

Influence of Oxygen Partial Pressure on the Metastability of Undoped Zirconia Dispersed in Alumina Matrix

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(Received 25 February 1994; revised version received 1 June 1994; accepted 14 June 1994)

Abstract

The influence of oxygen content in the sintering atmosphere on zirconia phases in alumina–zirconia ceramics was studied. As was demonstrated, in the case of samples sintered in an atmosphere with oxygen partial pressure between 2.80 ± 10^{-5} Pa and 2.80×10^{-2} Pa, 100% of zirconia was found to be in the cubic form. The appearance of transformable cubic zirconia is a result of oxygen vacancy concentration in zirconia. The increase of oxygen partial pressure and decrease of oxygen vacancy concentration leads to a breakdown of the cubic phase which transforms to the t- and/or m-phases. Critical values of oxygen vacancy concentration responsible for the metastability of cubic and tetragonal zirconia were estimated.

1 Introduction

Transformation toughening in ZrO_2 -containing ceramics requires the presence of metastable tetragonal (t) zirconia, so that the toughening obtainable from the stress-induced martensitic transformation to monoclinic (m) symmetry can be realized. As has been shown recently,^{1–3} when this type of ceramic is sintered in oxygen-deficient conditions, transformable cubic (c) phase appears, as a result of nonstoichiometry of ZrO_2 . The metastability of t- and c- ZrO_2 at low temperatures either in powder state or in compact form was proposed by different theories and hypotheses.^{4–1} Unfortunately, the controlling mechanisms responsible for metastability of high-temperature phases of zirconia are still unknown.

The present work is aimed to explain the effect of oxygen content in sintering atmosphere and related oxygen vacancy concentration on c–t

inversion in undoped zirconia grains dispersed in alumina matrix.

2 Experimental Methods

The starting material was a powder composition containing: 99.55 wt% Al_2O_3 , 0.20 wt% MgO and 0.25 wt% Y_2O_3 . Alumina powder (made by CEMAT-Skawina, Poland) was 99.99 wt% pure and the average grain size below $0.5 \mu\text{m}$. The remaining two components were of the same purity.

The components of the composition were homogenized for 48 h in a ball mill in distilled water. Then 10 wt% zirconia—obtained from zirconyl chloride by chemical methods described earlier¹²—was added and homogenized for further 48 h. The powders were cold isostatically pressed at 140 MPa into rectangular die (41×65 mm). The samples were sintered at 1973 K of 90 min either in a gas furnace (air atmosphere) or in an electric furnace under eleven levels of oxygen partial pressure (p_{O_2}) in sintering atmosphere between 2.8×10^{-5} Pa and 1.07×10^{-4} Pa. The values of p_{O_2} were realized by controlled introduction (by using electronic valves) of air into the high-vacuum chamber of the furnace or earlier prepared oxygen–argon gas mixtures.

The critical stress-intensity factor, K_{IC} , was determined after Evans¹³ on notch-beam specimens of configuration described earlier¹² and an Instron TIM type testing machine. The bearing spacing was 36 mm and the rate of loading 0.1 mm min^{-1} .

The bending strength was determined by three-point bending on bars $5 \times 5 \times 50$ mm using the same testing machine, the same rate of loading and bearing spacing. These tests were performed on 15 samples for each composition.

Table 1. Mechanical properties of alumina ceramics containing 10 wt% zirconia

Properties	Sintering atmosphere	
	Air	0.133 mPa vacuum
	Oxygen partial pressure (Pa)	
	2.1×10^{-4}	2.8×10^{-5}
Critical stress-intensity factor, K_{Ic} , MPa m ^{1/2}	6.60 ± 0.57	8.00 ± 0.67
Bending strength, MPa	324.40 ± 58.7	397.80 ± 28.5
Grindability, mm	0.1	0.01

The measurement of grindability was carried out with a Mackensen blower using 500–630 μ m SiC powder, 0.15 MPa pressure and a cell of 28 cm³ volume. To intensify the abrasion by the grinding powder, the test was repeated three times at the same place on the samples. As a measure of grindability, the depth of the hole blown by the grinding powder in 15 samples for each composition was recorded.

The phase composition of zirconia in each of the free and fractured surfaces ceramics was determined by X-ray diffraction (Siemens diffractometer Kristalloflex 4). The measurements were carried out in the 2θ -angle 20–160° at 293 K using monochromatized $\text{CuK}\alpha_1$ radiation (quartz, (10 $\bar{1}$ 1) reflection Johanson type) in steps of 1/16 deg min⁻¹. The precision of goniometer was tested using an ultrapure silicon powder standard.

