

# Frequency dependence of dielectric nonlinearity in PMN relaxor system

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## Abstract

The linear  $\varepsilon_1^*$  and the third harmonic complex dielectric constant  $\varepsilon_3^*$  in  $\text{PbMg}_{1/3}\text{Nb}_{2/3}\text{O}_3$  (PMN) single crystal were measured as a function of frequency and temperature in a small electric field. The dielectric dispersion of  $\varepsilon_3^*$  was studied and the characteristic relaxation time together with the static dielectric nonlinearity were determined as a function of the temperature. The static dielectric nonlinearity  $\beta_s$  is increasing with decreasing temperature in the temperature range 266–242 K, while the relaxation time follows the Vogel–Fulcher law. © 2001 Elsevier Science Ltd. All rights reserved.

**Keywords:** Dielectric properties; Ferroelectric properties; PMN

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## 1. Introduction

Recently the investigation of relaxors is getting on intensity. Some aspects of the nature of the freezing transition are revealed. In zero bias electric field relaxors show the transition into the nonergodic phases,<sup>1–4</sup> but if relaxors are cooled in the electric field higher than critical, a long range ferroelectric phase is formed.<sup>5,6</sup>

With recently introduced spherical random-bond random-field (SRBRF) model<sup>7,8</sup> it is possible to describe temperature dependencies of the Edwards-Anderson order parameter  $q_{\text{EA}}$  and the quasistatic nonlinear dielectric ratio  $a_3 = \varepsilon_3/\varepsilon_1^4$  in PMN relaxor. The SRBRF model explains also the crossover in the temperature dependence of  $a_3$  from decreasing into the increasing behavior when approaching the freezing transition  $T_f$  from above<sup>9</sup> in zero bias electric field and the crossover from the glass-like behavior of  $a_3$  into the ferroelectric-like monotonous decreasing behavior under the bias electric field higher than critical  $E > E_C$ .<sup>10</sup> SRBRF model predicts also the peak of the temperature

dependence in the static dielectric nonlinearity  $a_3$  at the freezing transition. Because of dispersions in  $\varepsilon_1$  and  $\varepsilon_3$ , which characteristic relaxation times rapidly increases with decreasing temperature at temperatures much above  $T_f$ , it is experimentally not feasible to determine the static nonlinear susceptibility in the vicinity of the freezing temperature.

In the present work we will present the measurements of  $\varepsilon_1^*(\omega, T)$  and  $\varepsilon_3^*(\omega, T)$  in PMN single crystal and show that the dielectric nonlinearity  $\beta$  is the function of the frequency and temperature in the temperature interval between 266 and 242 K. The temperature dependence of the static dielectric nonlinearity  $\beta_s$  and the characteristic relaxation time will also be determined.

## 2. Experimental procedure

Measurements were done on (111) plate of PMN monocrystal with sputtered Ag electrodes. The method of measurements of  $\varepsilon_1$  and  $\varepsilon_3$  was described before.<sup>11</sup> The dielectric response was measured in the frequency interval of  $10^{-2}$ – $3 \cdot 10^2$  Hz. The amplitude of measuring ac electric field applied on the sample was 170 V/cm. The measurements were done in cooling run with the cooling rate of 0.5 K/min.

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### 3. Results and discussion

Fig. 1 shows  $|\beta| = |\varepsilon_3(\omega)|/|\varepsilon_1(\omega)|^3|\varepsilon_1(3\omega)|\varepsilon_0^3$  as a function of the temperature at five frequencies. The dielectric nonlinearity  $|\beta|$  shows the dispersion below  $\approx 260$  K.

Fig. 2 shows  $\varepsilon'_3$  and  $\varepsilon''_3$  as a function of the frequency at 252.5 K. The curve in Fig. 2 represents the fit to the expression.<sup>12–14</sup>

$$\varepsilon_3^*(\omega) = \varepsilon_{3\infty} + \frac{\Delta\varepsilon_3}{(1 + (i\omega\tau)^\alpha)^3}. \quad (1)$$

The parameters of the characteristic relaxation time  $\tau$ , the distribution parameter  $\alpha$ , and the dielectric strength  $\Delta\varepsilon_3$  of the imaginary part of the nonlinear dielectric constant were determined from the fits of  $\varepsilon''_3$  to Eq. (1). From the experimental values of the  $\varepsilon'_3$  the high frequency dielectric constant  $\varepsilon_{3\infty}$  was determined. Fig. 3 shows several Cole–Cole plots in PMN at different

temperatures. It should be mentioned that the Eq. (1) does not describe the experimental data of  $\varepsilon_3^*(\omega)$  in PMN at very high frequencies ( $\omega\tau \gg 1$ ). The extrapolation to  $\omega \rightarrow 0$  was also made with a linear plot through the measured points at low frequencies (Fig. 3), thus giving the static nonlinear dielectric constant  $\varepsilon_{3s}$ .

