

Formation mechanism and sintering behavior of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$

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Abstract

The reaction mechanism of a mixture of BaTi_4O_9 and TiO_2 was investigated. It was found that the development of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ was not via the direct reaction of BaTi_4O_9 and TiO_2 at the interface, but by nucleation from the matrix of BaTi_4O_9 inserted by the Ti species in the limited temperature range of 1200–1300°C. It is suggested that the formation of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ is via nucleation and growth. Moreover, it was observed that twinning existed in the remaining BaTi_4O_9 grains during the formation processes, which is due to the fact that the retained BaTi_4O_9 grains were stressed by the surrounding $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ grains. Possible explanations for the difficulty in preparing $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ are proposed. A sample with a high-density (about 99% theoretical density) and fine-grained uniform microstructure could be achieved and the dielectric properties are dielectric constant 39, Q 5863 at 7.3 GHz, and the temperature coefficient of resonance frequency 5 ppm/°C. © 2001 Elsevier Science Ltd. All rights reserved.

Keywords: $\text{Ba}_2\text{Ti}_9\text{O}_{20}$; Dielectric properties; Microstructure-final; Reaction sequence

1. Introduction

The recent advancement of the microwave wireless communication could be attributed to technologic improvement of the dielectric resonator. Efforts have been put on the miniaturization of the microwave circuitry. Dielectric resonators with large values of permittivity meet this function. A combination of high dielectric constant, high Q factor, and low temperature coefficient of resonant frequency^{1–3} is required for a high-quality dielectric resonator. Jonker and Kwestroo⁴ reported that single-phase $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ could only be obtained by doping small amounts of SnO_2 or ZrO_2 . However, it has been shown⁵ that single-phase $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ could be synthesized without doping near 1300°C but decomposed at temperatures above 1300°C. While a few reports^{6,7} using wet chemical methods could synthesize $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ at low temperatures (<1000°C), most papers^{8–10} showed that it could only be obtained by calcining at high temperatures $\geq 1200^\circ\text{C}$ for a long time. The sluggish formation of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ has been attributed to the increase of distance between intermediate phases,^{10–12} high surface and interface energies,⁸ or the

high potential energy barrier arising from the crystal structure.¹³ Therefore, it is apparent that the formation mechanism and low formation rate of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ still needed to be clarified. Moreover, owing to the difficulty in synthesizing the high-quality single-phase $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, its sintering behavior so far has been rarely studied.

In this investigation, the formation mechanism and sintering behavior of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ were intensively studied.

2. Experimental procedure

The starting materials used in this investigation were reagent-grade BaCO_3 (99.9%, 325 mesh, CERAC Inc., Milwaukee, USA) and TiO_2 (99.9%, 325 mesh, CERAC Inc., Milwaukee, USA). BaTi_4O_9 was prepared directly from BaCO_3 and TiO_2 in an appropriate ratio. $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ was synthesized via two ways: BaCO_3 with TiO_2 and BaTi_4O_9 with TiO_2 in appropriate ratios. These powders were mixed for 24 h in a Nylon jar containing ZrO_2 balls and ethyl alcohol. The mixed powders were rapidly dried by microwave to reduce the segregation. Subsequently, the powders were ground lightly with a mortar and pestle and then pressed as a pellet. These pellets were calcined in air at different temperatures without holding but at 1200°C, different times were also performed. The formed single-phase $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ powder

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was used for sintering study. The sintering behavior was carried out in a dilatometer at different temperatures.

An X-ray diffractometer (Model D/MAX III.V XRD, Rigaku, Tokyo, Japan) was used for determining the phases and the reaction amount. The procedure for determining the reaction amount is described as follows. The powder compacts was sintered at 1200°C for different times and then quenched in air for evaluating the reaction amount. The internal standard method¹⁴ was employed to determine the developing amount of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, in which the quenched samples were ground and SiO_2 (quartz) was used as an internal standard. The scanning rate was set to 1° per min over a range of 22–31°. These peaks, with the strongest intensity of diffraction were selected to measure the extent of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ and the collected counts of the peaks were fitted and integrated to extract the peak area. Transmission electron microscopy (TEM) (JEM-2010 (for Figs. 5 and 6) and JEM-3010 (for Fig. 8), Jeol, Japan) and high resolution transmission electron microscopy (HF-2000, Hitachi, Japan) were employed to identify the phases using selected area diffraction pattern (SADP) and examine the microstructures.