The phase content was estimated using integral intensities of the strongest lines taking into account the polarization, Lorentz, structure and multiplicity factors.¹⁴ The lattice parameters were calculated using the least-squares Cohen method.¹⁴

The loss of oxygen in ZrO_2 of samples sintered in atmospheres with increasing p_{O_2} was estimated by measuring the weight increasing during its reoxidation in air at 1273 K (1000 h). This allows the level of the oxygen vacancy concentration to be determined.

3 Results and Discussion

As can be seen from the data shown in Table 1, the critical stress-intensity factor, K_{Ic} , of ceramics sintered in high vacuum (0.133 mPa) is really

Table 2. Zirconia phases in Al_2O_3 -10 wt% ZrO_2 measured from free surface as a function of sintering atmosphere

Sintering atmosphere	Phases of zirconia (%)		
	Monoclinic	Tetragonal	Cubic
Air	16.5	83.5	—
0.133 mPa vacuum	—	—	100

Table 3. X-ray data of c- ZrO_2 in Al_2O_3 -10 wt% ZrO_2 sintered in vacuum (free surface)

	2θ , degrees	I/I_0	h	k	l
1	30.12	100	1	1	1
2	34.96	17	2	0	0
3	50.22	32	2	2	0
4	59.74	16	3	1	1
5	62.68	2	2	2	2
6	73.94	1	4	0	0
7	81.76	2	3	3	1
8	84.40	3	4	2	0
9	94.74	1	4	2	2
10	102.68	1	3	3	3
11	125.40	1	5	3	1
12	128.64	<1	6	0	0

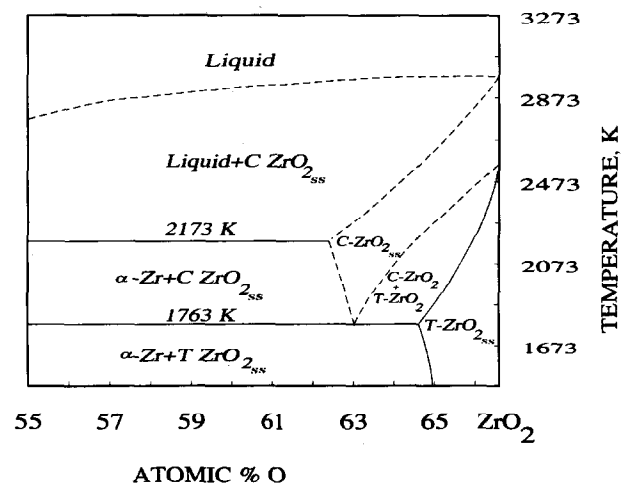
higher than that for the air-sintered ceramics. The bending strength and Mackensen's grindability of these ceramics also differ in the same way.

The observed differences can be correlated with the presence of zirconia phases in the matrix. In the case of air-sintered samples, 83.5% of zirconia is in the tetragonal form (Table 2).

X-ray analysis of samples sintered in high vacuum indicates 100% presence of the cubic form. The X-ray data of c- ZrO_2 obtained from free surface are listed in Table 3.

As can be seen from the phase diagram of the system Zr–O (Fig. 1) determined by Ruh & Garrett,¹⁵ the presence of c- ZrO_2 at 1973 K (the tetragonal–cubic phase transformation temperature is at 2558 ± 15 K) is possible under the conditions of high anion deficiency equal to $2 - x = 1.688 - 1.740$.

It seems that the appearance of metastable c- ZrO_2 in alumina ceramics is a result of sintering in high vacuum (under very low oxygen partial pressure) accompanied by oxygen nonstoichiometry. Furthermore, the constraint of the alumina matrix prevents the c-phase transforming during cooling from the sintering temperature to room temperature.

**Fig. 1.** Phase diagram of the Zr–O system.¹⁵

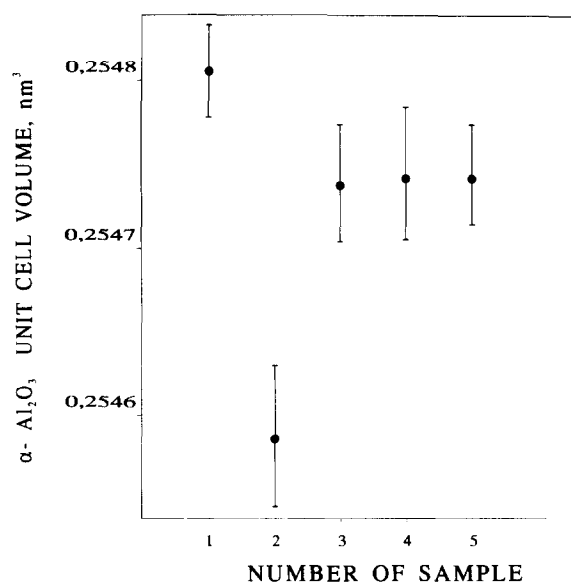


Fig. 2. Volume of α - Al_2O_3 unit cell in Al_2O_3 -10 wt% ZrO_2 versus sintering and measuring conditions. The measured samples are: (1) α - Al_2O_3 matrix; (2) free surface of high vacuum-sintered alumina-zirconia ceramics; (3) free surface of air-sintered alumina-zirconia ceramics; (4) fractured surface of high vacuum-sintered alumina-zirconia ceramics; (5) fractured surface of air-sintered alumina-zirconia ceramics.

