

# Investigation on low loss $(1-x)$ $\text{Mg}_{0.95}\text{Co}_{0.05}\text{TiO}_3$ – $(x)$ $\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$ composite series for achieving a nearly zero temperature coefficient of resonant frequency

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## Abstract

This report presents the characteristic properties of  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{TiO}_3$  (MCoT)– $\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$  (CLT) composite series, for achieving a material with large dielectric constant ( $\epsilon_r$ ), a high quality factor ( $Q \times f$ ) and nearly zero temperature coefficient of resonant frequency ( $\tau_f$ ). By the help of Rietveld refinement method it is observed that the combination of MCoT (ilmenite-structured) and CLT (perovskite-structured) forms a two-phase system. The microwave dielectric properties have been measured using the Hakki–Coleman resonator method. The values of density,  $\epsilon_r$  and  $\tau_f$  have been theoretically obtained using existing models. A new material  $0.80\text{Mg}_{0.95}\text{Co}_{0.05}\text{TiO}_3$ – $0.20\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$ , possessing an excellent combination of dielectric properties with  $\epsilon_r$  of 25.85,  $Q \times f$  of 80,040 GHz (at 8.05 GHz) and  $\tau_f \sim 0$  ppm/°C at 1300 °C, is investigated as a suitable material for microwave applications.

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**Keywords:** Lichtenecker logarithmic model; Mixture rule;  $\text{MgTiO}_3$ – $\text{CaTiO}_3$ ; Temperature coefficient of resonant frequency

## 1. Introduction

The development of microwave communication systems requires materials which can be used as resonators in filters, antennas and oscillators at microwave frequencies in radar detectors, cellular telephones and global positioning satellite (GPS) devices [1,2]. In recent years several types of dielectric ceramic materials have been developed and investigated to match with the requirements of dielectric resonators [2]. For this the material must have three basic properties: high dielectric constant ( $\epsilon_r$ ), low dielectric loss or high quality factor ( $Q \times f$ ) and near-zero temperature coefficient of resonant frequency ( $\tau_f$ ) at microwave frequencies [3]. This is because some of the key elements integrated within the dielectric in the high frequency circuits, such as filters and resonators need to be very stable against temperature fluctuation. For the development of dielectric ceramics with desirable properties, two conventional approaches are usually employed.

One is to search a dielectric material, e.g.  $\text{Ba}(\text{Mg}_{1/3}\text{Ta}_{2/3})\text{O}_3$  [4],  $(\text{Zr}_{0.8}\text{Sn}_{0.2})\text{TiO}_4$  [5] etc., in which the  $\tau_f$  may be tuned by adjusting material's chemistry. The other method is to achieve composite by mixing two or more compounds with negative and positive  $\tau_f$  values in order to compensate the  $\tau_f$  value nearly zero [6,7].

The  $\text{MgTiO}_3$ – $\text{CaTiO}_3$  ceramic composite series is well known as the material for temperature stable dielectric resonators. The ceramic  $0.95\text{MgTiO}_3$ – $0.05\text{CaTiO}_3$  of this series gives  $\epsilon_r \sim 21$ ,  $Q \times f \sim 56,000$  GHz (at 7 GHz) and  $\tau_f \sim 0$  ppm/°C [8,9]. However, the required sintering temperature for this is too high (1450 °C) for practical applications. It is found that the dielectric properties of this composite series can be further improved by replacing Mg and Ca with suitable substitutions [8–12]. For example, the  $0.85\text{Mg}_{0.95}\text{Ni}_{0.05}\text{TiO}_3$ – $0.15\text{Ca}_{0.61}\text{Nd}_{0.26}\text{TiO}_3$  ceramic, sintered at 1350 °C, is found to possess  $\epsilon_r \sim 24.05$ ,  $Q \times f \sim 67,000$  GHz and  $\tau_f \sim -9.3$  ppm/°C [11]. Previously we have also found that the  $0.79\text{Mg}_{0.95}\text{Zn}_{0.05}\text{TiO}_3$ – $0.21\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$  ceramic, sintered at 1275 °C shows good combination of dielectric properties with  $\epsilon_r \sim 26.26$ ,  $Q \times f \sim 60,738$  GHz (at 6.44 GHz) and a nearly zero  $\tau_f \sim -0.8$  ppm/°C [7].

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In this paper we report the structural, morphological and dielectric properties of the composite series  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{TiO}_3$  (MCoT)– $\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$  (CLT). We find that 0.80MCoT–0.20CLT sample, sintered at 1300 °C, shows nearly zero  $\tau_f$  with higher  $Q \times f$  as compared to that of our previous series. The XRD data of all samples have been analyzed using the Rietveld refinement method. The correlation between the microstructures and microwave dielectric properties has been investigated for this series. The experimental data of density,  $\epsilon_r$  and  $\tau_f$  have been compared with theoretical data, obtained using existing models.

## 2. Experimental

The composite samples  $(1-x)\text{MCoT}-(x)\text{CLT}$  with  $x = 0.10, 0.15, 0.20, 0.25$  and  $0.30$  were synthesized by the conventional solid-state reaction method, as discussed in our previous report [7,12]. The corresponding samples will be hence after referred as 90MCoCLT, 85MCoCLT, 80MCoCLT, 75MCoCLT and 70MCoCLT respectively. The pellets were sintered at different temperatures in the range of 1200–1325 °C for 4 h in air. Phase purity and crystal structure of the samples at room temperature were identified using Bruker D8 Advance X-ray diffractometer, for the range  $20^\circ \leq 2\theta \leq 80^\circ$  with a step size of 0.02. The X-rays were produced using a sealed tube and the wavelength of X-ray was 1.5406 Å ( $\text{CuK}_\alpha$ ). The X-rays were detected using a fast counting detector based on silicon strip technology (Bruker LynxEye detector). The structural analysis has been carried out by the well known Rietveld refinement method using FullProf software [13,14]. The Raman spectra were recorded at room temperature in a backscattering geometry, using a RENISHAW inVia Raman microscope attached with four standard Leica microscope objective lenses and an argon ion laser source with the excitation wavelength 514 nm. The spectra for the range of 100–1000  $\text{cm}^{-1}$  were collected using 2400 lines/mm grating, with a 20 s data point acquisition time. The morphological and elemental analyses of the samples were obtained by JEOL scanning electron microscope (SEM); equipped with Oxford INCA Energy dispersive X-ray (EDX) Spectrometer.

