

Synthesis and characterization of lead zirconate titanate (PZT) obtained by two chemical methods

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Abstract

Lead zirconate titanate (PZT) was synthesized at the ratio of $\text{Zr/Ti}=52/48$ using two synthesis methods: the polymeric precursor method (PPM) and the microwave-assisted hydrothermal method (MAHM). The synthesized materials were characterized by X-ray diffraction (XRD), scanning electron microscopy (SEM), particle size distribution by sedimentation, hysteresis measurements and photoluminescence (PL). The results showed that PZT powders are composed of tetragonal and rhombohedral phases. Different particle sizes and morphologies were obtained depending upon the synthesis method. From the hysteresis loop verified that PZT powders synthesized by the PPM have a typical loop of ferroelectric material and are more influenced by spatial charges while particles synthesized by the MAHM have a hysteresis loop similar to paraelectric material and are less influenced by spatial charges. Both samples showed PL behavior in the green region (525 nm) whereas the sample synthesized by the PPM showed higher intensity in spectra.

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1. Introduction

Perovskite ceramics based on lead represent the main class of ferroelectric materials used commercially in the form of multilayer capacitors, piezoelectric transducers, pyroelectric detectors and optical sensors [1–3]. Among these ceramics, PZT is the most efficient and widely applied material [4,5]. These ceramics properties are strongly influenced by the density and microstructure which depend upon the procedure of synthesis and the powder processing [6]. Furthermore, the morphotropic phase boundary (MPB) [7] is an essential parameter to be considered because in this region tetragonal and rhombohedral phases coexist, and consequently the properties of these materials are improved (e.g., piezoelectric properties).

A PZT perovskite structure is distorted below 350 °C [8] (Curie temperature). When this structure has Zr^{4+} in position B (the center of the unit cell), the PbZrO_3 rhombohedral phase is evident. However, when Ti^{4+} occupies the B site of structure, the tetragonal phase of PbTiO_3 appears [9]. Both phases are ferroelectric and consequently exhibit spontaneous polarization [6,10]. The position of charge centers in the unit cell is crucial because in a polarizable material, the centers can be shifted relative to each other which results in a charge-induced dipole in the unit cell that produces characteristic ferroelectricity. When centers of positive and negative charges are at different positions within the unit cell in the absence of any charges and have a permanent dipole, the cell has spontaneous polarization [11]. In ferroelectric materials, the spontaneous polarization can be reversed by applying an electric field (the coercive field) (E_c). For higher fields which extend to the saturation polarization (P_s) and upon removal of the applied field, the polarization does not return to the null value. This phenomenon is defined as remanent polarization (P_r), and it is represented by the hysteresis loop [6].

PZT can be synthesized by different methods, and different morphologies can be obtained [12–15]. The PPM is often used

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to synthesize perovskites, particularly the PZT [15,16]. This method promotes the polyesterification of cation chelates which form a resin of high viscosity and decrease the cation segregation during thermal decomposition [17]. However, in the fabrication of PZT ceramics, PbO volatility at high temperatures can occur which causes a fluctuation in the PZT composition. Usually an excess precursor which contains lead is used to correct this loss [4,18]. Today, another method which is commonly used to obtain these materials is the MAHM; it has been increasingly reported in the literature. This method has shown advantages such as lower energy consumption, a low temperature, a rapid heating process due to the direct interaction of radiation with water as well as a consequent acceleration of the crystallization process [19,20]. Several materials with different structures have been synthesized by the MAHM. Moura et al. synthesized ZnO with a flower-like shape [18]; Volanti et al. obtained CuO with sea urchin-like morphology [21]; and Teixeira et al. obtained PZT plate-like structures [22].

This study compares the influence of both methods on PZT powders characteristics, especially their ferroelectric and PL properties. The materials obtained in each synthesis also were characterized by XRD, SEM and particle size distribution. The best response of these powders relative to each other was evaluated from measurements.