The presence of the stress field in the ceramics confirms the X-ray results for the α - Al_2O_3 unit cell volume for the alumina matrix with and without zirconia particles sintered in air and in vacuum (Fig. 2). As shown, the largest deformation of the α - Al_2O_3 unit cell is in samples where only the c-phase of ZrO_2 exists. In other samples deformations are relaxed. It should be expected that the particles of c- ZrO_2 , when placed in the locally enhanced tensile stress field at the tip of an advancing crack, are freed from the constraint of the matrix and transform to the forms stable at the lower temperature range.

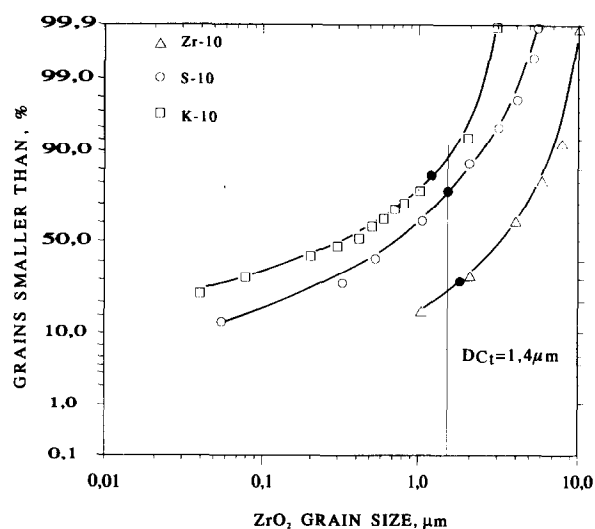


Fig. 3. Zirconia grain-size distribution of air-sintered alumina ceramics containing 10 wt% Zr-type ZrO_2 , 10 wt% S-type ZrO_2 and 10 wt% K-type ZrO_2 . ●, Content of the finest ZrO_2 grains corresponding to the content of tetragonal form.

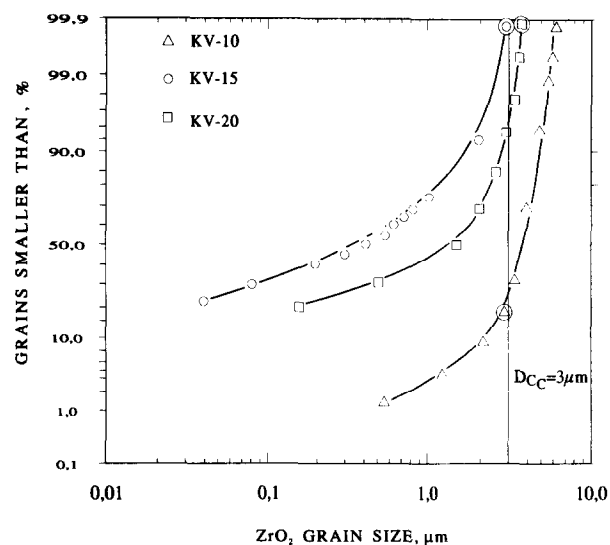


Fig. 4. Zirconia grain-size distribution of high vacuum-sintered alumina ceramics containing 10 wt%, 15 wt% and 20 wt% ZrO_2 of K-type (obtained by chemical method).² ○, Content of the finest ZrO_2 grains corresponding to the content of cubic form.

Tetragonal and monoclinic zirconia on fractured surfaces of vacuum-sintered ceramics show that the cubic form is the transformable phase and is responsible for enhancing the toughness of the ceramics.³ This phase then appears to play the same role as the tetragonal form in the case of ceramics sintered in an oxidizing atmosphere.

The critical grain size of t- ZrO_2 inclusions in the case of air-sintered ceramics is $d_{ct} = 1.4 \mu\text{m}$ (Fig. 3).¹² This value was estimated by comparison of ZrO_2 grain size distribution with the content of retained t- ZrO_2 . A similar estimation made for samples sintered in high vacuum (Fig. 4) indicates an increase of the critical grain-size inclusion for c- ZrO_2 up to a value of $d_{cc} = 3.0 \mu\text{m}$.² Obviously, the reason for the enhancement of the critical grain-size inclusion could be found in the non-stoichiometry of ZrO_2 .

