

# High temperature deformation of ceramic particle composites

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Received 8 March 2011; received in revised form 8 June 2011; accepted 2 July 2011

Available online 19 August 2011

## Abstract

The particle composites  $\text{Al}_2\text{O}_3/(2 \text{ and } 3\text{Y})\text{TZP}$  and  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$  were tested in bending at temperature of  $1280^\circ\text{C}$  over strain rates from  $3.4 \times 10^{-7}$  to  $1 \times 10^{-4} \text{ s}^{-1}$  and over stresses from 23 to 85 MPa. Strain rate of the composites decreased as a volume fraction of  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$  increased.  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$  composites deformed easier under the comparable conditions than alumina/zirconia composites. Four models of composite creep behaviour were compared to the experimental data. All the models were unsuitable for  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$ , in turn an isostress, an isostrain and a constrained isostrain models provide the good predictions for creep rates for alumina/zirconia ceramics, but the rheological model appeared not good. The threshold stresses approach seems to be useful for describing superplastic flow of  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$  composites.

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**Keywords:** Superplasticity; Bending test; Strain rate; Composite; Tetragonal  $\text{ZrO}_2$ ; Threshold stress

## 1. Introduction

Chemical and thermal stability, relatively good strength and fracture toughness, thermal and electrical insulation characteristics of alumina ( $\text{Al}_2\text{O}_3$ ) combined with availability in abundance and low cost of the material resources are advantageous for commercial engineering applications of this ceramics.<sup>1</sup> In turn magnesium aluminate spinel ( $\text{MgAl}_2\text{O}_4$ ) seems to be a good candidate ceramics for nuclear applications.<sup>2</sup> Spinel shows high resistance to the formation of defects under the influence of neutron irradiation and hence the change in mechanical properties is not critical. However in some applications the strength and fracture toughness of alumina and spinel are not sufficient. In these case zirconia ( $\text{ZrO}_2$ ) particles are frequently employed as toughening agents for these ceramics.<sup>3–6</sup> Zirconia has three crystallographic forms, namely: monoclinic (m), tetragonal (t) and cubic (c) phases.<sup>7,8</sup> The transformation of pure zirconia from t-phase to m-phase occurs at a temperature about  $950^\circ\text{C}$ , which is accompanied by a volume expansion of 4%. This volume expansion generates stresses which prohibit the opening of an advancing crack, so the toughness of zirconia at room temperature is high compared with other

ceramics. The phase transformation temperature from t to m can be lowered by doping with suitable oxides such as  $\text{Y}_2\text{O}_3$ ,  $\text{CeO}_2$ ,  $\text{CaO}$ ,  $\text{MgO}$ , etc. For grain size lower than a critical size t-phase at room temperature is stable. Zirconia stabilized by 2–3 mol%  $\text{Y}_2\text{O}_3$  consists almost 100% tetragonal phase.<sup>7,8</sup> These ceramics attained strength about 1.5 GPa<sup>7</sup> and fracture toughness about  $7 \text{ MPa m}^{1/2}$  and therefore they are mainly used as toughening components in the mentioned above ceramics. It should be also noticed that the composite consisting of 80 wt%  $\text{ZrO}_2$  (stabilized by 2 mol%  $\text{Y}_2\text{O}_3$ ) and 20 wt%  $\text{Al}_2\text{O}_3$  (28 vol%) attained strength values about 2.5 GPa (after hot isostatic pressing in the last stage of manufacture).<sup>8</sup> Then it is a great interest of application of the ceramic materials in some tools and engine parts production but obtaining of ceramic elements is not easy and cheap because of brittleness and hardness of ceramics at room temperature. To some extent an opportunity of easy shaping and joining of them is created by superplasticity. This phenomenon, well known in metallic materials,<sup>9</sup> was demonstrated for the first time for ceramic materials for 3 mol%  $\text{Y}_2\text{O}_3$  stabilized tetragonal  $\text{ZrO}_2$  in 1985 in Japan by Wakai et al. The publication of the results of their work took place in 1986.<sup>10</sup> Since then many articles concerning superplasticity in ceramics have been published. Some of them describe superplastic flow in tetragonal zirconia,<sup>11–13</sup> alumina,<sup>14</sup>  $\text{MgAl}_2\text{O}_4$  spinel,<sup>15</sup> alumina–zirconia<sup>16–18</sup> and spinel–zirconia composites.<sup>19,20</sup> These composites are an object of the main interest of this paper. In the present investigation, the influence of

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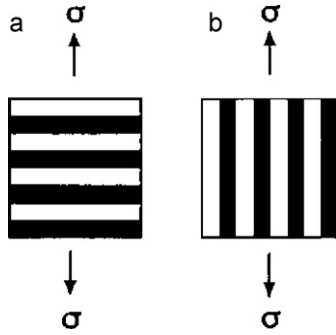


Fig. 1. Schematic diagram showing (a) isostress and (b) isostrain model.

alumina and spinel volume fraction on strain rate of  $\text{Al}_2\text{O}_3/\text{ZrO}_2$  and  $\text{MgAl}_2\text{O}_4/\text{ZrO}_2$  particulate composites at  $1280^\circ\text{C}$  in bending test is studied. These experimental conditions were chosen in order to avoid of grain size growth or cavitation nucleation during the test. For comparison, in<sup>12–20</sup> the compression and tensile tests were made at temperatures usually higher than  $1280^\circ\text{C}$  and hence a strain reached there about several hundred percent, but in our case it does not exceed 2%.