The apparent density as well as apparent porosity of the grown samples was obtained using the Archimedes principle. In first step, the dry weight ( $D$ ) of the sintered pellet was measured with a digital electronic balance. A glass beaker with the sample immersed in distilled water was kept in a vacuum chamber for 2 h. After that the beaker was taken out from the vacuum chamber. In this process the pores present in the pellet were completely filled with water. The weight of the pellet was again taken and interpreted as soaked weight ( $W$ ). In second step, the sample was suspended in water with the help of a hanger to hang the pellet in water and the measured weight was interpreted as suspended weight ( $I$ ). The apparent density ( $\rho_{\text{apparent}}$ ) and apparent porosity were measured using the Archimedes principle

$$\rho_{\text{apparent}} = \frac{D}{W-I}, \quad (1)$$

$$\text{Apparent porosity} = \frac{W-D}{W-I} \quad (2)$$

The theoretical density ( $\rho_{\text{theory}}$ ) has been calculated using the following formula [15]:

$$\rho_{\text{theory}} = \frac{ZA}{VN_A}, \quad (3)$$

where  $Z$  is number of atoms in unit cell,  $A$  is atomic weight (g/mol),  $V$  is volume of unit cell ( $\text{cm}^3$ ) and  $N_A$  is Avogadro number ( $\text{mol}^{-1}$ ). Relative density ( $\rho_{\text{relative}}$ ) of sintered specimens has been calculated from the following equation:

$$\rho_{\text{relative}} = \frac{\rho_{\text{apparent}}}{\rho_{\text{theory}}} \quad (4)$$

Microwave dielectric properties of the composites were measured using  $TE_{011}$  resonance mode in a shielding cavity (designed by QWED, Poland) using Agilent PNA N5230A network analyzer with a weak or moderate coupling [16]. This method was first described by Hakki and Coleman [17]; according to them the dielectric constant can be calculated from the following equation:

$$\epsilon_r = 1 + \left( \frac{c}{\pi D f_0} \right) (\alpha_1^2 + \beta_1^2), \quad (5)$$

where  $c$  is the velocity of light,  $\alpha_1$  can be obtained by the mode chart [18] and  $\beta_1$  can be obtained from resonant frequency ( $f_0$ ) and the sample dimension. This method was later analyzed and developed by Courtney [18], which was further improved by Kobayashi et al. [19,20]. In this paper,  $\epsilon_r$  has been calculated using Eq. (5) and the loss tangent has been calculated using the formula of Kobayashi and Katho [20]:

$$\tan \delta = \frac{A}{l-1} \left( \frac{l}{Q_{ul}} - \frac{1}{Q_{u1}} \right), \quad (6)$$

where  $Q_{ul}$  is the unloaded quality factor of  $l$ th order and  $A$  is as described in Reference [20].

The temperature coefficient of resonant frequency ( $\tau_f$ ) of the sample was measured by introducing the cavity in a temperature controlled chamber [7]. The following equation was used for this calculation:

$$\tau_f = \frac{f_2 - f_1}{f_1(T_2 - T_1)}, \quad (7)$$

where  $f_1$  and  $f_2$  represent the resonant frequencies at two different temperatures  $T_1$  ( $\sim 25^\circ\text{C}$ ) and  $T_2$  ( $\sim 85^\circ\text{C}$ ) respectively.

## 3. Results and discussions

### 3.1. XRD patterns

The room temperature XRD patterns of MCoT, CLT and  $(1-x)\text{MCoT}-(x)\text{CLT}$  samples sintered at 1300 °C for 4 h are shown in Fig. 1. The XRD patterns of composite samples illustrate the presence of ilmenite structured MCoT as the main crystalline phase and perovskite structured CLT as a minor phase suggesting the formation of a two-phase system. With the

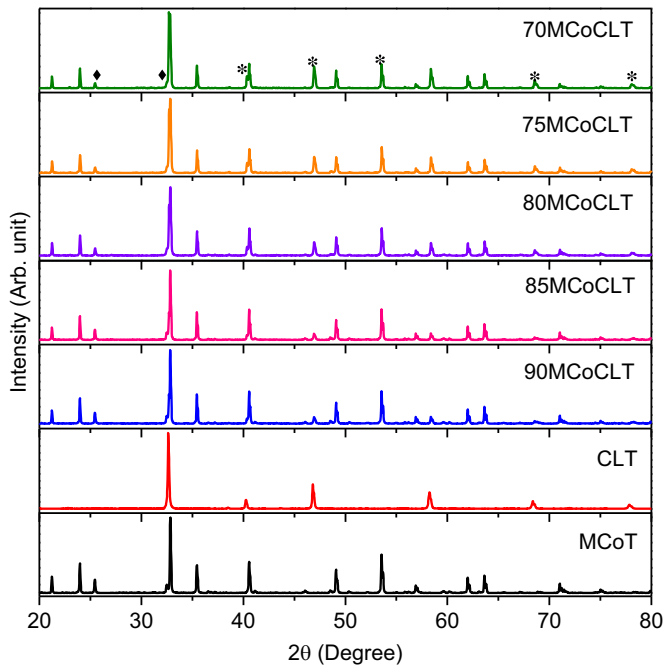


Fig. 1. XRD patterns of MCoT, CLT and  $(1-x)\text{MCoT}-(x)\text{CLT}$  samples, sintered at  $1300^\circ\text{C}$  [◆:  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$ , \*: CLT].

increase of  $x$ , CLT phase is gradually enhanced, the peaks due to CLT are marked with '\*'. The XRD pattern of MCoT phase is in good agreement with hexagonal structure according to the Joint Committee on Powder Diffraction Standards (JCPDS) card no. 06-0494, whereas CLT phase shows good agreement with orthorhombic structure of  $\text{CaTiO}_3$  corresponding to JCPDS card no. 22-0153. In the XRD patterns the peaks indicated by '◆' arise because of the  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  phase. This is usually formed as an intermediate phase and is difficult to completely eliminate from the sample prepared by the mixed oxide route.