For dielectric measurement, the sintered pellets were cut perpendicular to the cylindrical axis to form parallel faces and their side walls were ground. The relative dielectric constant, Q value, and temperature coefficient of resonant frequency at microwave frequencies were investigated using the method proposed by Hakki and Coleman¹⁵ and developed by Kobayashi and Tanaka.¹⁶ A microwave network analyzer (Model 8510C, pulsed-RF network analyzer, Hewlett-Packard Co., Santa Clara, CA) was used to measure the microwave properties.

3. Results

Fig. 1 shows X-ray diffraction (XRD) patterns of the formation processes of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ by calcining the mixture of $\text{BaCO}_3\text{:TiO}_2 = 1\text{:}4.5$ at different temperatures without holding. It was observed that minute BaTiO_3 occurred first at 800°C and disappeared above 1000°C. BaTi_4O_9 appeared at 900°C and almost dominated at 1200°C. It should be noted that TiO_2 has completely disappeared at 1200°C but $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ still was not observed. Fig. 2 shows XRD patterns of the mixture of $\text{BaCO}_3\text{:TiO}_2 = 1\text{:}4.5$ isothermally heated at 1200°C for different times. It was observed that $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ appeared in 3 h but could not be completely formed with longer time. Fig. 3 shows the XRD patterns of the formation processes of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ by calcining the mixture of $\text{BaTi}_4\text{O}_9\text{:TiO}_2 = 2\text{:}1$ at different temperatures without holding. As observed, BaTi_4O_9 remained almost unchanged but TiO_2 disappeared at temperatures > 1000°C. Fig. 4 shows the isothermal calcination of the mixture of $\text{BaTi}_4\text{O}_9\text{:TiO}_2 = 2\text{:}1$ at 1200°C for different times. It is

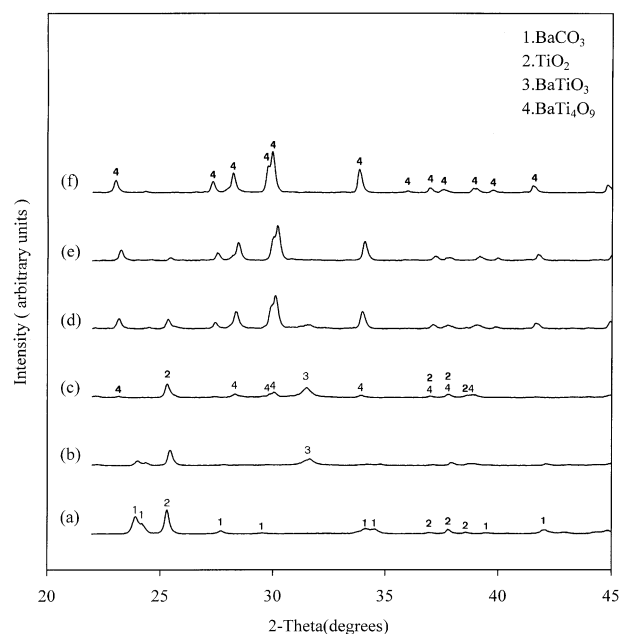


Fig. 1. X-ray diffraction patterns of the mixture of BaCO_3 and TiO_2 calcined at different temperatures without holding : (a) mixture, (b) 800°C, (c) 900°C, (d) 1000°C, (e) 1100°C and (f) 1200°C.

apparent that $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ could more easily develop by calcining the mixture of BaTi_4O_9 and TiO_2 comparing with Fig. 2. Moreover, though BaTi_4O_9 has reduced to a minute amount in 3 h, it took more than 20 h to completely eliminate this retained BaTi_4O_9 .