2. Experimental procedure

2.1. Synthesis methods

Powders of $\text{Pb}(\text{Zr}_{0.52}\text{Ti}_{0.48})\text{O}_3$ (PZT) have been synthesized by the PPM and by the MAHM. The reagents used were: Pb $(\text{NO}_3)_2$ (Mallinckrodt; 99.7%), $\text{ZrOCl}_2 \cdot 8\text{H}_2\text{O}$ (Merck; 99.95%), TiO_2 (Vetec; 99.8%), KOH (JT Baker; 87.2%), ethylene glycol (Aldrich; 99.5%), standard solutions of zirconium and titanium citrates and citric acid (Synth; 99.5%).

2.1.1. Synthesis by PPM

For this synthesis, a solution of zirconium and titanium citrates with known concentrations was used to prepare PZT powders in the ratio Zr/Ti of 52/48 [18]. This mixture was homogenized with constant stirring and heating (approximately at 90 °C) [17]. Due loss of organic matter in this method, an excess quantity (5%) of aqueous solution of Pb $(\text{NO}_3)_2$ was added to assure the stoichiometry, followed by citric acid. A clear solution was obtained, and ethylene glycol was added for the formation of a polyester. The molar ratio of lead: citric acid: ethylene glycol was 1:4:16 mol. Then the polyester was calcined at 400 °C to eliminate organic matter, and the resulting material was heat-treated at 600, 700 and 800 °C for 3 h.

2.1.2. Synthesis by MHAM

For this synthesis, a commercial microwave furnace (MARCH-CEM, USA) was used operating in a frequency of 2.45 GHz and 600 W. An aqueous suspension containing Pb $(\text{NO}_3)_2$, $\text{ZrOCl}_2 \cdot 8\text{H}_2\text{O}$ and TiO_2 was prepared, and a solution

of KOH (1.8 mol L^{-1}) was added which resulted in a final concentration of 0.31 mol/L PZT. This precursor suspension was maintained at room temperature under constant stirring and was completely solubilized in the middle of the reaction with the assistance of the pressure and control temperature provided by microwave furnace. The KOH is a mineralization agent, which assists the reactants mass transport during the formation of seeds in the crystallization process and it also contributes to the crystal nucleation and the growth process, resulting in accelerating the reaction. Approximately 30 mL of this suspension was placed in a Teflon vessel with a capacity of 90 mL. The fill to 30% of the Teflon vessel volume ensured maximum pressure and efficiency. The Teflon vessel was sealed and placed in the microwave furnace and heated at 180 °C for 2 h. After synthesis, the light yellow precipitate was formed which is separated from the residual solution by centrifugation and washed with distilled water until a neutral pH was obtained; then it was dried at room temperature.

2.2. Characterizations

The materials were characterized by XRD (Rigaku, model D/Max-2500/PC) using $\text{CuK}\alpha$ radiation in the 2θ range from 20° to 80° with 0.02°/min, FE-SEM (JEOL, JSM-7500F). The particle size distribution of PZT powders was analyzed by sedimentation velocity centrifugation using an X-ray beam (X-ray Disc Centrifuge System Model BI-XDCW Particle Sizer Analyzer). PZT powders were compacted in the form of pellets with uniaxial pressure of 27.6 MPa then isostatic pressure of 210 MPa. After this process the samples were placed in alumina boat and PbO powder was added in the amount of 5% of the weight of sample. The alumina boat was sealed with alumina paste to prevent the loss of lead by volatilization, and placed in a tubular furnace at 1200 °C for 3 h and heating rate of 10 °C/min.

After sintering, the pellets were weighed, and the diameter and thickness were measured. Then they were polished to calculate the relative density of the samples from the theoretical density. For hysteresis measurements (Equipment Radiant Technology RT6000 HVA using an amplifier with the maximum potential difference of 4000 V), an electric field of 3 MV/m was applied to the pellets (with thickness around 1.0 mm) at a constant frequency of 10 Hz. PL spectra were collected with a Thermal Jarrel-Ash Monospec 27 monochromator and a Hamamatsu R446 photomultiplier. The 350 nm exciting wavelength of a krypton ion laser (Coherent Innova) was used on the pellets, with the nominal output power of the laser maintained at 550 mW.

