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# Effect of glass additives on the strength and toughness of polycrystalline alumina

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#### Abstract

The effect of stress at grain boundaries on the mechanical properties of alumina ceramics was investigated. Residual stresses at grain-boundaries resulted from a mismatch in thermal expansion coefficient (TEC) between the alumina matrix and the glass-phase segregated at grain-boundaries. The BaO–Al<sub>2</sub>O<sub>3</sub>–SiO<sub>2</sub> (BAS) system and the Li<sub>2</sub>O–Al<sub>2</sub>O<sub>3</sub>–SiO<sub>2</sub> (LAS) system glasses were chosen to have a higher and a lower TEC than that of alumina, respectively, resulting in microscopic tensile and compressive stresses at grain-boundaries for Al<sub>2</sub>O<sub>3</sub>/BAS and Al<sub>2</sub>O<sub>3</sub>/LAS composites, respectively. The experimental results showed that the Al<sub>2</sub>O<sub>3</sub>/BAS composite fractured intergranularly with a fracture toughness higher than that of monolithic alumina. On the other hand, the Al<sub>2</sub>O<sub>3</sub>/LAS composite experienced transgranular fracture and high bending strength despite its low toughness. Both composites could be sintered to full density at 1500°C for 2 h due to the presence of a liquid phase. It was concluded that strengthening and toughening of alumina ceramics could be tailored by designing their grain-boundary microstresses. © 2001 Elsevier Science Ltd. All rights reserved.

Keywords: Al<sub>2</sub>O<sub>3</sub>; Glass; Grain boundaries; Mechanical properties; Thermal expansion coefficient

### 1. Introduction

Most of ceramics are polycrystalline materials composed of grains and grain-boundaries whose physical and chemical characteristics can largely affect the structures properties of ceramics. 1-4 Practically, the important role of grain-boundaries has been widely recognized in designing and processing ceramics with high performance. For example, the concept of "grain-boundary engineering" makes a great contribution to the design of ceramics with improved structures properties, such as Si<sub>3</sub>N<sub>4</sub> and SiAlON ceramics.<sup>5–10</sup> It is also well known that grain-boundary chemistry can exert a significant effect on the mechanical properties of ceramics, such as strength, fracture toughness, creep and superplasticity. 11–18 As widely recognized in recent studies 19,20, if there is a difference in the shrinkage rate between grains and grain-boundary phase, residual stresses are induced

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at grain-boundaries during the cooling of the ceramics from sintering temperature. By a liquid-phase sintering process, ceramics can be sintered with different liquidforming additives which lower the sintering temperature, thus forming thin continuous or semicontinuous glass phases at grain boundaries. At room temperature, residual stress results from the mismatch in thermal expansion coefficient (TEC) of the grain-boundary glass and the crystalline matrix. 21,22 Residual microstress at grain-boundaries has a significant effect on the crack propagation mode and thus on the mechanical properties of polycrystalline ceramics. <sup>23–26</sup> Generally, when the TEC of the grain-boundary phase is greater than that of grains, a tensile stress field will be generated at grainboundaries. While, for equilibrium to be kept, compressive stress will be generated in the grains. The tensile stress at the grain boundary is expected to drive the crack path along the intergranular glass phase, resulting in intergranular fracture mode. This may in turn lead to a higher fracture toughness. When the TEC of the grain-boundary phase is lower than that of the crystalline grains, there will be compressive stress at grain

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boundaries, resulting in a transgranular fracture mode. Despite a low fracture toughness, these materials may show a high bending strength.<sup>27–30</sup> With this understanding, we can design residual stresses at ceramic grain-boundaries to achieve the desired mechanical properties.

In this paper, we studied the effect of grain-boundary stresses on the bending strength and fracture toughness of alumina ceramics with added BaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> (BAS) and Li<sub>2</sub>O-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> (LAS) glass-phases, whose TECs were chosen to be higher and lower than that of alumina grains, respectively. The barium aluminosilicate system is ideal for designing higher thermal expansion glass phases, because upon crystallization taking place during cooling, the high temperature form of the crystalline phase, BaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub> shows higher TEC than that of alumina. On the other hand, in the tri-element phase-diagram of the Li<sub>2</sub>O-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> system, there is a zone of lower TEC as compared to alumina. The present study discusses the possibility of controlling grainboundary stresses in order to confer desirable properties on alumina ceramics.