## 2. Theoretical background

The creep and superplasticity in the material can be described by the following equation<sup>11–14</sup>:

$$\dot{\varepsilon} = \frac{A_0 D G b}{k T} \left( \frac{b}{d} \right)^p \left( \frac{\sigma}{G} \right)^n \quad (1)$$

where  $\dot{\varepsilon} = d\varepsilon/dt$  is the strain rate,  $A_0$  is a dimensionless constant,  $D$  is the diffusion coefficient [ $=D_0 \exp(-Q/RT)$ , where  $D_0$  is the frequency factor,  $Q$  the activation energy and  $R$  the gas constant],  $\sigma$  is the applied stress,  $G$  is the shear modulus,  $b$  is the Burgers vector,  $d$  is the grain size,  $k$  is Boltzmann's constant,  $p$  is the inverse grain size exponent and  $n$  is the stress exponent.

In order to describe two-phase particle composite behaviour several models were proposed.<sup>21,22</sup> Two of them, so-called isostress and isostrain model,<sup>21</sup> based on the standard composite theory (rule of mixture -ROM). The third, so-called rheological model,<sup>22</sup> based on assumption that one phase is rigid and the other is deformable. ROM models (Fig. 1) assume that the duplex microstructure can be simplified to one that consists of plates of each phase. Two conditions can be fulfilled: (a) isostress (plates are aligned perpendicular to the applied stress), where the stress is the same in each phase, and (b) isostrain (where the plates are parallel to the applied stress), where the strain and strain rate are the same for each phase.

The composite strain rate for isostress case is given by the relation

$$\dot{\varepsilon} = V_1 \dot{\varepsilon}_1 + (1 - V_1) \dot{\varepsilon}_2 \quad (2)$$

where  $V_1$  and  $\dot{\varepsilon}_1$  are the volume fraction and strain rate of component one and  $(1 - V_1)$  and  $\dot{\varepsilon}_2$  are the volume fraction and strain rate of component two.

The stress in the composite for isostrain case is given by the relation

$$\sigma = V_1 \sigma_1 + (1 - V_1) \sigma_2 \quad (3)$$

Assuming that each component obeys Eqs. (1) and (3) is given by

$$\sigma = V_1 K_1 \dot{\varepsilon}^{1/n_1} + (1 - V_1) K_2 \dot{\varepsilon}^{1/n_2} \quad (4)$$

where  $K_i = G(kT/A_0 D G b)^{1/n_i} (d/b)^{p/n_i}$  for each component  $i$ .

An analytical solution of Eq. (4) for  $\dot{\varepsilon}$  as a function of  $V_1$  is not possible for  $n_1 \neq n_2$ . However Eq. (4) can be rearranged to provide a solution for  $V_1$  as a function of  $\dot{\varepsilon}$  as

$$V_1 = \frac{\sigma - K_2 \dot{\varepsilon}^{1/n_2}}{K_1 \dot{\varepsilon}^{1/n_1} - K_2 \dot{\varepsilon}^{1/n_2}} \quad (5)$$

So the values of  $\dot{\varepsilon}$  which give  $0 < V_1 < 1$  are those of interest. These are the values which fall between  $\dot{\varepsilon}_1$  and  $\dot{\varepsilon}_2$  for the given applied stress. It is then a matter of determining the values of  $V_1$  as a function of  $\dot{\varepsilon}$ , then plotting  $\dot{\varepsilon}$  as a function of  $V_1$ .

By assuming that the stress exponents in each phase are equal (i.e.  $n = n_1 = n_2$  – constrained isostrain model<sup>18</sup>), Eq. (4) can be simplified and written in the terms of the composite strain rate,  $\dot{\varepsilon}$ :

$$\dot{\varepsilon} = \frac{\sigma^n}{(V_1 K_1 + (1 - V_1) K_2)^n} \quad (6)$$

In the rheological model<sup>22</sup> the strain rate of the composite is given by

$$\dot{\varepsilon} = \dot{\varepsilon}_2 (1 - V_1)^{2+n_2/2} \quad (7)$$

where  $\dot{\varepsilon}_2$  is the strain rate of the deformable matrix,  $V_1$  is the volume fraction of the rigid inclusions,  $n_2$  is the stress exponent of the matrix.

## 3. Experimental procedure

The starting materials were powders of  $\text{Al}_2\text{O}_3$  (AKP-53, 99.99% purity, Sumitomo Chemicals Co. Ltd., Japan),  $\text{MgAl}_2\text{O}_4$  (S30CR, 99% purity, Bajkalox, France) and 2 and 3 mol% yttria stabilized tetragonal  $\text{ZrO}_2$  (2Y and 3Y-TZP, 99.9% purity, Tosoh, Japan). The following types of composites were made: A –  $\text{Al}_2\text{O}_3/3\text{Y-TZP}$ , B –  $\text{Al}_2\text{O}_3/2\text{Y-TZP}$  and S –  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$ . The basic constituents and several mixtures of these for the composites were ball milled in water. After drying and granulation the plates were obtained by uniaxial pressing at 20 MPa, isostatical pressing at 120 MPa and then sintering for 2 h in air accordingly at 1500, 1600 and  $1630^\circ\text{C}$  for A, B and S composites. From the sintered plates the bars of 1 mm height, 4 mm width and 30 mm length were machined. Some samples were polished and thermally etched at temperatures  $50^\circ\text{C}$  less than the sintering temperature for 1 h in vacuum. The electron scanning microscope micrographs of the etched samples were used for measurements of average grain size by Feret's diameter method.