The XRD data of all samples have been analyzed using the Rietveld refinement method and refined results are shown in Fig. 2(a)–(c). From the XRD results it is confirmed that the MCoT sample has two phases: main phase MCoT and impurity phase  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  (Fig. 1). Hence XRD data of this sample have been refined using a mixture model of two phases. The refinement has been carried out initially taking the positional parameters of hexagonal structure of MCoT [7] and orthorhombic structure of  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  [21]. The occupancy factors for the mixed Mg and Co sites for both phases have been fixed at the nominal composition. Successful refinement confirms that the main phase of this sample has hexagonal structure with  $R\bar{3}$  space group and the lattice parameters:  $a=b=5.0674\text{ \AA}$  and  $c=13.9291\text{ \AA}$ . Its impurity phase has orthorhombic structure with  $Bbmm$  space group and lattice parameters:  $a=9.7587\text{ \AA}$ ,  $b=10.0081\text{ \AA}$  and  $c=3.7483\text{ \AA}$ . The weight (mass) fractions of hexagonal and orthorhombic phases based on the refined scale factors are found to be 96.91% and 3.09% respectively. The refinement results of CLT ceramic are shown in Fig. 2(b). The refinement is done, initially by taking positional parameters of orthorhombic structure with  $Pbnm$  space group of  $\text{CaTiO}_3$  [22]. The occupancy factors for the mixed Ca and La sites have been

fixed at the nominal composition. Successful refinement confirms that CLT ceramic has orthorhombic structure with  $Pbnm$  space group and the lattice parameters are:  $a=5.4804\text{ \AA}$ ,  $b=5.4929\text{ \AA}$  and  $c=7.7512\text{ \AA}$ . It is noteworthy to point out that the CLT phase generally shows either of pseudo-cubic [23] or orthorhombic [24,25] structures. In our recent article [7] we have reported that XRD data of CLT can be fitted well to cubic structure with  $Pm\bar{3}m$  space group. But more thorough investigation of such fittings has led us understand that the XRD data of CLT can be fitted more precisely with orthorhombic structure as mentioned above.

For the refinement of 80MCoCLT composite sample a mixture model of three phases (MCoT,  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  and CLT) has been used and obtained results are shown in Fig. 2(c). The refinement results reveal that 80MCoCLT ceramic is mixture of hexagonal structured MCoT with  $R\bar{3}$  space group, orthorhombic structured  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  with  $Bbmm$  space group and orthorhombic structured CLT with  $Pbnm$  space group. The weight fraction of MCoT,  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  and CLT phases based on the refined scale factors are found to be 79.34%, 2.55% and 18.11% respectively. On the basis of refined crystallographic data, it can be concluded that a good agreement is achieved between the calculated and observed XRD patterns. The Wyckoff positions and crystallographic data of 80MCoCLT composite, sintered at  $1300^\circ\text{C}$ , after refinement using the Fullprof program are demonstrated in Table 1. The obtained lattice parameters and goodness of fit indicator ( $\chi^2$ ) for all composite samples, sintered at  $1300^\circ\text{C}$ , are listed in Table 2. This study clearly indicates the coexistence of both the phases in composite samples without any detectable amount of interdiffusion between them. The Rietveld method has also been successfully applied for determination of the quantitative phase analysis (QPA) of the composite materials [26]. There is a simple relationship between the individual scale factor determined, considering all refined structural parameters of individual phases of a multiphase sample and the phase concentration (volume/weight fraction) in the mixture. The QPA resulted from the refinement procedure is summarized in Table 3. One can observe that the QPA is in good agreement with the composition of each composite phase in the samples investigated.

The XRD patterns of 80MCoCLT sample, sintered at various temperatures in the range  $1200$ – $1325^\circ\text{C}$ , are shown in Fig. 2(d). It is evident from the figure that the patterns remain almost unaltered with sintering temperature. However, the peak corresponding to the  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  phase has become more prominent for the samples sintered at higher temperatures.

### 3.2. Raman spectra

The Raman spectra of MCoT, CLT and 80MCoCLT samples are shown in Fig. 3(a)–(c). According to the description in the Bilbao crystallographic center website [27], the ilmenite structure  $\text{MgTiO}_3$  has ten Raman-active vibrational modes ( $\Gamma_{\text{Raman}} = 5A_g + 5E_g$ ), which supports our findings. The  $A_g$  ( $225.7$  and  $306.1\text{ cm}^{-1}$ ) modes occur because of the vibrations of Mg and Ti atoms along the  $z$ -axis. The others  $A_g$  modes observed at  $397.7$ ,  $498.8$  and  $714.7\text{ cm}^{-1}$  are attributed to the vibrations of O atoms.