# 2. Experimental procedures

The LAS and BAS glasses were prepared by milling mixtures of 22.9 wt.% Al<sub>2</sub>O<sub>3</sub>, 60.4 wt.% SiO<sub>2</sub> with 16.7 wt.% Li<sub>2</sub>CO<sub>3</sub>, and 18.3 wt.% Al<sub>2</sub>O<sub>3</sub>, 24.9 wt.% SiO<sub>2</sub> with 56.8 wt.% BaCO<sub>3</sub>, respectively. Then, melting at 1550°C for 6 h and quenching in cold distilled water were performed. The transparent glasses were crushed to <1 mm and milled with high-purity alumina mediums. High-purity commercial alumina powder was, respectively, mixed with 5 wt.% BAS and 5 wt.% LAS glass powders in ethanol for 24 h using high-purity alumina balls. After drying, sieving through 120 µm net, PVA was added. The mixed powders were uniaxially pressed at 100 MPa and then cold isostatically pressed at 250 MPa. The green samples were packed in loose alumina powder inside an alumina crucible and calcined at 700°C for 1 h, followed by sintering at 1500°C for 2 h. For comparison, monolithic alumina was also prepared by the same sintering schedule.

The bending strength was measured in three-point bending with a span of 20 mm and a crossed speed at 0.5 mm/min at room temperature using an Instron 1195 Universal Test Machine. The tensile surface of the bend bars was polished and the edge chamfered to mirror surface. The dimension of test pieces was  $2.5 \times 5 \times 25$  mm. Fracture toughness,  $K_{\rm IC}$ , was determined using an indentation technique with a Vicker Indenter (AKASHI) using 98N load. The equation used for calculating  $K_{\rm IC}$  was that proposed by Anstis et al.<sup>31</sup> A number of specimens  $\geq 6$  was tested for each data point. The thermal expansion coefficient of the bulk glasses was measured using an alumina rod dilatometer (Netzsch-402ES, Germany).

The presence of crystalline phases of sintered bulk samples was identified by X-ray diffraction (XRD) (D/ max-radiffractometer, Rigaku, Japan) analysis with Ni filtered  $CuK_{\alpha}$  radiation. The samples for microstructural observation were cut from the sintered bodies, polished and chemically etched in 0.1 N HF acid at 50°C for 8-10 s. Both etched surfaces and fracture surfaces were observed with a scanning electron microscope (SEM) (EPMA-8705QHz, Shimadzu, Japan). A transmission electron microscope (TEM) (JEM-200cx, JEM-400cx, Jeol, Japan) equipped with X-ray energy dispersive spectroscopy (EDS) was used to obtain the chemical composition of the grain boundary phases. TEM specimens were prepared following the standard procedure of cutting, polishing and Ar-ion-milling to perforation. TEM specimens were coated with a thin layer of evaporated carbon to suppress charging.

### 3. Results and discussion

#### 3.1. Microstructural characterizations

The X-ray diffraction patterns of the sintered samples are shown in Fig. 1. It can be seen from the figure that the only crystalline phase in the  $Al_2O_3/5$  wt.% LAS composite is  $\alpha$ - $Al_2O_3$  phase, while the crystalline phases

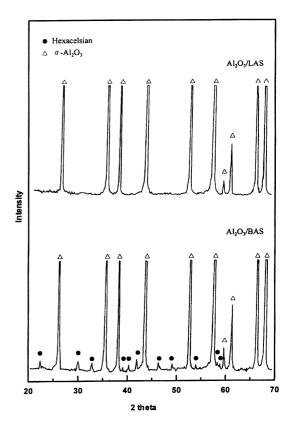


Fig. 1. XRD pattern of  $Al_2O_3/5$  wt.% LAS and  $Al_2O_3/5$  wt.% BAS composites sintered at  $1500^{\circ}C$  for 2 h.

in the  $Al_2O_3/5$  wt.% BAS composite are  $\alpha$ - $Al_2O_3$  phase and a minor fraction of hexacelsian phase. This indicates that LAS glass in the composite did not crystallize during cooling, while BAS glass showed a slight crystallization. The different crystallization behavior is thought to be due to both differences in glass composition and crystallization kinetics.