3. Results and discussion

Fig. 1 shows XRD patterns of the powders obtained by the PPM and calcined at different temperatures and by MAHM. XRD pattern peaks can be consistently indexed by the tetragonal structure (card JCPDS #33-0784) and also by the rhombohedral structure of the PZT (card JCPDS #73-2022). This result was expected because the molar ratio of

Zr/Ti (52/48) used in this work is within the morphotropic phase boundary [23] which ensures the coexistence of the two crystalline structures of PZT. Also, XRD pattern powder peaks synthesized by the PPM become better defined with an increase in the calcination temperature which indicates an increase in crystallinity of these materials.

Fig. 2 shows FE-SEM images of PZT powders obtained by PPM calcinated at different temperatures (see Fig. 2a–c) and by MAHM (see Fig. 2d). Note that the powder prepared by PPM is composed of micro-sized rounded particles; this structure forms large agglomerates. In addition, the size of this particle increases with an increase in the calcination

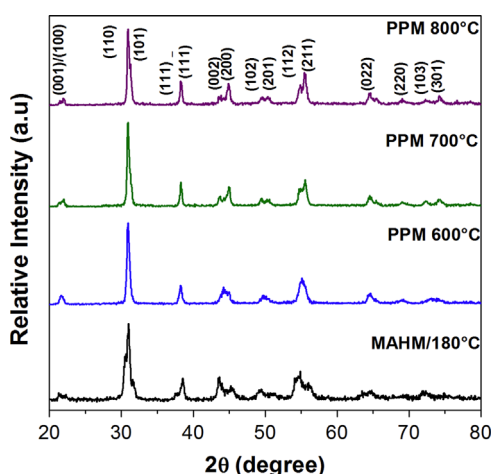


Fig. 1. XRD patterns of PZT powders obtained by the PPM and calcined at 600, 700 and 800 °C and by MAHM at 180 °C/2 h.

temperature, but agglomerates have no significant variation in size. On the other hand, the powder prepared by the MAHM is composed of micro-sized cubes, and these structures do not form large agglomerates because they are not subjected to the calcination process.

Powders obtained by the two synthesis methods were analyzed according to the particle size distribution. Fig. 3a–c shows the particle size distribution histogram of PZT powders synthesized by the PPM and calcinated at different temperatures. This analysis confirms that approximately 64% of particle sizes range from 1.1 to 1.7 μm , 81% of the particle sizes range from 1.25 to 1.75 and 58% of the particle sizes range from 1.3 to 1.7 μm at the calcination temperatures of 600, 700, and 800 °C, respectively. Fig. 3d is associated with PZT powders synthesized by the MAHM. About 80% of the particle sizes are between 1.25 and 3.25 μm . However, as viewed by FE-SEM (see Fig. 2a–d), the particles were agglomerated, so the size range obtained is related to the particle agglomerates and not isolated particles. The agglomerate size range has no significant variation according to the temperature increase which occurs because the temperature increase promotes the growth of particle sizes and not agglomerate sizes [24].

As the ferroelectric property is related to the density of the material, the PZT powder density obtained by the two synthesis processes was investigated. Table 1 shows the green density and the density after the sintering process. These data refer to the average of three samples made for each synthesis method. The green powder density of both synthesis methods are similar (approximately 60% of pure PZT found in the