Fig. 5 shows the bright-field image (BFI) and selected area diffraction pattern (SADP) of TEM for the mixture of $\text{BaTi}_4\text{O}_9\text{:TiO}_2 = 2\text{:}1$ calcined at 1150°C without hold-

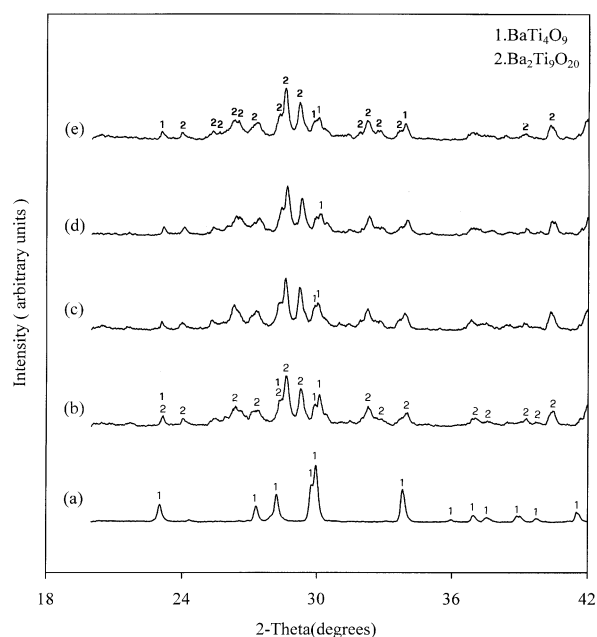


Fig. 2. X-ray diffraction patterns of the mixture of BaCO_3 and TiO_2 isothermally heated at 1200°C for different times : (a) 0 h, (b) 3 h, (c) 6 h, (d) 9 h and (e) 12 h.

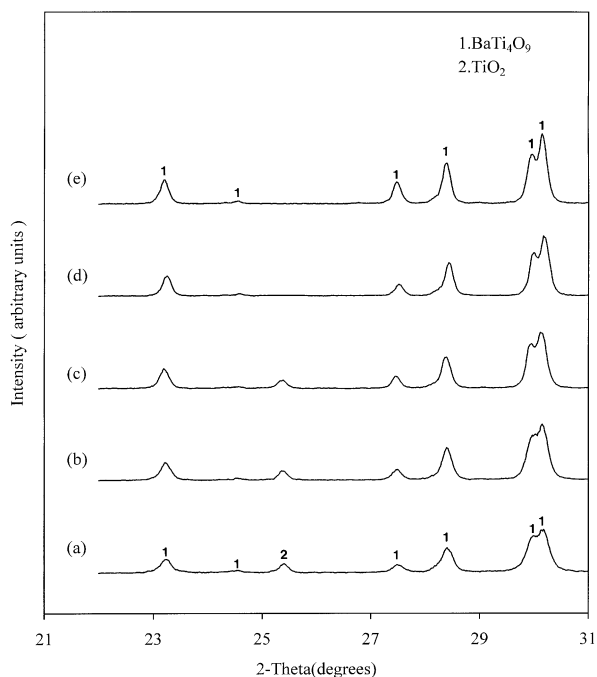


Fig. 3. X-ray diffraction patterns of the mixture of BaTi_4O_9 and TiO_2 calcined at different temperatures without holding: (a) 800°C, (b) 900°C, (c) 1000°C, (d) 1100°C and (e) 1200°C.

ing. It is interesting to show that based on the analysis of SADP, the calcined phase was identified as the structure of BaTi_4O_9 . Moreover, there are not only some spots are not spherical but also many extra spots also appear in SADP, which implies that Ti species might diffuse in the BaTi_4O_9 without reaction and distort its lattice. Fig. 6