The creep tests were performed in four-point bending geometry (upper and support span were accordingly 10 and 20 mm) under constant load at  $1280^\circ\text{C}$  using Zwick 1446 universal

Table 1  
Grain sizes for composites A (Al<sub>2</sub>O<sub>3</sub>/3Y-TZP).

Designation	$d_{\text{Al}_2\text{O}_3}$ (μm)	$d_{\text{ZrO}_2}$ (μm)
3Y-TZP		0.47 ± 0.13
28A	0.31 ± 0.06	0.18 ± 0.04
50A	0.30 ± 0.08	0.22 ± 0.19
70A	0.35 ± 0.09	0.27 ± 0.17
86A	0.37 ± 0.19	0.33 ± 0.19
Al <sub>2</sub> O <sub>3</sub>	0.87 ± 0.49	

All of the composites exhibit densities ≥97% of theoretical density.

Table 2  
Grain sizes for composites B (Al<sub>2</sub>O<sub>3</sub>/2Y-TZP).

Designation	$d_{\text{Al}_2\text{O}_3}$ (μm)	$d_{\text{ZrO}_2}$ (μm)
2Y-TZP		0.48 ± 0.23
10B	0.39 ± 0.12	0.51 ± 0.33
20B	0.46 ± 0.19	0.57 ± 0.36
40B	0.55 ± 0.22	0.42 ± 0.19
60B	0.83 ± 0.19	0.40 ± 0.16
80B	1.14 ± 0.41	0.36 ± 0.12
Al <sub>2</sub> O <sub>3</sub>	0.87 ± 0.49	

All of the composites exhibit densities ≥99% of theoretical density.

machine. The maximum strain of samples was not more than 2%, but maximum test time was not more than 4 h. Strain rate  $\dot{\epsilon}$  vs. stress  $\sigma$  was calculated from experimental data accordingly to.<sup>23</sup>

#### 4. Results

Scanning electron micrographs of the selected basic components and composites are shown in Fig. 2. Compositions are designated by the volume fraction of Al<sub>2</sub>O<sub>3</sub> or MgAl<sub>2</sub>O<sub>4</sub>; for example, 86A contains 86 vol% Al<sub>2</sub>O<sub>3</sub> and 14 vol% 3Y-TZP. Average grain sizes with standard deviations are given in Tables 1–3. Microstructure analysis of the composites after testing was not made, but relatively low temperature and small deformation allow us assume that the increase in grain size is negligible. This assumption is supported by the results of<sup>18</sup> where the grain size increase in compression tested

Table 3  
Grain sizes for composites S (MgAl<sub>2</sub>O<sub>4</sub>/3Y-TZP).

Designation	$d_{\text{MgAl}_2\text{O}_4}$ (μm)	$d_{\text{ZrO}_2}$ (μm)
3Y-TZP		0.47 ± 0.13
10S	0.92 ± 0.40	1.21 ± 0.66
20S	1.03 ± 0.56	1.35 ± 0.57
30S	1.19 ± 0.28	1.10 ± 0.49
40S	1.23 ± 0.34	1.20 ± 0.31
50S	1.05 ± 0.28	0.98 ± 0.19
60S	1.13 ± 0.35	0.97 ± 0.25
70S	1.21 ± 0.74	0.77 ± 0.21
80S	1.81 ± 0.72	0.53 ± 0.18
85S	2.18 ± 0.88	0.74 ± 0.26
90S	1.97 ± 0.59	0.53 ± 0.14
95S	1.03 ± 0.34	0.56 ± 0.14
MgAl <sub>2</sub> O <sub>4</sub>	1.91 ± 1.71	

All of the composites exhibit densities ≥96% of theoretical density.

Al<sub>2</sub>O<sub>3</sub>/3Y-TZP composites at temperature 1350 °C (higher than in our case) was insignificant.

The relationships between stress and strain rate were analyzed in log–log scales from which stress exponent  $n$  was derived (see Eq. (1)). Values of  $n$  as a function of volume fraction of Al<sub>2</sub>O<sub>3</sub> or MgAl<sub>2</sub>O<sub>4</sub> are shown in Fig. 3.

As it is seen that for  $n$  varies from 1.4 to 3.0, 1.7 to 2.9 and 1.8 to 3.1 for A, B and S composites, respectively. They are scattered around the value  $n=2$  (especially for A and B composites). Hence the results of strain rate measurements for the studied composites are plotted on  $(d\epsilon/dt)^{1/2} - \sigma$  scales (Fig. 4). It is shown in Fig. 4 that the experimental data could be fit by a linear function  $(d\epsilon/dt)^{1/2}$  of  $\sigma$  and that Al<sub>2</sub>O<sub>3</sub> and MgAl<sub>2</sub>O<sub>4</sub> can be treated as a rigid phase (strain rate of the composites decreases as volume fraction of Al<sub>2</sub>O<sub>3</sub> or MgAl<sub>2</sub>O<sub>4</sub> increases).