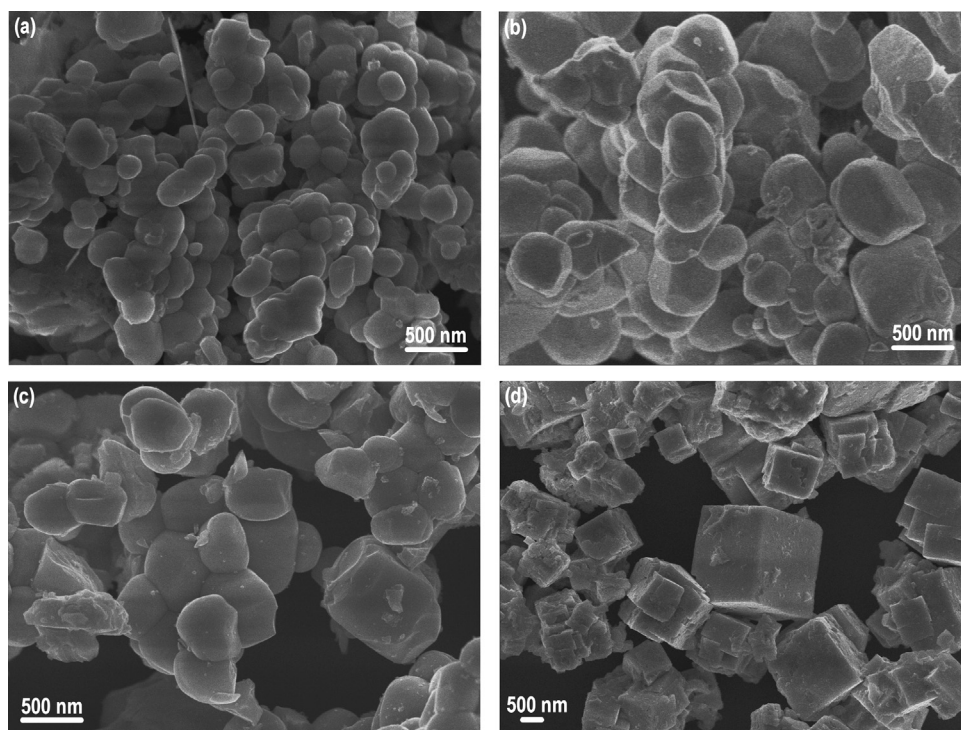


Fig. 2. FE-SEM of PZT powders synthesized by the PPM and calcined at different temperatures: (a) 600; (b) 700; (c) 800 °C; and (d) PZT powder synthesized by the MAHM concentration of 0.31 mol L⁻¹ at 180 °C for 2 h.

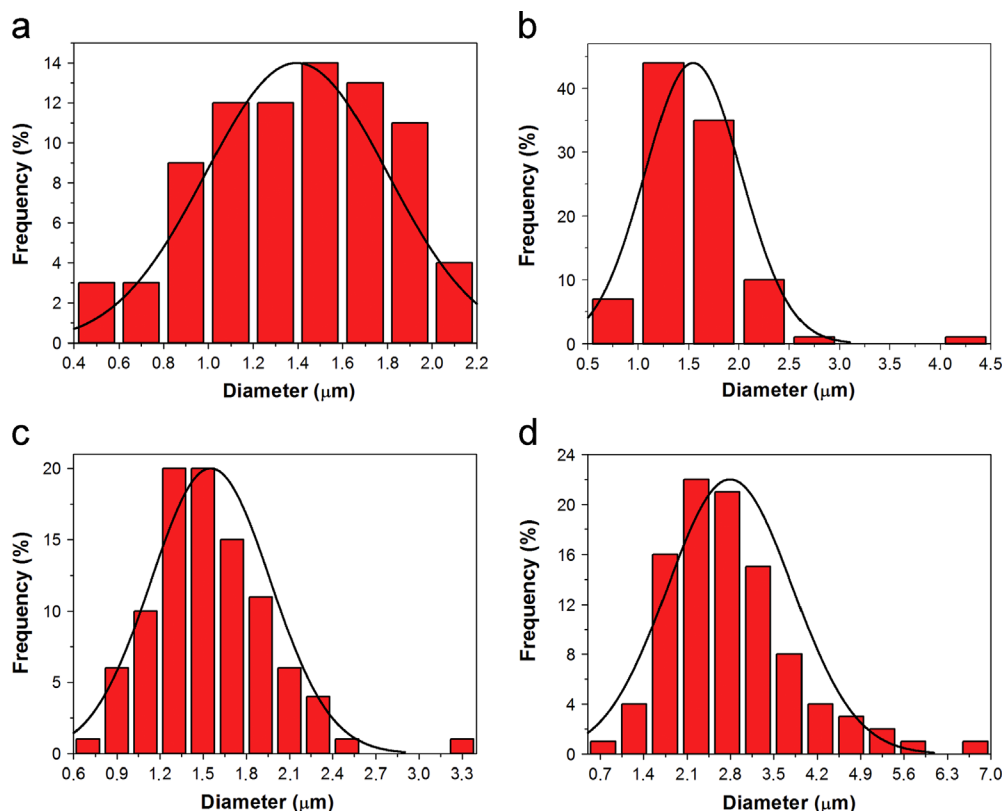


Fig. 3. Particle size distribution histograms of PZT powder obtained by the PPM with calcination temperatures of: (a) 600; (b) 700; and (c) 800 °C for 3 h. In the (d) histogram of PZT particle size distribution obtained by the MAHM at 180 °C for 2 h.