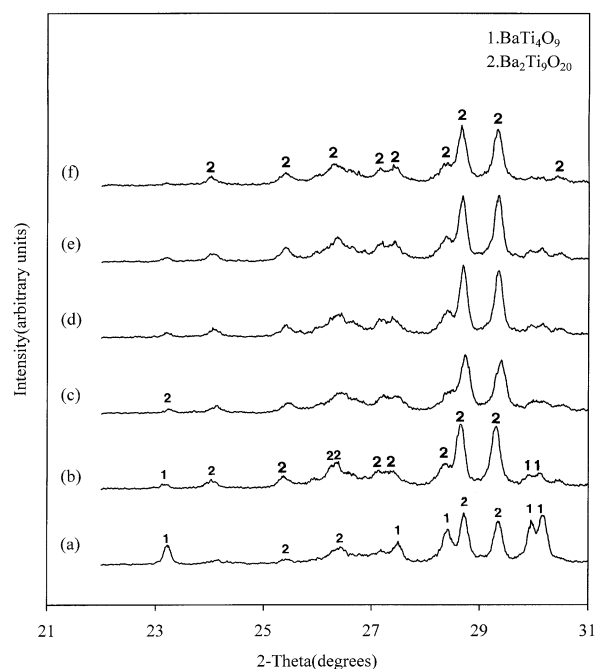


Fig. 4. X-ray diffraction patterns of the mixture of BaTi_4O_9 and TiO_2 isothermally heated at 1200°C for different times: (a) 1 h, (b) 3 h, (c) 9 h, (d) 15 h, (e) 20 h and (f) 30 h.

shows the BFI and SADP of the mixture of BaTi_4O_9 : $\text{TiO}_2 = 2:1$ calcined at 1200°C for 3 h. Based on the analysis of SADP, these nanometered grains (≈ 50 nm) observed at the local area of the sample were identified as the $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. Among the solid state reaction models,¹⁷ the Johnson–Mehl–Avrami (JMA) equation ($-\ln(1-x) = kt^n$) based on the model of the nucleation and growth,^{18,19} was found to have the best fit, shown in Fig. 7. The value of n representing the slope was evaluated as 0.5, which suggests that the particle shape is lath-shaped,¹⁷ supported by the microstructure shown in Fig. 8. Fig. 9 shows that most residual BaTi_4O_9 grains reveal twinning when $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ was apparently developed, which indicates that the residual BaTi_4O_9 grains might be stressed by $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ grains. Fig. 10 shows isothermal sintering behavior at different temperatures. The average activation energy about 1320 kJ/mol was evaluated in Fig. 11.

4. Discussion

Two intermediate phases, i.e., BaTi_4O_9 ^{1,4,5,11,20} and $\text{BaTi}_5\text{O}_{11}$ ^{6,8–10,20,21} were reported in forming $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. However, it should be pointed out that $\text{BaTi}_5\text{O}_{11}$ was never observed in using the solid-state reaction.^{1,4,5,11,22}

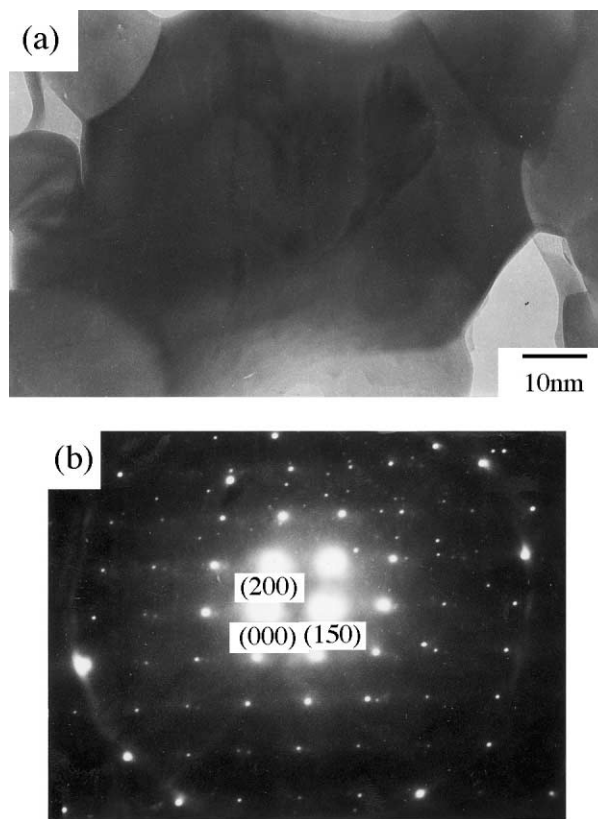


Fig. 5. (a) TEM bright-field image and (b) selected area diffraction pattern (zone axis: $[0\ 0\ \bar{1}0]$) for the mixture of BaTi_4O_9 and TiO_2 calcined at 1150°C without holding.

