO-excess powder during sintering.

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