SEM micrographs of polished surfaces are shown in Fig. 2(a) and (b) for the  $Al_2O_3/5$  wt.% LAS and  $Al_2O_3/5$ 5 wt. % BAS, respectively. The microstructure in Fig. 2(a) shows both equaxied and platelet α-Al<sub>2</sub>O<sub>3</sub> grains of a similar size. When etching, the glass phase at grain boundaries and triple-grains junctions was leached out. The resulting Al<sub>2</sub>O<sub>3</sub> skeleton suggests that alumina and glass were interpenetrating phases. For Al<sub>2</sub>O<sub>3</sub>/LAS composite, a TEM analysis revealed no crystalline phases, as shown in Fig. 3, the selected-area diffraction (SAD) patterns at triple-grain junctions systematically showing a halo pattern, inset in Fig. 3. A combined analysis of TEM and EDS indicated that the glass-phase at triple-grain junctions possessed an average composition of  $15.2\pm0.2$  mol% Li<sub>2</sub>O,  $16.0\pm0.3$  mol% Al<sub>2</sub>O<sub>3</sub> and  $68.8\pm0.2$  mol% SiO<sub>2</sub>. Fig. 2(b) for the Al<sub>2</sub>O<sub>3</sub>/BAS composite shows almost equaxied α-Al<sub>2</sub>O<sub>3</sub> grains with a minor fraction small crystallines precipitated from the liquid-phase at triple-grain junctions, the glass residue being etched out. The LAS system reveals some extended Al<sub>2</sub>O<sub>3</sub> regions and the BAS system shows continuous grain-boundary wetting, this difference was due to the different etching ratio and grain-boundary width for LAS and BAS glasses. The differences in wetting behavior and glass phase/ Al<sub>2</sub>O<sub>3</sub> distribution also may have some effects. A TEM image of the Al<sub>2</sub>O<sub>3</sub>/BAS composite is shown in Fig. 4 that reveals the presence of both residual glass-phase and crystalline phase. The SAD pattern collected at the location A inset in Fig. 4 confirms the presence of amorphous phase. Quantitative EDS analyses of the precipitated crystalline phase at triple-grain junctions (region A in Fig. 5) yielded an average composition of  $32.8\pm0.5$  mol% BaO,  $19.8\pm0.2$  mol% Al<sub>2</sub>O<sub>3</sub> and  $47.4\pm0.4$  mol% SiO<sub>2</sub>, which is not far from the stoichiometric composition of BaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>, the EDS is shown in Fig. 6. Chemical identification of the hexacelsian phase was confirmed by electron diffraction pattern, shown in Fig. 5. Having both the investigated ceramics a similar grain size, it is originated that composition and viscosity

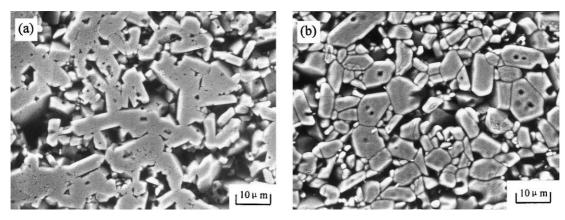


Fig. 2. SEM micrographs of composite etched surfaces: (a) Al<sub>2</sub>O<sub>3</sub>/5 wt.% LAS; (b) Al<sub>2</sub>O<sub>3</sub>/5 wt.% BAS.

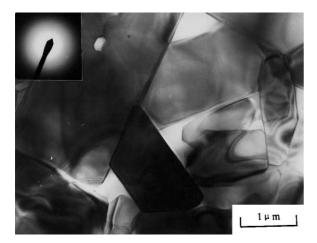


Fig. 3. TEM microstructural characteristics of Al<sub>2</sub>O<sub>3</sub>/5 wt.% LAS composite with an EDS pattern of grain boundaries.

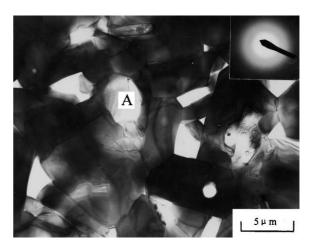


Fig. 4. TEM microstructural characteristics of Al<sub>2</sub>O<sub>3</sub>/5 wt.% BAS composite with an EDS pattern of point A.

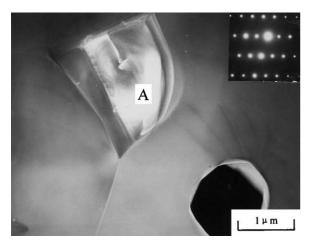


Fig. 5. TEM micrograph of three-grain boundary of Al<sub>2</sub>O<sub>3</sub>/5 wt.% BAS composite with an EDS pattern point of A.

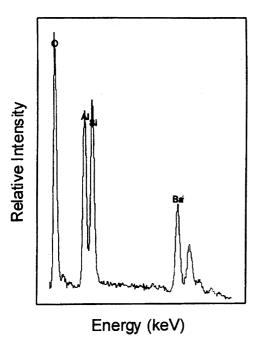
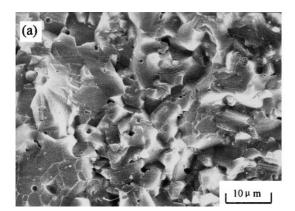


Fig. 6. An EDX spectrum obtained from the region shown in point A in Fig. 6.

of LAS and BAS glasses have no significant influence on the microstructure for Al<sub>2</sub>O<sub>3</sub>-based composites. SEM micrographs of fracture surfaces of the composites are shown in Fig. 7. The fracture mode for Al<sub>2</sub>O<sub>3</sub>/LAS and Al<sub>2</sub>O<sub>3</sub>/BAS composites was almost completely transgranular and intergranular, respectively.