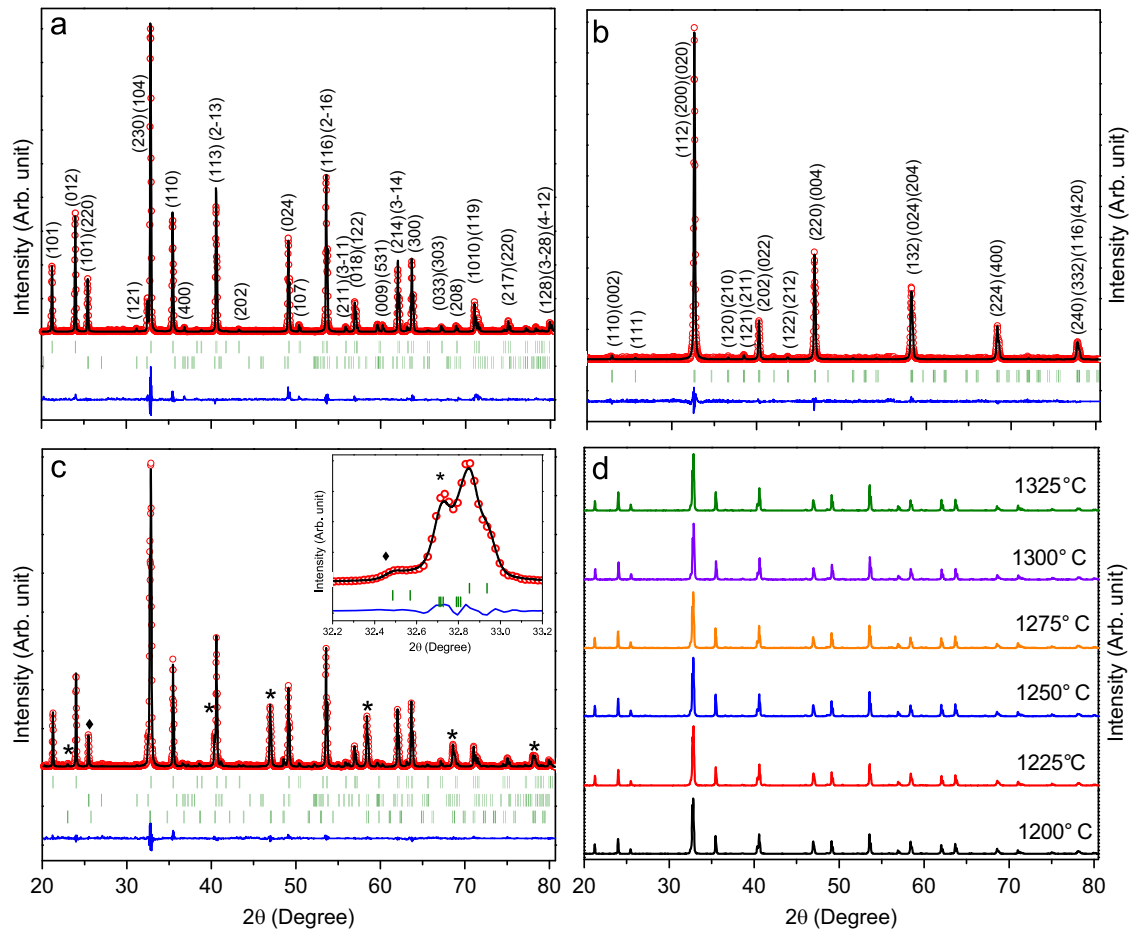


Fig. 2. Observed (open symbols) and calculated (solid lines) XRD patterns for (a) MCoT, (b) CLT and (c) 80MCoCLT. Differences between the observed and the calculated intensities are shown at the bottom of the figure. The calculated Bragg-reflected positions are marked by the vertical bars. The Miller indices of the major Bragg reflections are also indicated. (d) XRD patterns of 80MCoCLT ceramic, sintered at different sintering temperatures.

Table 1  
Rietveld refinement results and atomic coordinates employed in order to model the MCoT and CLT unit cells.

Sample	Symmetry and space group	Atoms	Site	Atomic coordinate		
				x	y	z
MCoT	Hexagonal S.G. – $R\bar{3}$	Mg/Co	6c	0.0	0.0	0.3584
		Ti	6c	0.0	0.0	0.1453
		O1	18f	0.3171	0.0159	0.2360
CLT	Orthorhombic S.G. – $Pbnm$	Ca/La	4c	0.0121	0.0146	0.25
		Ti	4b	0.0	0.5	0.0
		O1	4c	–0.0101	0.5132	0.25
		O2	8d	0.7506	0.2872	0.0198

$R_p = 10.7$ ,  $R_{wp} = 16.3$ ,  $R_{exp} = 13.0$ ,  $R_{Bragg} = 4.16$  (MCoT) and  $R_{Bragg} = 6.56$  (CLT)

For  $A_g$  modes ( $498.8$  and  $714.7\text{ cm}^{-1}$ ), the six O atoms of octahedral configuration present breathing-like vibrations, but each with different vibration directions. The intense  $E_g$  mode appeared at  $281.8\text{ cm}^{-1}$  is related to the anti-symmetric breathing vibration of the O octahedron. The  $E_g$  modes ( $327.9$  and  $352\text{ cm}^{-1}$ ) can be described as the twisting of the O octahedron with the vibrations of Mg and Ti atoms parallel to the  $xy$ -plane. The  $E_g$  ( $484.7\text{ cm}^{-1}$ )

mode arises due to the anti-symmetric breathing vibration of the O octahedra with the cationic vibrations of both Mg and Ti atoms parallel to the  $xy$ -plane, while the  $E_g$  ( $640.7\text{ cm}^{-1}$ ) mode is related to the anti-symmetric twisting vibration of the O octahedra associated with the Ti–O stretching [28,29]. The perovskite structured CLT shows 8 Raman modes as shown in Fig. 3(b). According to the literature [30,31], orthorhombic



structure with space group  $Pbnm$ , has 24 Raman-active modes, which can be described by the representation  $\Gamma_{\text{Raman}, Pbnm} = 7A_g + 7B_{1g} + 5B_{2g} + 5B_{3g}$ . The Raman band  $B_{2g}$  ( $116.1 \text{ cm}^{-1}$ ) is related to the  $\text{Ca-TiO}_3$  lattice mode. The bands  $A_g$  ( $163.4$  and  $285.3 \text{ cm}^{-1}$ ),  $B_{1g}$  ( $219.5 \text{ cm}^{-1}$ ) and  $B_{3g}$  ( $330.8 \text{ cm}^{-1}$ ) are assigned to  $\text{O-Ti-O}$  bending modes. The band  $A_g$  ( $461.2 \text{ cm}^{-1}$ ) is related to  $\text{Ti-O}_6$  torsional modes. The other bands at  $399.6$  and  $513.8 \text{ cm}^{-1}$  might be related to Raman bands of  $\text{LaTiO}_3$ . The peak at  $796.5 \text{ cm}^{-1}$  is related to  $B_{2g}$  mode. In Raman spectrum of CLT, fewer bands are observed possibly due to very low polarizability, so as to prevent such bands from being seen in the spectrum. Fig. 3(c) shows the Raman spectra of  $(1-x)\text{MCoT}-(x)\text{CLT}$  composite samples. Most of the active Raman modes of these spectra correspond to MCoT phase, but with a small shift at lower wave number as illustrated in the inset. Only some of the peaks of CLT phase remain clear (marked with “#”); this may be because of the fact that most of the peak positions of this phase are closer to those of MCoT phase. It is observed that the peak intensity of composite samples decreases with CLT addition.