The temperature dependence of the static dielectric nonlinearity  $\beta_s = \varepsilon_{3s}/\varepsilon_{1s}^4\varepsilon_0^3$  is shown in Fig. 4. The values of  $\varepsilon_{1s}$  were taken from the measurements of the field-cooled dielectric constant.<sup>3</sup>  $\beta_s$  is increasing with the decreasing temperature in the temperature interval between 266 and 242 K. This is in accordance with the prediction of the SRBRF model above  $T_f$ . To determine  $\beta_s$  at temperatures lower than 240 K the measurements of  $\varepsilon_3^*(\omega)$  at frequencies much lower than 0.01 Hz would be necessary. The logarithm of the reciprocal characteristic relaxation time  $1/2\pi\tau$  determined from the  $\varepsilon''_3$  vs frequency (Fig. 2) by the fits to the Eq. (1) is presented as a function of the temperature in Fig. 5. The solid curve in Fig. 5 is a fit to the Vögel–Fulcher

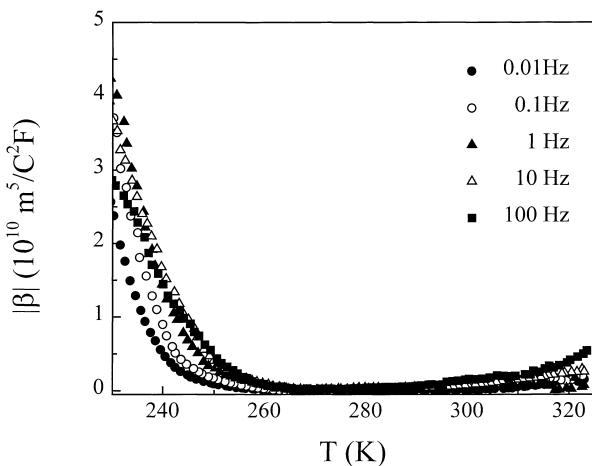


Fig. 1. The temperature dependence of  $|\beta|$  at five frequencies.

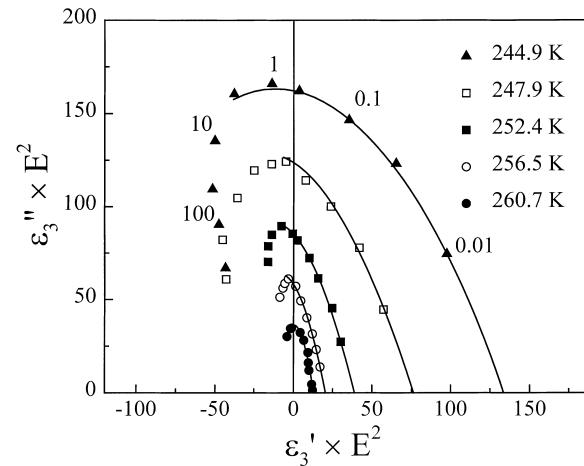


Fig. 3. Measured values of  $\varepsilon''_3$  plotted vs  $\varepsilon'_3$  at five temperatures.

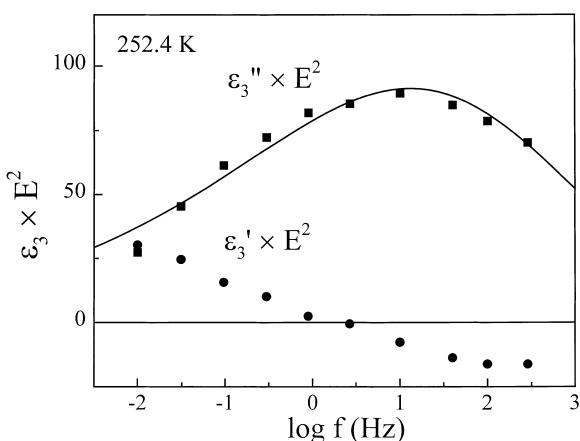


Fig. 2.  $\varepsilon'_3$  and  $\varepsilon''_3$  vs frequency at 252.4 K.