According to the present results, if the oxygen vacancy concentration plays a decisive role in the metastability of c-phase, it would then be possible to transform it to t- or m-phase, due to the reduction of the vacancy concentration in the ZrO_2 lattice as a result of sintering alumina-zirconia ceramics in atmospheres richer in oxygen. After Kountouros *et al.*,¹¹ a critical minimum and a critical maximum vacancy concentration for each ZrO_2 phase should also exist.

As can be seen from Table 4, in the p_{O_2} range between 2.80×10^{-5} and 2.80×10^{-2} Pa, the cubic form is the only phase of zirconia. However, an increase of oxygen content in the sintering atmosphere causes changes in the lattice parameters of the c-phase (see Table 5 and Fig. 5). An increase of the constant a values and the unit cell volume is observed. These results seem to be an effect of oxygen loss decrease from the zirconia structure

Table 4. Zirconia phases in Al_2O_3 -10 wt% ZrO_2 measured from free surface as a function of oxygen content in sintering atmosphere

Oxygen partial pressure (Pa)	Oxygen vacancy concentration (%)	Phases of ZrO_2 (%)		
		<i>m</i>	<i>t</i>	<i>c</i>
2.80×10^{-5}	14.85	—	—	100
2.80×10^{-4}	13.65	—	—	100
2.80×10^{-3}	12.90	—	—	100
2.80×10^{-2}	9.13	—	—	100
1.40×10^{-1}	5.25	—	20.6	79.4
1.80×10^{-1}	3.12	Traces	100	—
1.07×10^0	0.45	5.6	94.4	—
1.00×10^1	0.145	7.0	93.0	—
0.85×10^2	0.05	8.0	92.0	—
1.39×10^3	0	8.4	91.6	—
1.07×10^4	0	10.6	89.4	—
2.10×10^4	0	16.5	83.5	—

during sintering in less oxygen-deficient atmospheres. The decrease of the X-ray mean half breadth (Fig. 6) and lattice parameter scattering from a value of 0.000 16 to 0.000 02 (see Table 5) also indicates an improvement in the c-phase structure.

When the oxygen content in the sintering atmosphere decreases below the critical p_{O_2} value for the c-phase, t- ZrO_2 appears and coexists with c- ZrO_2 (see Table 4— $p_{\text{O}_2} = 1.40 \times 10^{-1}$ Pa).

In the case of 1.80×10^{-1} Pa oxygen pressure t- ZrO_2 is the only form of zirconia present, but from 1.07×10^0 Pa oxygen pressure is accompanied by m- ZrO_2 . It indicates that the critical minimum vacancy concentration for t-phase has been exceeded. A further increase of the oxygen

Table 5. Lattice parameters of c- ZrO_2 as a function of oxygen content in sintering atmosphere

Oxygen partial pressure (Pa)	Lattice constants <i>a</i> (nm)	Volume of unit cell (nm^3)
2.80×10^{-5}	$0.512\,49 \pm 0.000\,16$	$0.134\,604 \pm 0.000\,129$
2.80×10^{-4}	$0.512\,98 \pm 0.000\,11$	$0.134\,989 \pm 0.000\,089$
2.80×10^{-3}	$0.513\,19 \pm 0.000\,08$	$0.135\,155 \pm 0.000\,063$
2.80×10^{-2}	$0.514\,63 \pm 0.000\,02$	$0.136\,302 \pm 0.000\,017$
1.40×10^{-1}	$0.514\,14 \pm 0.000\,32$	$0.135\,908 \pm 0.000\,253$

content (air atmosphere) leads to an increase of m- ZrO_2 up to 16.5%.

In a similar way to the cubic form, an increase of the oxygen content in the sintering atmosphere influences the lattice parameters of the t- and m-phases (Tables 6 and 7). As can be seen from Fig. 7 the tetragonality (c/a axial ratio) of t- ZrO_2 considerably improves. An increase of the m-phase unit volume is also observed (Table 7). Figures 8 and 9 illustrate the changes of zirconia phase composition with oxygen content in a sintering atmosphere.

The presence of the stress field in samples with c- ZrO_2 is also confirmed by XRD results of the α - Al_2O_3 unit cell volume of samples sintered in p_{O_2} atmospheres between 2.80×10^{-4} and 2.80×10^{-2} Pa (see Fig. 10). Calculated deformation of α - Al_2O_3 unit cell is equal to 0.2% (see Table 8). In other samples with t- ZrO_2 the unit cell volume becomes similar to values typical for alumina ceramics without zirconia. In this way, t- ZrO_2 seems to be a factor responsible for the relaxation of stresses caused by c- ZrO_2 in the matrix.