#### 5. Discussion

The obtained data of superplastic flow measurements of the composites were next analyzed using models presented in Section 2. Fig. 5 presents the plots of the logarithm of strain rate against volume fraction of Al<sub>2</sub>O<sub>3</sub> or MgAl<sub>2</sub>O<sub>4</sub> for A, B and S composites at flow stress of 50 MPa. The curves for isostress, isostrain and rheological model were obtained using end-constituents data (i.e.  $n_i$ ,  $\dot{\epsilon}_i$ ,  $K_i$ ) for Al<sub>2</sub>O<sub>3</sub> or MgAl<sub>2</sub>O<sub>4</sub> ( $i=1$ ) and 2Y-TZP or 3Y-TZP ( $i=2$ ), but for constrained isostrain model experimental data were fit using least-squares method to Eq. (6) with  $n=2$  rewritten as:

$$y = V_1(K_1 - K_2) + K_2 \quad (8)$$

where  $y = \sigma/\sqrt{\dot{\epsilon}}$  and  $\sigma = 50$  MPa

Values of parameters, including fitting parameters  $K_1$  and  $K_2$  for constrained isostrain model, used for calculating of model curves are placed in Table 4.

Observations of Fig. 5 lead to the following conclusions:

- For composites A for volume fraction of Al<sub>2</sub>O<sub>3</sub>  $V_1 \leq 0.5$  the experimental points are arranged around the isostress model curve, but for  $V_1 > 0.5$  they are arranged around the isostrain and constrained isostrain model curve.
- For the composite B the constrained isostrain model provides the best fit to the experimental data.
- In the case of the composite S proposed models do not practically fit the experimental data.
- The rheological model seems to be useless for the data interpretations.

In order to extend a discussion of the results the comparison of the studied composites was conducted in Fig. 6. It can be seen that strain rates for composites A and S are similar but for B are lower than for A and S. Reason why the strain rate for the composite A is higher than for B is obvious; since composite A grain sizes are smaller than for B. This is why the composites A and S have similar rates of strain will be discussed below.

In order to interpret the results of superplastic deformation measurements of the composites one can hypothesize that the

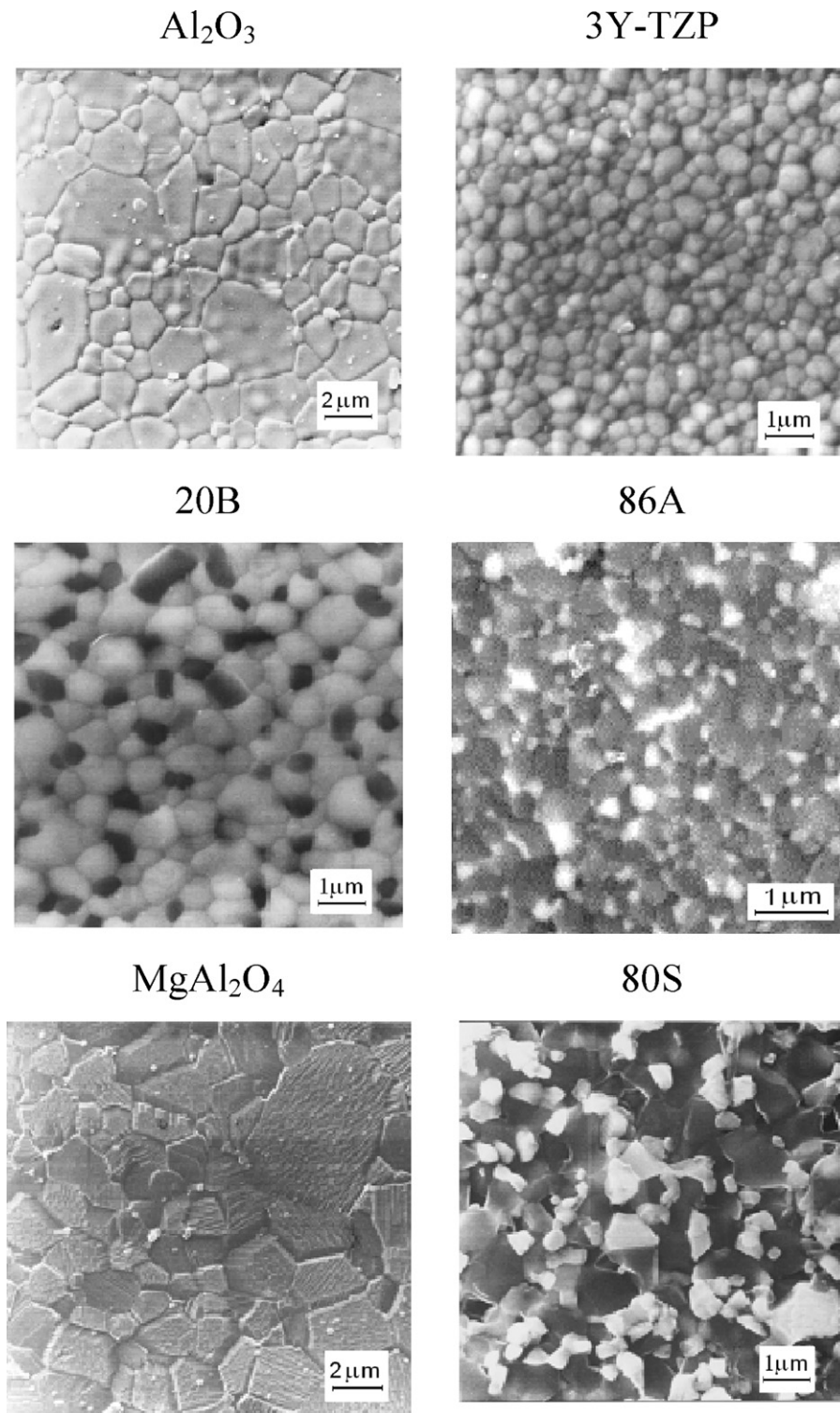


Fig. 2. Scanning electron micrographs of polished and etched surfaces of the selected studied materials. The grains (in composites) with the light shading are 3Y-TZP or 2Y-TZP and the grains with the dark shading are  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$ .