Table 1
Green density of PZT pellets and density after sintering.

Sample	Green density (g/cm ³) and (%)	Density after sintering (g/cm ³) and (%)	Mass loss (%)
PZT (PPM)	4.81 → 60.9	7.20 → 91.2	5.8
PZT (MAHM)	4.42 → 56.0	7.21 → 91.3	2.9

literature—7.9 g/cm³) [25]. The same result occurs after the synthesis process (approximately 91% of theoretical density) (see Table 1).

Fig. 4 shows hysteresis loops obtained for the PZT powders by different synthesis methods. Considering that at low frequencies the contribution of spatial charges are visible, hysteresis measurements were performed at 10 Hz to investigate the influence of spatial charges on ferroelectric effects. Note that powders prepared by the PPM present a typical ferroelectric material loop and show remanent polarization (P_r) of 7.2 μC/cm² (see Fig. 4a) while for the powders prepared by the MAHM, reveal a characteristic loop of paraelectric materials (see Fig. 4b) and P_r cannot be observed. These results can be related to the spatial charges contribution for ferroelectric effect due to a smaller defect concentration on PZT powders prepared by the MAHM which we believe is consequence of the morphological influence obtained by this method.

Fig. 5 shows PL spectra at room temperature obtained for PZT powders synthesized by the PPM and the MAHM after

excitation with a 350 nm laser light. A broad PL emission with the maximum at around 525 nm is verified. The higher intensity is for PZT powders prepared by the PPM in relation to the samples prepared by the MAHM. The lower PL of samples obtained by MAHM indicates that it is more ordered. Although the powders synthesized by both the methods are in the same phase, PZT structures obtained by the MAHM are more symmetrical than PZT structures obtained by the PPM, and consequently the PL intensity is lower.

The order can be related to the presence of ideal $[\text{PbO}_{12}]_o^x$, $[\text{ZrO}_6]_o^x$ and $[\text{TiO}_6]_o^x$ clusters or $[\text{PbO}_{12}]_o'$, $[\text{ZrO}_6]_o'$ and $[\text{TiO}_6]_o'$ electron polaron while disorder can be related to presence defective $[\text{PbO}_8]_d^x$ or $[\text{PbO}_7\text{V}_o^x]$, $[\text{ZrO}_6]_d^x$ or $[\text{ZrO}_5\text{V}_o^x]$ and $[\text{TiO}_6]_d^x$ or $[\text{TiO}_5\text{V}_o^x]$ clusters [26]. More recently, the cluster-to-cluster charge transfer (CCCT) process in a crystal containing more than one kind of cluster is characterized by excitations involving electronic transitions from one cluster to another cluster. The vacancy left behind by the electron polaron in an otherwise ideal cluster is termed a “hole polaron” which has all the attributes of an electron polaron except for being positively

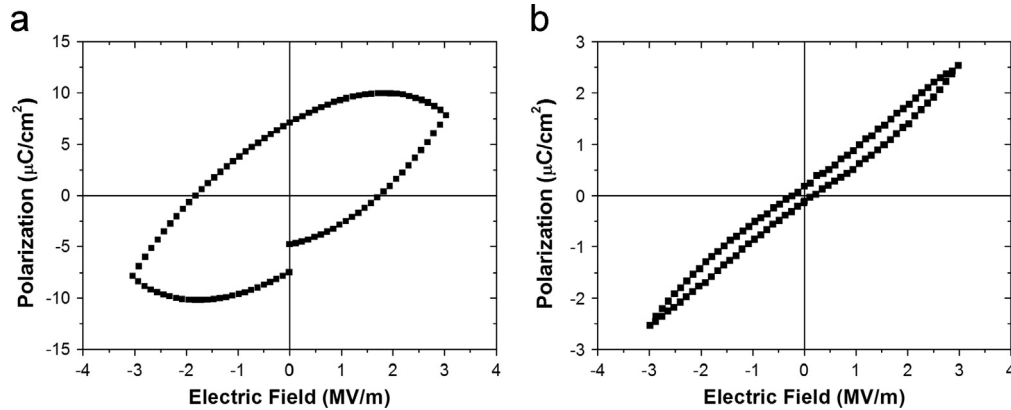


Fig. 4. P – E hysteresis loops for PZT. In (a) PZT pellet obtained by PPM and (b) PZT pellet obtained by MAH.