Table 6. Lattice parameters of t- ZrO_2 as a function of oxygen content in sintering atmosphere

Oxygen partial pressure (Pa)	Lattice constants (nm)		<i>c/a</i>	Volume of unit cell (nm^3)
	<i>a</i>	<i>c</i>		
1.40×10^{-1}	$0.360\,661 \pm 0.000\,059$	$0.518\,793 \pm 0.000\,087$	$1.438\,45 \pm 0.000\,48$	$0.067\,482\,72 \pm 0.000\,033\,63$
1.80×10^{-1}	$0.360\,265 \pm 0.000\,021$	$0.519\,391 \pm 0.000\,039$	$1.441\,69 \pm 0.000\,19$	$0.067\,412\,20 \pm 0.000\,012\,89$
1.07×10^0	$0.360\,275 \pm 0.000\,017$	$0.519\,365 \pm 0.000\,039$	$1.441\,58 \pm 0.000\,18$	$0.067\,412\,52 \pm 0.000\,011\,28$
1.00×10^1	$0.360\,271 \pm 0.000\,016$	$0.519\,382 \pm 0.000\,041$	$1.441\,64 \pm 0.000\,18$	$0.067\,410\,31 \pm 0.000\,011\,09$
0.85×10^2	$0.359\,981 \pm 0.000\,156$	$0.519\,848 \pm 0.000\,038$	$1.444\,10 \pm 0.000\,17$	$0.067\,365\,3 \pm 0.000\,010\,7$
1.39×10^3	$0.360\,409 \pm 0.000\,188$	$0.519\,299 \pm 0.000\,049$	$1.440\,86 \pm 0.000\,21$	$0.067\,454\,3 \pm 0.000\,013\,4$
1.07×10^4	$0.360\,409 \pm 0.000\,042$	$0.519\,006 \pm 0.000\,070$	$1.440\,05 \pm 0.000\,36$	$0.067\,416\,2 \pm 0.000\,024\,9$
2.10×10^4	$0.360\,159 \pm 0.000\,092$	$0.519\,340 \pm 0.000\,016$	$1.441\,97 \pm 0.001\,73$	$0.067\,366\,5 \pm 0.000\,055\,2$

Table 7. Lattice parameters of m- ZrO_2 as a function of oxygen content in sintering atmosphere

Oxygen partial pressure (Pa)	Lattice constants (nm)			Volume of unit cell (nm^3)
	<i>a</i>	<i>b</i>	<i>c</i>	
1.07×10^0	$0.513\,253 \pm 0.000\,408$	$0.517\,343 \pm 0.000\,339$	$0.530\,255 \pm 0.000\,425$	$0.138\,998\,21 \pm 0.000\,328\,81$
1.00×10^1	$0.513\,438 \pm 0.000\,795$	$0.516\,957 \pm 0.001\,005$	$0.530\,112 \pm 0.000\,498$	$0.139\,011\,33 \pm 0.000\,637\,25$
0.85×10^2	$0.513\,476 \pm 0.000\,277$	$0.518\,789 \pm 0.000\,433$	$0.529\,819 \pm 0.000\,303$	$0.139\,437\,45 \pm 0.000\,286\,96$
1.39×10^3	$0.513\,435 \pm 0.000\,565$	$0.517\,513 \pm 0.000\,893$	$0.530\,798 \pm 0.000\,443\,8$	$0.139\,267\,98 \pm 0.000\,529\,16$
2.10×10^4	$0.515\,450 \pm 0.000\,110$	$0.530\,900 \pm 0.000\,110$	$0.518\,390 \pm 0.000\,110$	$0.140\,006\,12 \pm 0.000\,148\,50$

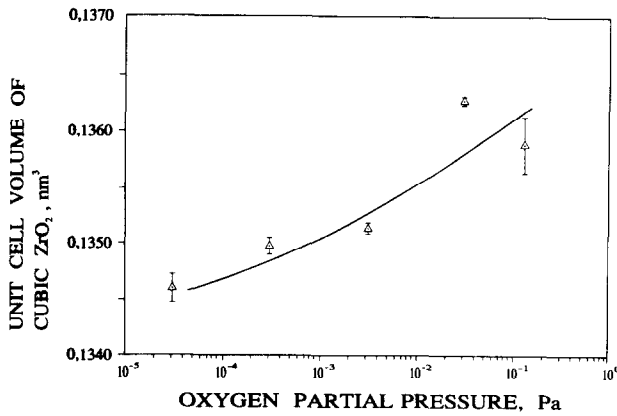


Fig. 5. Cubic zirconia unit cell volume as a function of oxygen content in sintering atmosphere.