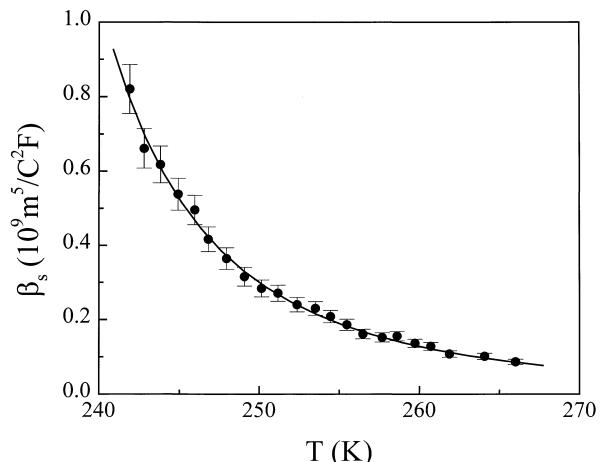


Fig. 4. The temperature dependence of  $\beta_s$ .

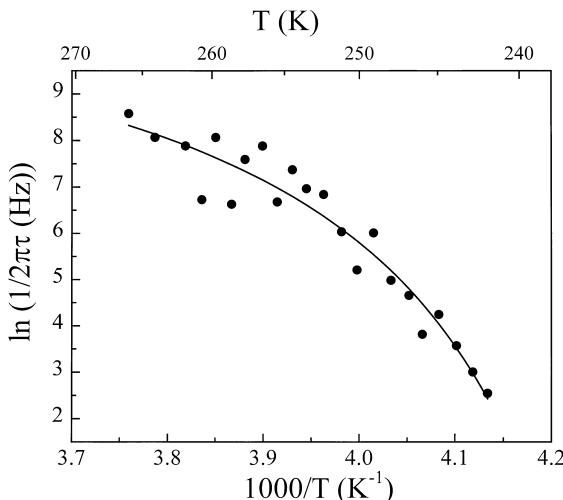


Fig. 5. Temperature dependence of the logarithm of the reciprocal characteristic relaxation time  $1/2\pi\tau$  in PMN.

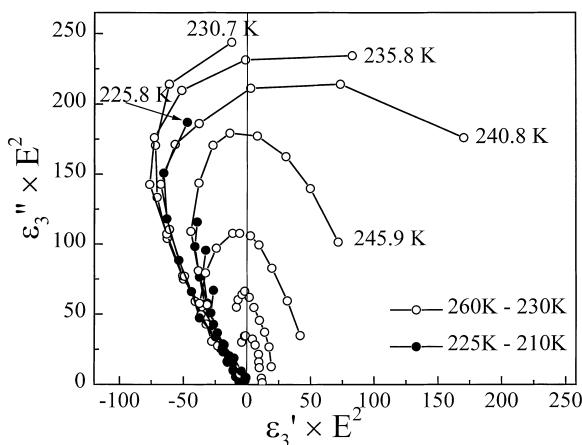


Fig. 6. Measured values of  $\epsilon''_3$  plotted vs  $\epsilon'_3$  in the temperature range of 260–210 K.

expression with  $T_0 = 227 \pm 5$  K,  $U = 139 \pm 64$  kK, and  $\tau_0 = 1.1 \times 10^{-6}$  s. The value of  $T_0$  is close to the value determined previously.<sup>3</sup>

Fig. 6 shows measured values of  $\epsilon''_3$  plotted vs  $\epsilon'_3$  in PMN at eleven temperatures in the temperature interval 260–210 K with the temperature step of 5 K. The Cole-Cole plots below  $T_0$  are indicated by (●) and the plots above  $T_0$  by (○). The solid lines connect the data measured at the same temperature. Fig. 6 demonstrates a rapid increase of the characteristic relaxation time with decreasing temperature, which effectively preclude the observation of  $\epsilon_{3s}$  in PMN through the freezing temperature. These makes confirmation of the existence of the peak in  $\beta$  predicted by the SRBRF model impossible by the present experimental technique. However, it should be noted that the observed temperature dependence of the  $\beta_s$  is qualitatively in agreement with the results of the SRBRF model in the measured temperature range.

#### 4. Conclusions

The linear and nonlinear dielectric constant of the PMN single crystal were studied as a function of the frequency and temperature. The static nonlinear dielectric constant  $\epsilon_{3s}$  and the characteristic relaxation time  $\tau$  were determined as a function of the temperature.  $\epsilon_{3s}$  and thus  $\beta_s$  are increasing with decreasing temperature in the temperature range of 266–242 K according to the SRBRF model, while  $\tau$  shows Vögel–Fulcher type behavior.

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