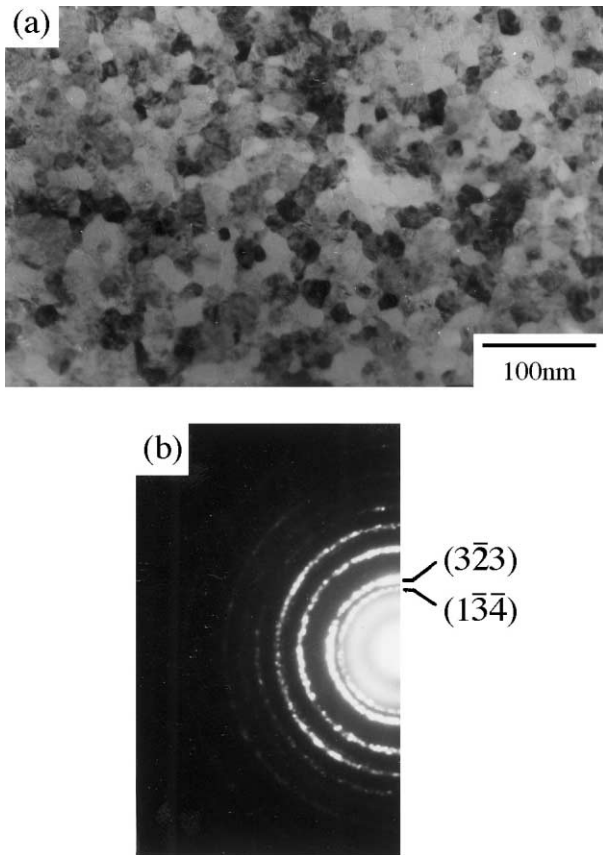


Fig. 6. The mixture of BaTi_4O_9 and TiO_2 calcined at 1200°C for 3 h showing the possible $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ nuclei (a), identified by the selected area diffraction pattern (b).

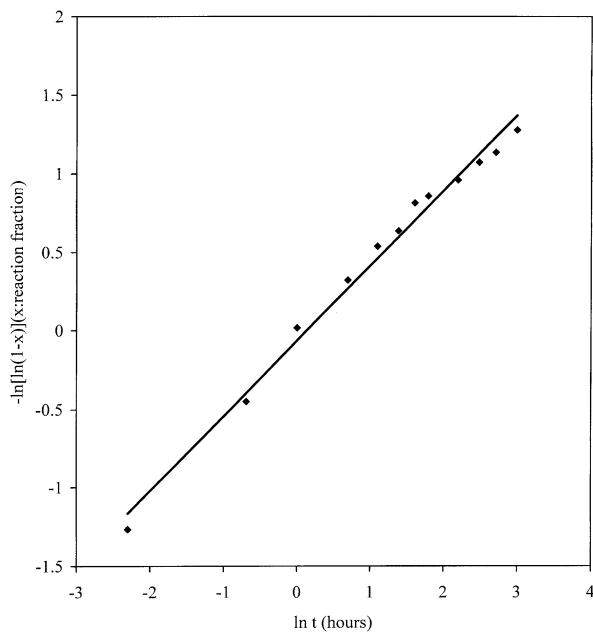


Fig. 7. Scaled reaction data fitted by the nucleation-growth model (Johnson–Mehl–Avrami equation).

This implies that mechanical mixing would be difficult in preparing a very high ratio of Ti/Ba, due to the fact that some precursor phase with a lower Ti/Ba ratio would form first and further reaction would have ions diffuse over a longer distance to form the desired phase. $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ was also reported to have such a problem.¹¹ In comparing Figs. 2 and 4, it was shown that under the same preparation conditions, the use of a mixture of BaTi_4O_9 and TiO_2 has smaller amount of BaTi_4O_9 remaining than that of BaCO_3 and TiO_2 in forming $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, which supports that the mixing might be a reason to explain the sluggish formation of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. However, the reason why the formation temperature was restricted in a very limited range of $1200\text{--}1300^\circ\text{C}$ would need to be further discussed.