interaction of the components of both phases, i.e. the diffusion of ions  $\text{Zr}^{4+}$  and  $\text{Y}^{3+}$  into  $\text{Al}_2\text{O}_3$  and  $\text{MgAl}_2\text{O}_4$  grains and  $\text{Al}^{3+}$  and  $\text{Mg}^{2+}$  ions into  $\text{ZrO}_2$  grains during the sintering process could significantly affect superplastic flow.<sup>17,19</sup> It was shown in<sup>24,25</sup> that the presence of ions  $\text{Zr}^{4+}$  and  $\text{Y}^{3+}$  on the grain boundaries of alumina decreases the rate of diffusion

of the matrix ions, thus reducing the strain rate of this phase. In turn, in the case of  $\text{ZrO}_2$   $\text{Al}^{3+}$  and  $\text{Mg}^{2+}$  ions strengthen the ability of the matrix superplastic deformation,<sup>26–28</sup> but literature data on the diffusion of ions such as zirconium and yttrium into spinel grains and its effects on the superplastic behaviour of this material were not found. Thus strain rate

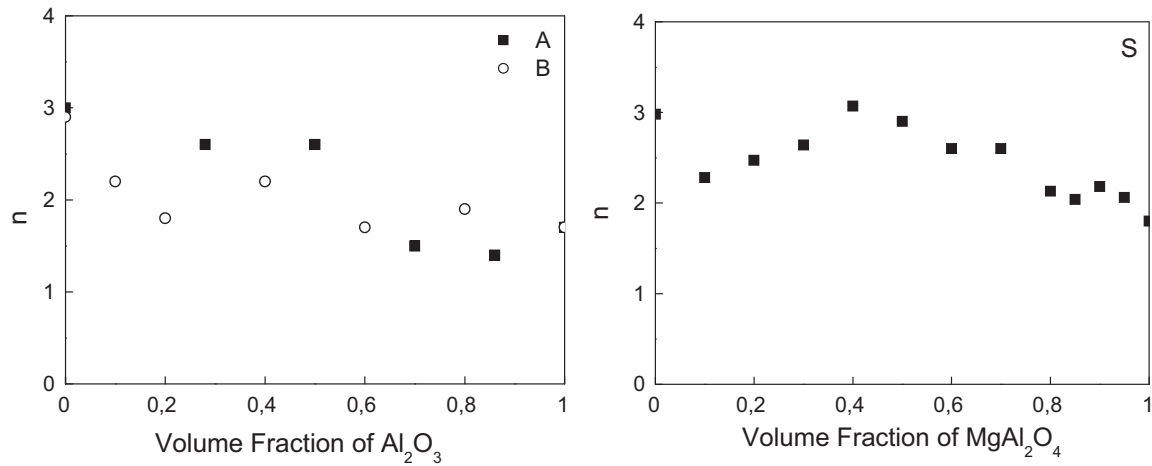


Fig. 3. Stress exponent  $n$  as a function of volume fraction of  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$  for A, B and S composites at temperature  $1280^\circ\text{C}$ .

cannot be interpreted here simply with the classical rule of mixtures. This is particularly evident in Fig. 5 in the case of composite B, where the average grain size of the composite are comparable with those for the starting materials (see Table 2). The experimental points corresponding to the  $V_1 > 0.5$  lie below the isostrain curve. This is probably due to a significant reduction in the superplastic deformation of  $\text{Al}_2\text{O}_3$  phase caused by diffusion of ions  $\text{Zr}^{4+}$  and  $\text{Y}^{3+}$  into alumina grains; for constrained isostrain model strain rate derived for volume fraction of  $\text{Al}_2\text{O}_3$  equalled 1 is lower than experimentally obtained one for pure

$\text{Al}_2\text{O}_3$ . In the case of composites A smaller grains of the composite in comparison with end-constituents (see Table 1) resulted in the reduction of the effect of strain rate change due to zirconium and yttrium ion diffusion into  $\text{Al}_2\text{O}_3$  and aluminum ion diffusion into  $\text{ZrO}_2$  grains. As it can be seen from Fig. 6, despite the considerable difference of the grain size of composites A and S (see Tables 1 and 3), strain rate of both composites are similar. It means that the spinel/zirconia composite under comparable conditions (like grain size, stress and temperature) is deformed much faster than the corresponding alumina/zirconia compos-