### 3.3. Microstructural and elemental analysis

Fig. 4 shows the surface microstructural images of the  $80\text{MCoCLT}$  composite sintered at different temperatures in the range  $1200$ – $1325^\circ\text{C}$ . The image of Fig. 4(a) indicates that the specimen does not appear dense and the grains of small size are grown at  $1200^\circ\text{C}$ . The grain size increases as the sintering temperature increases. The pores are almost eliminated for the sample sintered at  $1300^\circ\text{C}$  and a noticeable grain growth and a relatively uniform surface morphology are observed at this

temperature. However, inhomogeneous grain growth is monitored at temperature  $1325^\circ\text{C}$  with melted and porous microstructures, which might degrade the microwave dielectric properties of the ceramics. In order to analyze the composition, the EDX results of  $80\text{MCoCLT}$  composite sample are demonstrated in Fig. 4(g) and (h) for two different positions of Fig. 4 (e). Spots ‘A’ and ‘B’ show mostly the expected peaks of MCoT and CLT phases respectively; the Pt peaks in the EDX spectra come from the coating of platinum over the surface of sample required to avoid charging.

### 3.4. Densification studies

The apparent density of the  $(1-x)\text{MCoT}-(x)\text{CLT}$  composite samples with different  $x$  values is shown in Fig. 5(a) as a function of sintering temperature. Initially there is a significant increase in density with increasing sintering temperature, it becomes maximum at  $1300^\circ\text{C}$  and thereafter trend of variation is reversed. The degradation of density at temperature above  $1300^\circ\text{C}$  occurs due to the inhomogeneous grain growth and partial melting of grain boundaries, as understood from SEM studies [See Fig. 4(f)]. It can also be observed that density of the sample enhances with increasing CLT content, since the density of CLT is relatively higher ( $\sim 4.73 \text{ g/cm}^3$ ) than that of MCoT ( $\sim 3.59 \text{ g/cm}^3$ ). At  $1300^\circ\text{C}$ , the apparent density of the composite samples lies in the range  $3.78$ – $4.05 \text{ g/cm}^3$  respectively. For a two-phase composite sample, the theoretical density of the composite can be calculated using mixing model [26] as given below

$$\frac{1}{\rho_{\text{composite}}} = \frac{(1-x)}{\rho_1} + \frac{x}{\rho_2}, \quad (8)$$

where  $x$  is weight% (wt%) of second phase,  $\rho_1$  and  $\rho_2$  are the theoretical density of first and second phases respectively; these values have been obtained from the Rietveld refinement. The values of apparent density, theoretical density, relative density and apparent porosity of all composite samples, sintered at  $1300^\circ\text{C}$  are listed in Table 3. It is evident from this table that the apparent density determined experimentally is slightly less than theoretical density, because the macroscopic specimen usually contains minute cracks and pores.

Table 2

The goodness of fit indicator ( $\chi^2$ ) and lattice parameter of  $(1-x)\text{MCoT}-(x)\text{CLT}$  composite samples, sintered at  $1300^\circ\text{C}$ .

Samples	MCoT		CLT			$\chi^2$
	$a$ (Å)	$c$ (Å)	$a$ (Å)	$b$ (Å)	$c$ (Å)	
90MCoCLT	5.0619	13.9217	5.4716	5.4721	7.7272	1.92
85MCoCLT	5.0665	13.9223	5.4691	5.4743	7.2775	2.61
80MCoCLT	5.0654	13.9214	5.4713	5.4692	7.7269	1.96
75MCoCLT	5.0683	13.9232	5.4734	5.4698	7.7267	2.25
70MCoCLT	5.0642	13.9191	5.4695	5.4734	7.7283	2.18

Table 3

The values of apparent density, apparent porosity, theoretical density and relative density of composite samples, sintered at  $1300^\circ\text{C}$ .

Sample	Weight fraction (%)		Density			Apparent porosity
	MCoT*	CLT	Theoretical $\rho$ ( $\text{g/cm}^3$ )	Experimental $\rho$ ( $\text{g/cm}^3$ )	Relative $\rho$ (%)	
90MCoCLT	90.07	9.93	4.038	3.776	93.503	1.403E-5
85MCoCLT	84.69	15.31	4.101	3.895	94.989	1.089E-5
80MCoCLT	81.89	18.11	4.129	3.959	95.880	3.693E-6
75MCoCLT	74.68	25.32	4.210	3.986	94.680	4.062E-5
70MCoCLT	70.86	29.14	4.252	4.046	95.152	3.737E-6

\*Weight fraction of  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  is included.

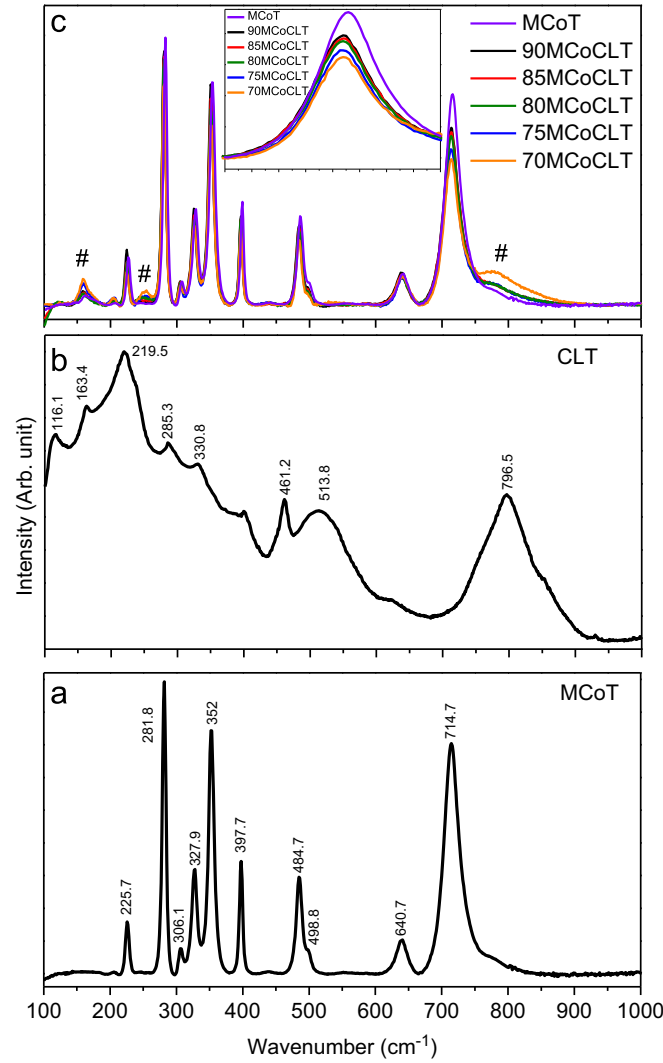


Fig. 3. Raman spectra of (a) MCoT, (b) CLT and (c)  $(1-x)\text{MCoT}-(x)\text{CLT}$  samples. The mode appeared at  $715\text{ cm}^{-1}$  has been enlarged in the inset.