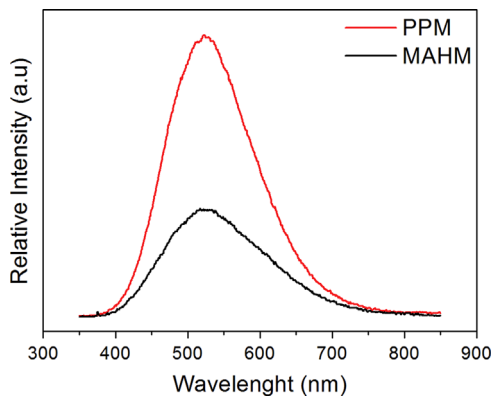
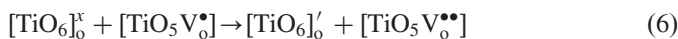
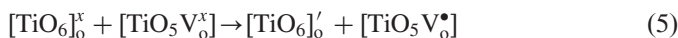
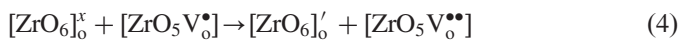
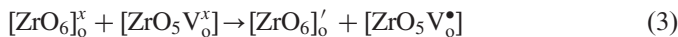
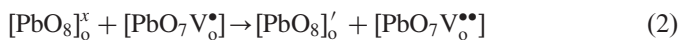
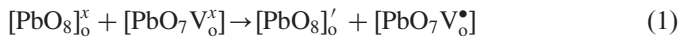


Fig. 5. PL spectra at room temperature of PZT powders obtained by the PPM and the MAHM.

charged, and hence there is a coulomb attraction between the electron/hole.

The CCCT process provides direct insight into charge carrier dynamics in materials. Hole polaron trap states are localized at oxygen anions in both bulk and surface, oxygen vacancies in a disordered structure with $[\text{PbO}_8]_o^x/[\text{PbO}_7\text{V}_o^x]$, $[\text{ZrO}_6]_o^x/[\text{ZrO}_5\text{V}_o^x]$, and $[\text{TiO}_6]_o^x/[\text{TiO}_5\text{V}_o^x]$ complex clusters [27] are hole trapping centers according to the following equations:



Structural and electronic reconstructions of all possible combinations of clusters belonging to a specific crystal are essential for the understanding of the CCCT process and its influence on the PL and on ferroelectric effects (see Fig. 4b); as the system evolves to a higher structural order, there is a decrease in

defect densities which is caused by the transformation of a $\text{V}_o^{\bullet\bullet}$ to V_o^\bullet and subsequently the V_o^x oxygen vacancy in clusters [26] charge redistribution may promote a electron–hole recombination of localized excitons.

4. Conclusions

In this study, the influence of the synthesis method on morphology and on ferroelectric and PL properties of PZT powders was observed. XRD patterns confirm that PZT phases co-exist in the morphotropic phase boundary with different synthesis methods. FE-SEM images showed that particles with round and cubic forms were obtained by PPM and the MAHM, respectively.

Spatial charges have more influence on powders obtained by the PPM as verified by the formation of hysteresis loops that look round. PL spectra measurements verified a higher intensity in powders synthesized by the PPM; powders obtained by the MAHM were more ordered and contributed to low emission spectra. However, in both synthesis methods, powders show intense PL spectra in the green region (around 525 nm). The influence of the synthesis method on the formation of defects is confirmed by PL spectra and can also be correlated with hysteresis loop measurements. The two techniques complement each other and contribute to the understanding of phenomena related to the defect density and the existence of spatial charges in these materials.

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