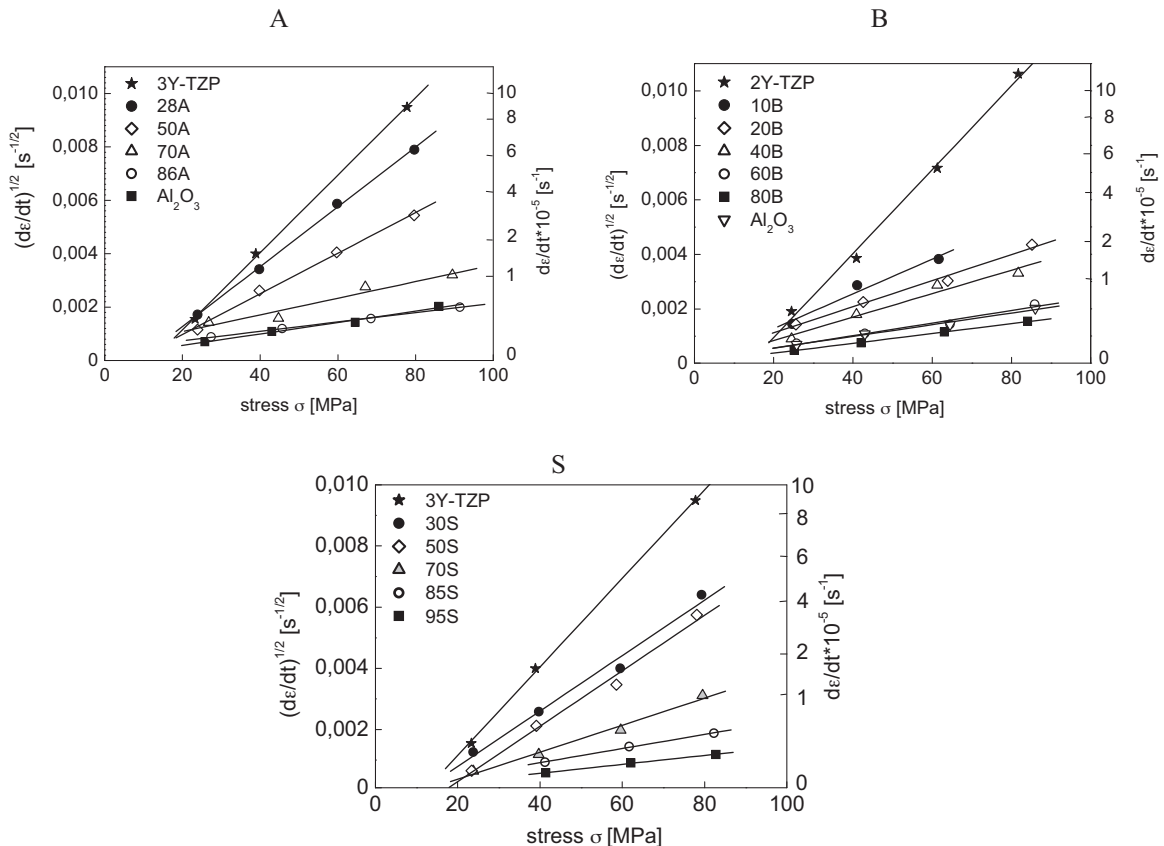


Fig. 4. Square root of strain rate  $(d\epsilon/dt)^{1/2}$  vs. applied stress  $\sigma$  for A, B and S composites at  $1280^\circ\text{C}$ . For sake of clarity the plots for chosen S composites are shown.



Table 4

Parameters for model curves calculations at  $\sigma = 50$  MPa and  $T = 1280$  °C.

Model	Composite	Parameters					
		$n_1$	$n_2$	$\dot{\epsilon}_1$	$\dot{\epsilon}_2$	$K_1$	$K_2$
Isostress Eq. (2)	A			$1.5 \times 10^{-6}$	$2.7 \times 10^{-5}$		
	B			$1.5 \times 10^{-6}$	$3.5 \times 10^{-5}$		
	S			$1.1 \times 10^{-7}$	$2.7 \times 10^{-5}$		
Isostrain Eq. (4)	A	1.7	3.0			$1.28 \times 10^5$	$1.71 \times 10^3$
	B	1.7	2.9			$1.28 \times 10^5$	$1.72 \times 10^3$
	S	1.8	3.0			$3.68 \times 10^5$	$1.71 \times 10^3$
Constrained isostrain Eq. (6)	A					$3.74 \times 10^4$	$4.90 \times 10^3$
	B					$6.50 \times 10^4$	$6.99 \times 10^3$
	S					$5.37 \times 10^4$	$1.12 \times 10^3$
Rheological Eq. (7)	A		3.0		$2.7 \times 10^{-5}$		
	B		2.9		$3.5 \times 10^{-5}$		
	S		3.0		$2.7 \times 10^{-5}$		

In determining the parameters  $K_1$  and  $K_2$  for the constrained isostrain model all the experimental points with the exception of volume fraction of  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$   $V_1 = 1$  are taken into account due to the fact that for all the experimental points and without  $V_1 = 0$  and 1 negative (not physical) values of  $K_2$  for the composite S were obtained.

ite. In this situation, it seems that none of the proposed models can explain the behaviour of the composite S because they do not provide the interaction between phases. Increased strain rate of the composite S compared with A and B is caused probably by a significant increase in diffusion coefficient of  $\text{Zr}^{4+}$  ions in the  $\text{ZrO}_2$  grains due to the simultaneous doping with  $\text{Al}^{3+}$  and  $\text{Mg}^{2+}$  ions.<sup>28</sup>

Our results are not directly comparable with data from the literature since the latter have been obtained in tensile and compressive tests and at higher temperatures<sup>17,18,20</sup> however, for instance, the conclusions concerning an application of the constrained isostrain model to interpret the results for composite B are the same as in.<sup>18</sup>

Relationships between strain rate and applied stress are presented in Fig. 4 as linear plots of  $(d\epsilon/dt)^{1/2}$  vs.  $\sigma$ . An extrapolation of a straight line to zero strain rate yields the value of  $\sigma_0$  which could be treated as threshold stress in superplasticity<sup>11,20</sup>; the deformation mechanisms do not work at stresses  $< \sigma_0$ . The values of  $\sigma_0$  are shown in Fig. 7 as a function of volume fraction of  $\text{Al}_2\text{O}_3$  and  $\text{MgAl}_2\text{O}_4$ .