### 3.5. Microwave dielectric properties

The dielectric constant ( $\epsilon_r$ ) of the composites as a function of sintering temperature, is depicted in Fig. 5(b). The dependence of  $\epsilon_r$  as a function of sintering temperature shows the same trend as obtained between density and sintering temperature. The value of  $\epsilon_r$  increases with increasing sintering temperature. After reaching its maximum at  $1300\text{ }^\circ\text{C}$ , it decreases. It is also observed that the value of  $\epsilon_r$  for composite samples increases as the  $x$  value increases, because of the fact that CLT has a much higher  $\epsilon_r$  ( $\sim 113.35$ ) compared to that ( $\sim 16.54$ ) of MCoT. For MCoCLT series, sintered at  $1300\text{ }^\circ\text{C}$ , the  $\epsilon_r$  values have been found to lie in the range 21.67–31.52.

The theoretical  $\epsilon_r$  of two-phase MCoT–CLT composites, sintered at  $1300\text{ }^\circ\text{C}$ , has been calculated using different mixing formulae based on the effective medium models [32–36]. The mathematical equations of each model are described as follows:

Series mixing model [32]

$$\frac{1}{\epsilon_r} = \frac{(1-x)}{\epsilon_{r_1}} + \frac{x}{\epsilon_{r_2}}, \quad (9)$$

Parallel mixing model [33]

$$\epsilon_r = (1-x) \epsilon_{r_1} + x \epsilon_{r_2}, \quad (10)$$

Brick-wall model [34]

$$\epsilon_r = \epsilon_{r_2} \left( 1 - \frac{1-x}{1-n} \right) + \left( \frac{1-x}{1-n} \right) \frac{\epsilon_{r_1} \epsilon_{r_2}}{(1-n) \epsilon_{r_2} + n \epsilon_{r_1}}, n = 1/3x; \quad (11)$$

Lichtenecker empirical logarithmic model [35]

$$\ln \epsilon_r = (1-x) \ln \epsilon_{r_1} + x \ln \epsilon_{r_2}; \quad (12)$$

Calusius–Mossotti equation [36]

$$\frac{\epsilon_r - 1}{\epsilon_r + 2} = (1-x) \frac{\epsilon_{r_1} - 1}{\epsilon_{r_1} + 2} + x \frac{\epsilon_{r_2} - 1}{\epsilon_{r_2} + 2}, \quad (13)$$

where  $x$  is the wt% of CLT phase,  $\epsilon_{r_1}$  and  $\epsilon_{r_2}$  are the relative permittivities of MCoT and CLT phases respectively. The experimental values of  $\epsilon_r$  and its theoretical values, calculated using different models are plotted in Fig. 6 with the variation of the CLT content. From the figures it is observed that in the considered range, the data calculated using series mixing model