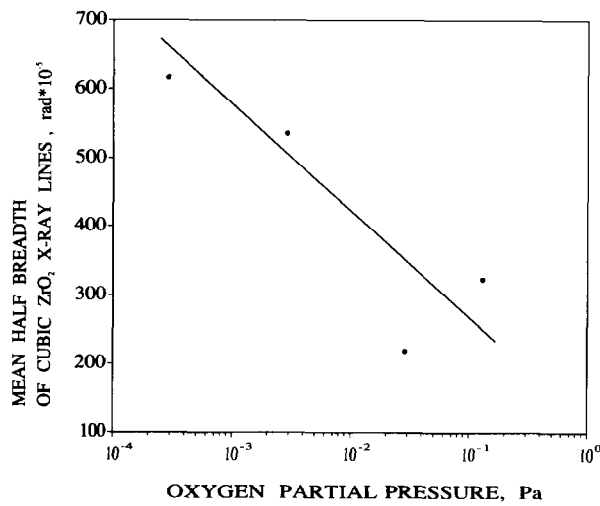


Fig. 6. Mean half breadth of X-ray lines of c-ZrO₂ as a function of oxygen content in sintering atmosphere.

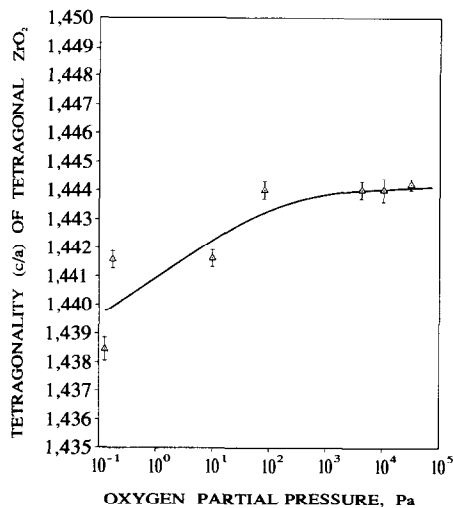


Fig. 7. Tetragonality (c/a) of t-ZrO₂ as a function of oxygen content in sintering atmosphere.

Samples sintered in p_{O_2} atmosphere equal to 1.40×10^{-1} Pa, where 20.6% of the tetragonal form coexists with 79.4% of the c-phase, are a good confirmation of the previously mentioned thesis.

The main conclusion concerning the influence of oxygen vacancy concentration on the meta-