The concept of threshold stress has been known for superplastic metallic alloys.<sup>29</sup> A characteristic of the creep behaviour of superplastic metallic alloys is the experimental observation that the relationship between the strain rate and the applied stress at constant temperature is often sigmoidal. This sigmoidal relationship is manifested by the presence of three distinct deformation regions<sup>29</sup>: region I – the low-stress region (the stress exponent,  $n > 2$ ); region II – intermediate-stress region ( $n$  is close to 2); region III – the high-stress region ( $n > 2$ ). It was suggested<sup>29</sup> that the transition in behaviour between region I and II may not necessarily reflected a change in deformation mechanism but can arise from the presence of a threshold stress  $\sigma_0$  which decrease strongly with increasing temperature. Physical meaning of this concept: it is the minimal force per unit area required for grains to displace with respect to each other. If  $\sigma_0$  exists then  $d\epsilon/dt \sim (\sigma - \sigma_0)^n$ . The possible origin of  $\sigma_0$  for superplastic-

ity in metallic alloys is impurity segregation at grain boundary and their interaction with grain boundary dislocation.<sup>29</sup> For yttria-stabilized tetragonal zirconia polycrystals two different explanations of the origin of the threshold exist:

1. It was established in<sup>30,31</sup> that grain-boundary segregation of yttrium caused an appearance of the threshold stress in this ceramics. This segregation changes the chemical composition as well as space charge at the boundaries, creating a local electric field, consequently affecting grain boundary sliding (GBS) which is responsible for the superplastic flow. GBS is accommodated by lattice diffusion of cations.
2. In turn in<sup>20</sup> it was claimed that the threshold stress could be ascribed to the nucleation of intragranular dislocations, which contributed to the relaxation of stress concentrations exerted around the grain junctions and boundary ledges by GBS. The strain rate is controlled by the rate of the dislocation recovery process limited by the lattice diffusion of cations.

Analyses of presented in this paper results do not allow to assess which of the models of  $\sigma_0$  origin is correct. It is seen in Fig. 7 that  $\sigma_0$  decreases as a function of  $\text{Al}_2\text{O}_3$  content to zero for composite A for alumina content above 0.5. However for composite B all  $\sigma_0$  values (with an exception of 2Y-TZP) are close zero. For composite S, up to content of  $\text{MgAl}_2\text{O}_4$  of 0.7,  $\sigma_0$  is almost constant and next decreases to zero up to 0.85. Papers<sup>20,32</sup> point out that the threshold stress effect is measured not only for zirconia ceramics but also for spinel–zirconia composites (even with large content of spinel phase). In turn in<sup>30</sup> it was claimed that no threshold stress should be measured if there was no segregation or charge effect. As an example alumina ceramics was given there. In alumina ceramics in which no segregation at the grain boundaries was described no threshold stress existed. The same situation was in yttria doped alumina in which yttrium segregation took place at the boundaries the effective electric charge of the dopants (compared with the par-

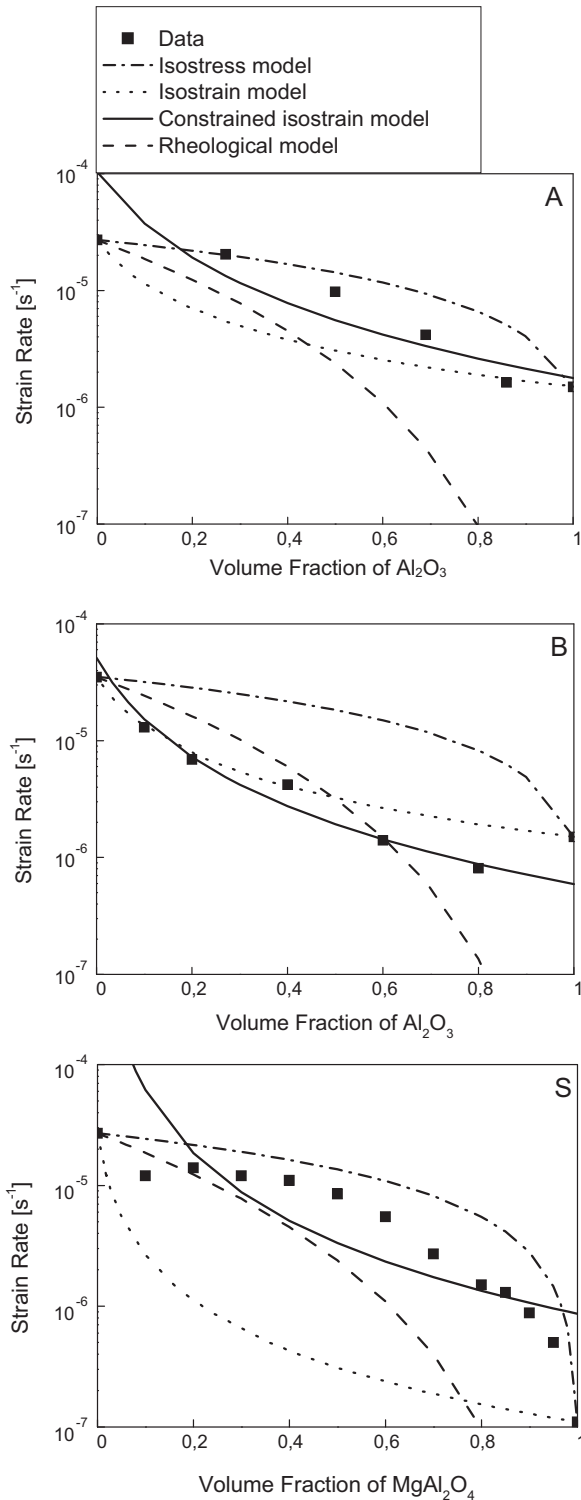


Fig. 5. Strain rate plotted as a function of volume fraction of  $\text{Al}_2\text{O}_3$  and  $\text{MgAl}_2\text{O}_4$  for studied composites A, B and S at stress 50 MPa and temperature 1280 °C.