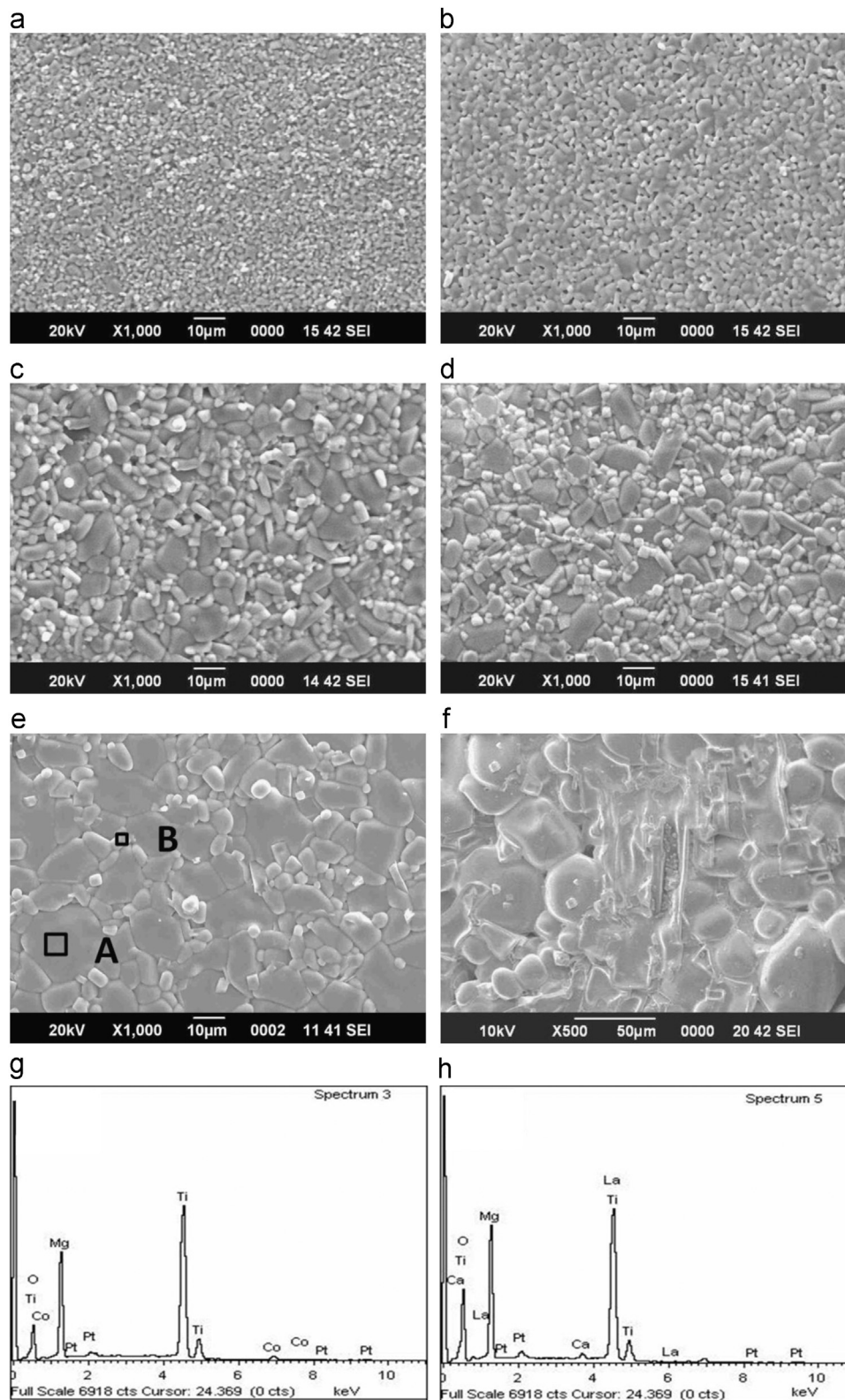


Fig. 4. SEM micrographs of 80MCoCLT sample, sintered at (a) 1200 °C, (b) 1225 °C, (c) 1250 °C, (d) 1275 °C, (e) 1300 °C and (f) 1325 °C; (g) and (h) EDX results for positions 'A' and 'B' respectively.

as well as Calusius–Mossotti equation are quite small as compared to the experimental data. On the other hand, the parallel mixing model gives overestimated values of  $\epsilon_r$ . We have observed that there are two appropriate models in this case. The

first is the Lichtenecker empirical logarithmic rule, which is often used for the mixtures of powders or porous systems. The second appropriate formula is the Brick–Wall model, which explains the exact solution for the dielectric constant of a mixture of coated

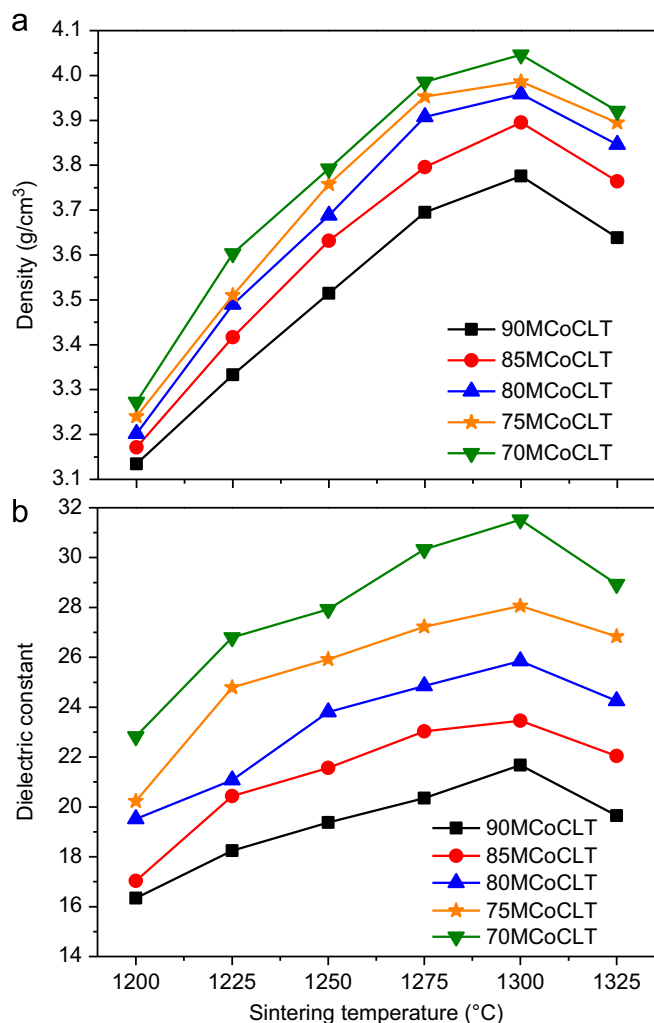


Fig. 5. Apparent density and dielectric constant of composite samples as a function of sintering temperature.

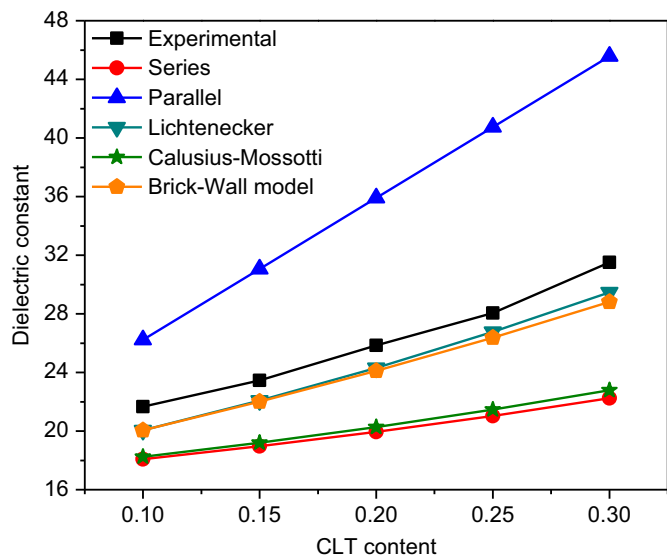


Fig. 6. The experimental and theoretical dielectric constant of (1-x)MCoT-(x)CLT composites, sintered at 1300 °C, as a function of CLT content.

spheres. However, the small deviation in  $\epsilon_r$  corresponding to these two models may be because of the dissimilar microstructural shapes of both the phases [37]. This might have occurred also because of the presence of porosity and the impurity phase  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$  having a relative permittivity  $\sim 17.56$  [38].

Fig. 7(a) presents the  $Q \times f$  values of different samples of this series as a function of sintering temperature. From this figure it is observed that the  $Q \times f$  of composites decreases with increasing CLT content because the  $Q \times f$  of CLT is ( $\sim 16,730$  GHz at 2.93 GHz) lower than that of MCoT ( $\sim 198,370$  GHz at 8.03 GHz). It is also examined that with increasing sintering temperature, the  $Q \times f$  value increases to a maximum and thereafter it decreases. The maximum  $Q \times f$  value of each composition of this series arises corresponding to the sintering temperature 1300 °C. With sintering temperature the enhancement in  $Q \times f$  of a composition can be attributed to the increase in density and grain size, decrease in pores and the grain boundary area as well as the uniformity of grain growth. A degradation of  $Q \times f$  value for the sample, sintered at 1325 °C, has been noticed because of its lesser density resulted from the inhomogeneous grain growth and melted microstructures [Fig. 4(f)]. The formation of impurity