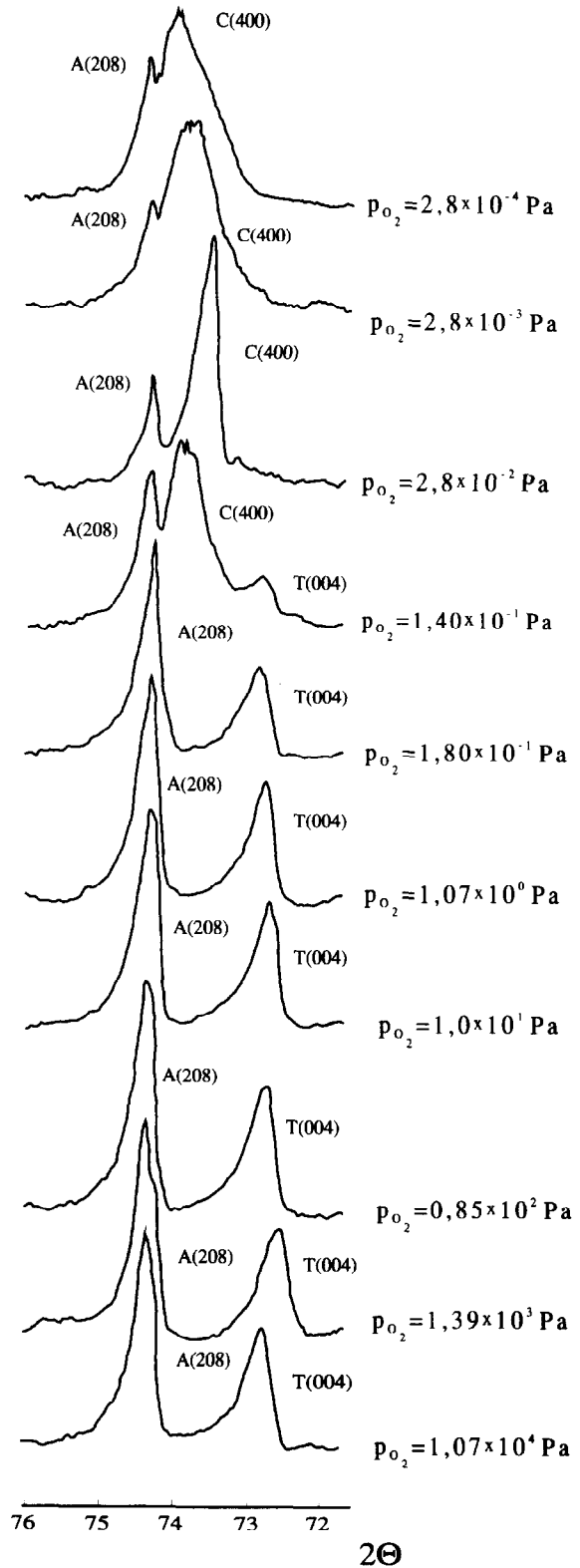


Fig. 8. Changes of XRD profiles of Al₂O₃-10 wt% ZrO₂ ceramics ($2\theta = 72-76^\circ$) as a function of oxygen content in sintering atmosphere. A = α -Al₂O₃, C = cubic, T = tetragonal zirconia respectively.

stability of zirconia phases comes from thermogravimetric determinations. In this case, samples sintered in oxygen-deficient conditions were reoxidized by reheating in air at 1273 K for 1000 h and an increase of their weight was recorded. Results of oxygen vacancy concentration in zirconia are listed in Table 4.

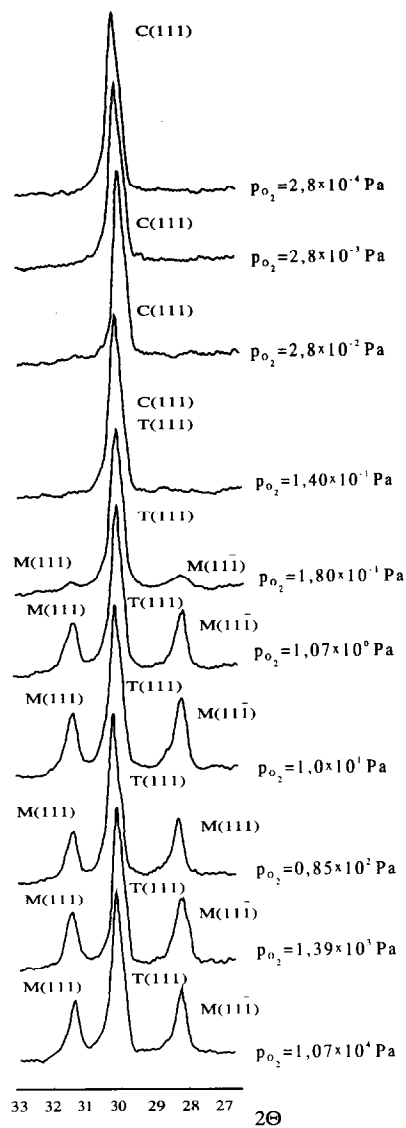


Fig. 9. Changes of XRD profiles of Al_2O_3 -10 wt% ZrO_2 ceramics ($2\theta = 27$ - 33°) as a function of oxygen content in sintering atmosphere. C = Cubic, T = tetragonal and M = monoclinic zirconia respectively.

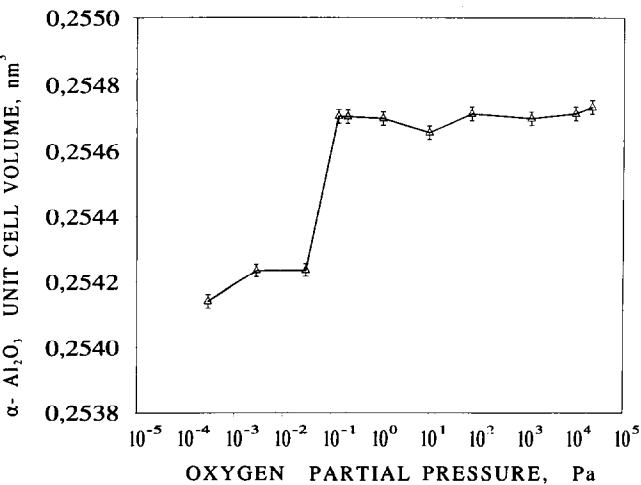


Fig. 10. Changes of α - Al_2O_3 unit cell volume in Al_2O_3 -10 wt% ZrO_2 ceramics as a function of oxygen content in sintering atmosphere.