Wu and Wang⁸ attributed the difficulty in preparing $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ to the high interface energy of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, based on the so-called bumps occurring at the grain boundaries shown in their microstructure. However, the so-called bumps could usually be observed in the ceramic microstructure with the second phase existing at the grain boundaries.²³ Moreover, the bumps were not observed in this investigation. Thus, in our opinion, the

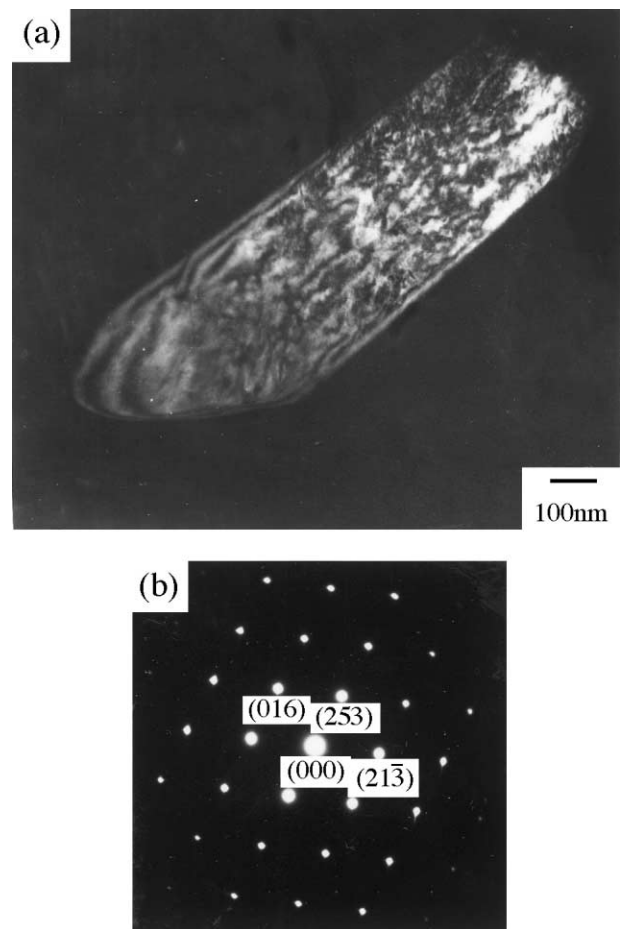


Fig. 8. The mixture of BaTi_4O_9 and TiO_2 calcined at 1200°C for 0.5 h showing the lath-shape particle (a), which was identified as $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ by the selected area diffraction pattern (zone axis: $[9\ \bar{1}2\ 2]$) (b).

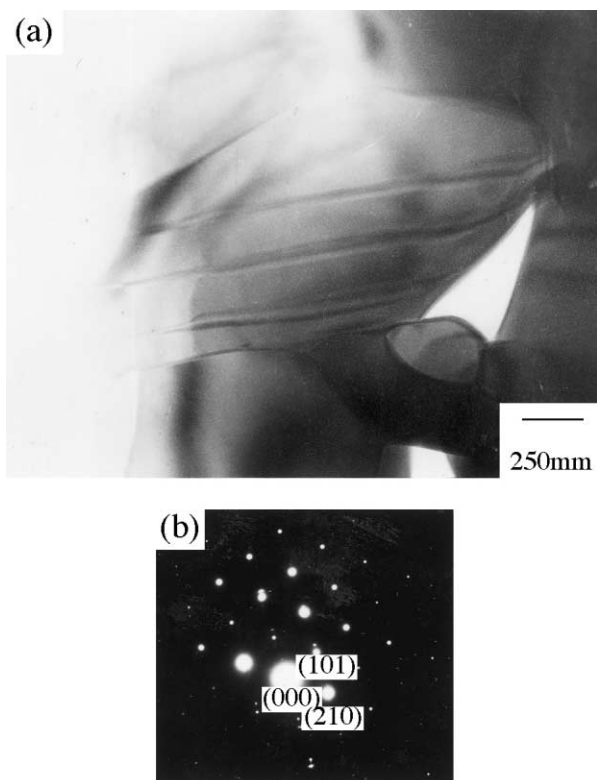


Fig. 9. A BaTi_4O_9 grain revealing twinning (a), identified by the selected area diffraction pattern (zone axis: $[1\ 2\ \bar{1}]$) (b).

suggestion about high interface energy of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ is misleading. Yu et al.¹³ proposed that stress might arise along the crystal structured layers because of the structural factor, which in turn would result in a high poten-