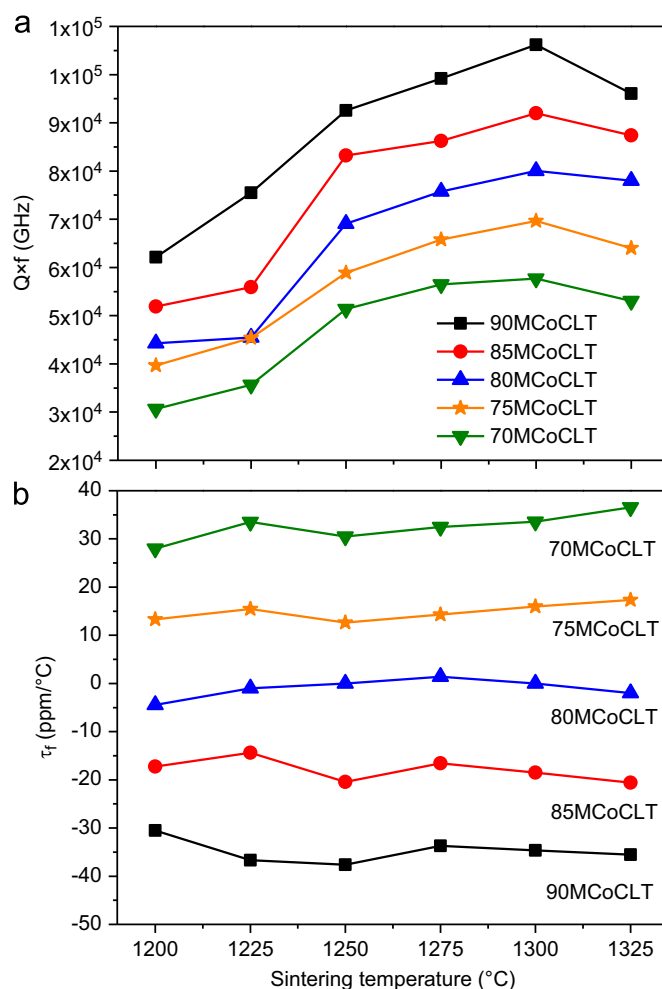


Fig. 7. (a)  $Q \times f$  and (b)  $\tau_r$  values of composite samples with the variation of sintering temperature.



Table 4

The microwave dielectric properties of  $(1-x)\text{MCoT}-(x)\text{CLT}$  composite samples, sintered at 1300 °C.

Sample	$\epsilon_r$	$Q \times f$ (GHz)	$\tau_f$ (ppm/°C)	
			Measured	Calculated
90MCoCLT	21.67	106,180	−34.6	−26.6
85MCoCLT	23.46	91,980	−18.5	−12.4
80MCoCLT	25.85	80,040	0.002	1.8
75MCoCLT	28.06	69,660	16.0	16.0
70MCoCLT	31.52	57,680	33.6	30.2

phase  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$ , as confirmed by XRD studies (Fig. 1) may also cause a decrease in the  $Q \times f$  value because it has lower quality factor ( $\sim 58,000$  GHz) [38].

The  $\tau_f$  values of  $(1-x)\text{MCoT}-(x)\text{CLT}$  composites, sintered at different temperatures are demonstrated in Fig. 7(b). From this figure it is evident that  $\tau_f$  is insensitive to the sintering temperature for the entire temperature range under consideration. However, the  $\tau_f$  value has been found to be related to the weight percentage of the second phase. Since the  $\tau_f$  values of MCoT and CLT are  $-55$  and  $229$  ppm/°C respectively, the  $\tau_f$  values of these composites rapidly become more positive with increasing CLT content. Its value becomes  $\sim 0$  for 80MCo CLT sample. The  $\tau_f$  of the mixture phases has been computed using a general mixture rule [37] as given below

$$\tau_f = (1-x)\tau_{f1} + (x)\tau_{f2}, \quad (14)$$

where  $x$  is wt% of the CLT phase,  $\tau_{f1}$  and  $\tau_{f2}$  are temperature coefficients of MCoT and CLT phases respectively. The obtained data have been compared with experimental results as illustrated in Table 4. It is evident that the experimental results of  $\tau_f$  slightly deviate from the corresponding calculated results obtained using mixture rule.

From Figs. 5(b), 7(a) and (b), we can notice that out of all composite samples the  $0.80\text{Mg}_{0.95}\text{Co}_{0.05}\text{TiO}_3-0.20\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$  ceramic sintered at 1300 °C shows best combination of microwave dielectric properties ( $\epsilon_r \sim 25.85$ ,  $Q \times f \sim 80,040$  GHz at 8.05 GHz and  $\tau_f \sim 0$  ppm/°C). Its quality factor is higher compared to the similar sample (sintered at 1275 °C) with nearly zero  $\tau_f$  of our previous series  $\text{Mg}_{0.95}\text{Zn}_{0.05}\text{TiO}_3-\text{Ca}_{0.6}\text{La}_{0.8/3}\text{TiO}_3$ , whereas  $\epsilon_r$  is almost same for both samples.

#### 4. Conclusions

Characteristic properties of  $(1-x)\text{MCoT}-(x)\text{CLT}$  composite ceramics have been studied in order to achieve a thermal stable material with good combination of dielectric properties. All composite samples exhibit mixed phases of MCoT (ilmenite-structured) as the main phase in association with second phase CLT (perovskite-structured) and an impurity phase  $\text{Mg}_{0.95}\text{Co}_{0.05}\text{Ti}_2\text{O}_5$ . The detailed structural study has been done by employing the Rietveld refinement technique with the help of the FullProf suite program. The microwave dielectric properties are strongly related to the density, percentage of second phase, sintering temperature and microstructure of the sample. It is found that with

the increase in CLT content, the  $\epsilon_r$  of the composite samples increases whereas its quality factor decreases. The values of density,  $\epsilon_r$  and  $\tau_f$  have been theoretically obtained using existing models. Deviation between theoretical and experimental results might have occurred due to the dissimilar microstructural shapes of both the phases. It is concluded that the values of  $\epsilon_r$  of these samples can be explained well using the Lichtenecker empirical logarithmic rule as well as the Brick-wall model. The composite with  $x = 0.20$  can be considered as a suitable material for DRs.

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