Table 8. Changes of unit cell volume and mean half breadth X-ray lines of $\alpha\text{Al}_2\text{O}_3$ in Al_2O_3 -10 wt% ZrO_2 as a function of oxygen content in sintering atmosphere

Oxygen partial pressure (Pa)	Change of unit cell volume $\Delta V/V$ (%)	Mean half breadth (rad)
2.80×10^{-4}	0.225	0.002 69
2.80×10^{-3}	0.182	0.002 75
2.80×10^{-2}	0.183	0.002 19
1.40×10^{-1}	0.002	0.001 35
1.80×10^{-1}	0.000	0.001 47
1.07×10^0	0.005	0.001 62
1.00×10^1	0.022	0.001 53
0.85×10^2	0.001	0.001 77
1.39×10^3	0.003	0.001 64

As was shown, the cubic form is the only phase of zirconia which exists in the oxygen vacancy concentration between 14.85 and 9.13%, that corresponds to a oxygen partial pressure in the sintering atmosphere in the range 2.80×10^{-5} Pa to 2.80×10^{-2} Pa. When the oxygen content increases to 1.40×10^{-1} Pa and the oxygen vacancy concentration decreases to a value of 5.25%, c- ZrO_2 coexists with the tetragonal form. Complete inversion to t- ZrO_2 is observed for 3.12% of oxygen vacancy content and this value seems to be a critical minimum value of oxygen vacancy concentration for this phase. Increasing the oxygen content in the sintering atmosphere the volume

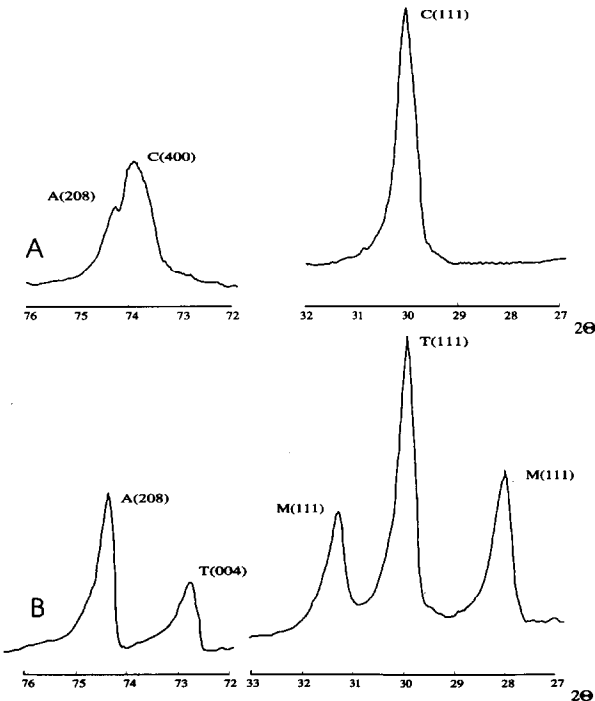


Fig. 11. Changes of zirconia phase composition as result of reoxidation heating of alumina-zirconia ceramics. A, Sample of ceramics sintered in atmosphere with oxygen partial pressure equalled 2.80×10^{-3} Pa; B, the same sample after reoxidation heating at 1273K for 1000 h in air. Explanation: A = α - Al_2O_3 , C = cubic, T = tetragonal and M = monoclinic zirconia respectively.

of m-ZrO₂ increases also up to value of 16.5%, typical for samples sintered in oxidizing (air) atmosphere.

These results confirm the earlier thesis¹¹ that the oxygen vacancies in zirconia are mainly responsible for the metastability of c- and t-phases. Decreasing the oxygen vacancy concentration with an increase of the oxygen partial pressure in the sintering atmosphere below the critical minimum value leads to a breakdown of the c-phase which transforms to the t- and/or m-phase (see Fig. 11).

4 Conclusions

This study demonstrated that the oxygen content in a sintering atmosphere clearly influences the phase composition of undoped zirconia grains dispersed in alumina matrix.

In the case of ceramics sintered in atmospheres with oxygen partial pressure between 2.80×10^{-5} Pa and 2.80×10^{-2} Pa, 100% of zirconia is in the cubic form. The appearance of transformable c-ZrO₂ is a result of oxygen vacancy concentration in zirconia. The concentration of oxygen vacancy equal to 9% seems to be the critical minimum value for this phase. Decreasing the oxygen vacancy concentration, as a result of increasing the oxygen content in the sintering atmosphere, below 9%, causes an increase of the t-ZrO₂ content. The critical value of the oxygen vacancy concentration for the tetragonal form is 3%. A further increase of the oxygen content to 1.07×10^0 Pa and a decrease of oxygen vacancy concentration to 0.5% lead to the appearance of m-ZrO₂.

Acknowledgement

This work was supported by the State Committee for Scientific Research under Grant No. 7.1013 91 01.

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