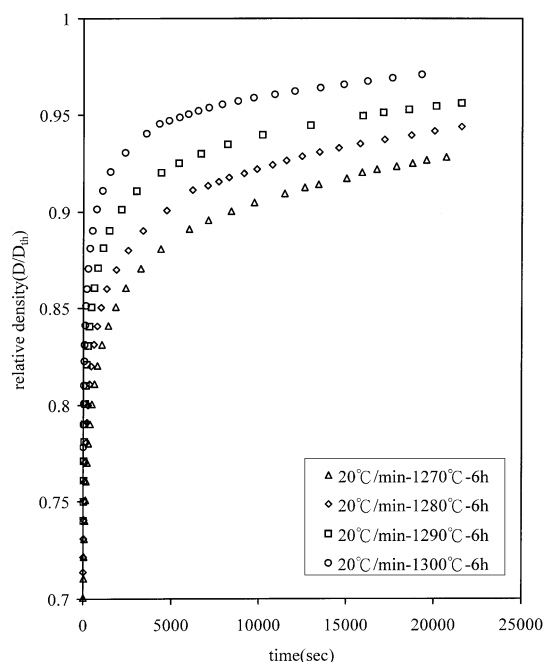


Fig. 10. Relative density versus time at different temperatures for $\text{Ba}_2\text{Ti}_9\text{O}_{20}$.

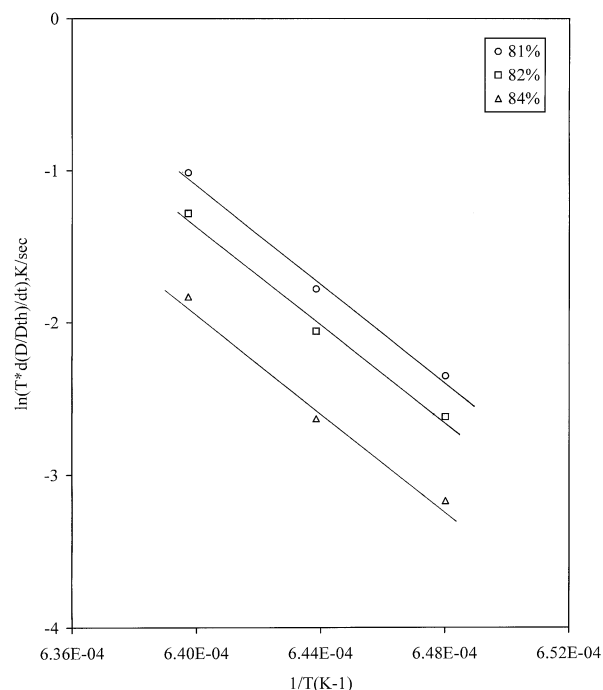


Fig. 11. Evaluation of the activation energy of isothermal sintering of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$.

tial-energy barrier for nucleation in the reaction. They argued that because the liquid phase arising from adding Bi_2O_3 did not promote the formation rate of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, the diffusion over a long distance is not a factor for the difficulty in preparing $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. However, as discussed above, diffusion over a long distance is due to the mixing problem, so even the liquid could provide a quick path for ions, it can not improve the mixing. Especially, when liquids occur locally, it would lead to inhomogeneous formation. Moreover, they thought that Al_2O_3 could form $\text{BaAl}_2\text{Ti}_6\text{O}_{16}$, which would intergrow with $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, and thus, decrease the height of the potential-energy barrier. However, this thinking is not convincing because intergrowth is commonly observed in layer-structured ceramics, e.g. in ferri-rite systems.²⁴