# 3.2. Residual stresses and mechanical properties

Table 1 lists the TEC of intergranular glasses and the mechanical properties of Al<sub>2</sub>O<sub>3</sub>/5 wt.% LAS and Al<sub>2</sub>O<sub>3</sub>/ 5 wt.% BAS composites in comparison with monolith Al<sub>2</sub>O<sub>3</sub>. It can be seen from the table that the Al<sub>2</sub>O<sub>3</sub>/LAS composite experience higher bending strength and lower fracture toughness than monolithic Al<sub>2</sub>O<sub>3</sub> ceramics, while the opposite trend is found for Al<sub>2</sub>O<sub>3</sub>/BAS. This can be attributed to the different residual stresses at grain-boundaries, resulting from the difference in TEC between alumina grains and the glass-phase. Since the precise composition of the glass is known, it is possible to estimate the TEC value of the glass from standard data using a linear equation.32 The LAS glass-phase in this study had TEC of  $4.36 \times 10^{-6}$  K<sup>-1</sup>, lower than that of  $Al_2O_3$  (6-8×10<sup>-6</sup> K<sup>-1</sup>), thus compressive stress formed at grain boundaries inhibiting the crack to propagate in intergranular fashion. Stress fringes resulting from stress created by thermal expansion mismatch could be observed by TEM in the alumina grain, as shown by arrow in Fig. 3. The BAS glass and the crystalline hexacelsian phase  $(\alpha \ge 8.0 \times 10^{-7})^{\circ}$ C)<sup>33</sup> had higher TEC than Al<sub>2</sub>O<sub>3</sub>, the TEC of BAS glass also increasing upon crystallization, so the residual stresses developed at grain boundaries is expected to be of tensile stress. Microcracks resulted from such tensile stresses that can be seen in Fig. 5 (shown by arrow), as a result of the higher thermal expansion of both hexacelsian phase and BAS glassphase trapped within the alumina grains (point B). Grain-boundary microcracking, generated by grainboundary tensile microstresses, triggers intergranular fracture and results in a higher fracture toughness, but a lower bending strength.



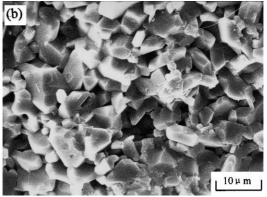


Fig. 7. SEM micrographs of composite fracture surfaces: (a) Al<sub>2</sub>O<sub>3</sub>/5 wt.% LAS; (b) Al<sub>2</sub>O<sub>3</sub>/5 wt.% BAS.

Table 1
The composition and TEC of the glass and the mechanical properties of the composites

Composites	Glass compostion (wt.%)				$\alpha~(10^{-6}/^{\circ}\text{C})$	Bending strength (MPa)	Fracture toughness (MPa m <sup>1/2</sup> )
	Al <sub>2</sub> O <sub>3</sub>	SiO <sub>2</sub>	Li <sub>2</sub> O	BaO			
Al <sub>2</sub> O <sub>3</sub> /5 wt.% LAS	25.4	67.1	7.5	_	4.36	404±30	3.44±0.2
Al <sub>2</sub> O <sub>3</sub> /5 wt.% BAS	21.0	28.5	_	50.5	10.7	$273 \pm 42$	$4.76 \pm 0.3$
$Al_2O_3$	-	-	-	-	6–8	$336 \pm 28$	$3.80 \pm 0.2$

### 4. Conclusion

- 1.  $Al_2O_3/5$  wt.% BAS composite sintered at  $1500^{\circ}C$  for 2 h showed intergranular fracture mode with an average fracture toughness of  $4.76\pm0.3$  MPa·m<sup>1/2</sup> and bending strength  $273\pm42$  MPa because the BAS glass have higher TEC than alumina, resulting in tensile microstresses at grain boundaries.
- 2.  $Al_2O_3/5$  wt.% LAS composite sintered at  $1500^{\circ}$ C for 2 h showed transgranular fracture mode with an average fracture toughness of  $3.44\pm0.2$  MPa  $m^{1/2}$  and bending strength of  $404\pm30$  MPa, because the LAS glass has lower TEC than  $Al_2O_3$  and results in compression microstresses at grain boundaries.
- 3. Strengthening or toughening in alumina ceramics can be achieved by adding glass-phases with suitable TEC, higher and lower TEC than alumina resulting in high toughness and high strength polycrystals, respectively.

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