In Figs. 3 and 4, there are two things that should be pointed out, i.e. when temperatures were $< 1200^\circ\text{C}$, BaTi_4O_9 was still retained but TiO_2 has disappeared and when temperatures were $\geq 1200^\circ\text{C}$, $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ apparently started to develop. This implies that the Ti species might diffuse in BaTi_4O_9 but did not react with BaTi_4O_9 to form $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ when temperatures were $< 1200^\circ\text{C}$, which is supported by the SADP identified as the structure of BaTi_4O_9 shown in Fig. 5. Moreover, as observed in SADP, there are extra spots in the diffraction pattern, which implies that the Ti species might diffuse in BaTi_4O_9 without reaction and some spots were not spherical indicating that the lattice of BaTi_4O_9 was distorted. In Fig. 6, possible $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ nuclei were observed at some local areas of the sample prepared by

the mixture of BaTi_4O_9 and TiO_2 calcined at 1200°C for 3 h. Furthermore, the model of nucleation and growth was employed to evaluate the kinetics of solid-state reaction at 1200°C . It was found to have the best fit compared with other models,^{17,25,26} shown in Fig. 7. Based on the above discussion, the formation mechanism of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ could be attributed to the nucleation and growth, and 1200°C should be its nucleation temperature. However, the mechanism for forming the nuclei of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ is not realized and beyond the scope of this investigation.

The reason why it takes more than 20 more hours to eliminate the tracer amount of BaTi_4O_9 should be another issue. When $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ was apparently developed (Fig. 4), it was shown in Fig. 9 that most residual BaTi_4O_9 grains were found to contain twins, which implies that the remaining grains of BaTi_4O_9 were stressed by the surrounding $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ grains. It is evaluated that when $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ nucleated from the matrix of BaTi_4O_9 inserted by the Ti species, the structural volume expanded by about 7%, which in turn would stress BaTi_4O_9 . It should be noted that this evaluation of structural volume change is different from that of Wu and Wang,⁸ in which they considered the structural volume change to be due to a direct reaction of BaTi_4O_9 and TiO_2 at the interface. Because the remaining BaTi_4O_9 was stressed, it would be more difficult for it to nucleate $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, which explains why the residual amount of BaTi_4O_9 needs to take a longer time to be eliminated. Inferring from the above discussion, it is considered that to release the stress of the remaining BaTi_4O_9 might be a possible way to improve the preparation of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. Thus, we reground the mixture of BaTi_4O_9 and TiO_2 calcined at 1200°C for 3 h and reheated at 1200°C . It was found that $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ could be completely formed in 3 h, which implies that the stressed BaTi_4O_9 was released when the sample was reground. The obtained single-phase $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ powder was pressed and sintered at 1390°C without holding. The density, about 99% theoretical density and the grain size about 2–3 μm could be achieved, shown in

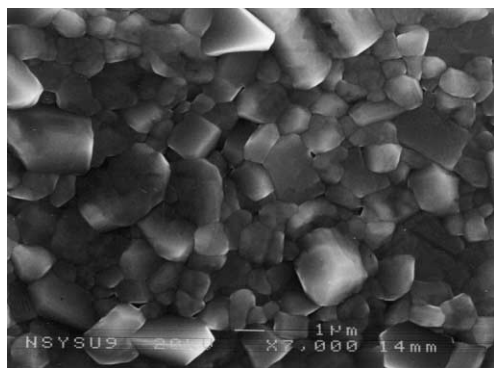


Fig. 12. A uniform microstructure of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ sintered at 1390°C without holding time with density about 99% theoretical density and grain size 2–3 μm .

Fig. 12 and the dielectric properties are dielectric constant 39, Q 5863 at 7.3 GHz, and the temperature coefficient of resonance frequency 5 ppm/ $^\circ\text{C}$.

5. Conclusions

(1) In preparing $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ by solid-state reaction, the use of the mixture of BaTi_4O_9 and TiO_2 is better than that of BaCO_3 and TiO_2 .

(2) The formation mechanism of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ might be via the nucleation and growth. It nucleated from the matrix of BaTi_4O_9 inserted by the Ti species rather than the direct reaction of BaTi_4O_9 and TiO_2 at the interface.

(3) The difficulty in completely forming $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ in a short time might be due to the fact that the remaining BaTi_4O_9 grains were stressed by the surrounding $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ grains.

(4) The evaluated activation energy of the isothermal sintering of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ is about 1320 kJ/mol. High-quality $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ ceramic with a density about 99% theoretical density and the grain size about 2–3 μm could be achieved and the dielectric properties are dielectric constant 39, Q 5863 at 7.3 GHz, and the temperature coefficient of resonance frequency 5 ppm/ $^\circ\text{C}$.

Acknowledgements

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