ent ion) was zero, no charge effect was expected. In consequence no threshold stress should be measured. The cited reports support the thesis that threshold stress phenomenon is significant for spinel–zirconia composites but disappears in alumina–zirconia

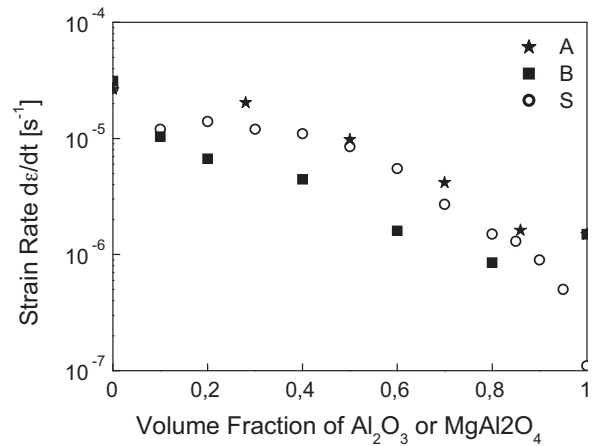


Fig. 6. The comparison of strain rates plotted as a function of volume fraction of  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$  for studied composites A, B and S at stress 50 MPa and temperature 1280 °C.

composites as it is observed in the case of A and B composites (Fig. 7).

Value of  $\sigma_0$  obtained here for 3Y-TZP and for 2Y-TZP 12.0 and 13.8 MPa respectively are consistent with  $\sigma_0$ -value predicted using  $\sigma_0 = (5 \times 10^{-4}/d) \exp(120,000/RT)$ .<sup>11</sup> The calculated hence values are 11.6 and 11.4 MPa respectively for 3Y-TZP and 2Y-TZP. In turn,  $\sigma_0$ -value obtained by extrapolation to temperature 1280 °C of the relationship for 30 vol%  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$  in<sup>20</sup> is about 30 MPa. It is higher than obtained here for the same composites (11.3 MPa). It probably stems from the fact that the grain sizes in<sup>20</sup> are much smaller than in our case (they are 0.3 and 0.35  $\mu\text{m}$  for 3Y-TZP and  $\text{MgAl}_2\text{O}_4$ , respectively, but in our case they are 1.1 and 1.2  $\mu\text{m}$ ). This relatively high level of  $\sigma_0$  for significant content of spinel in spinel/zirconia composites is interpreted in<sup>20</sup> as caused by enhanced diffusivity in zirconia which can more effectively relax the stress concentration around grain junctions, so that higher stresses are necessary to exert stress concentrations sufficient to nucleate dislocations in the spinel/zirconia composites.

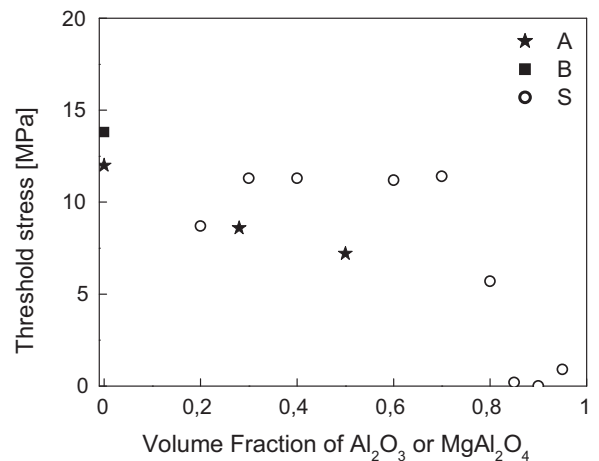


Fig. 7. The threshold stress for studied composites A, B and S at temperature 1280 °C plotted as a function of volume fraction of  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$ .

## 6. Conclusions

In the present paper the results of superplastic flow measurements of  $\text{Al}_2\text{O}_3/3\text{Y-TZP}$  (A),  $\text{Al}_2\text{O}_3/2\text{Y-TZP}$  (B) and  $\text{MgAl}_2\text{O}_4/3\text{Y-TZP}$  (S) particle composites at temperature  $1280^\circ\text{C}$  have been reported. The results can be summarized as follows:

- Values of stress exponent  $n$  are scattered around  $n=2$  for A and B composites and they are in the range of 1.8–3.1 for S composites.
- The strain rate of the composites decreases as a function of  $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$  content.
- Composites S show greater susceptibility to superplastic deformation than A and B.
- Isostress, isostrain and constrained isostrain model can predict successfully the superplastic behaviour of A and B composites but not of S. In turn, the rheological model seems to be useless for the data interpretations.
- The threshold stress approach can be applied for describing superplastic flow of S composites but it seems to be rather unsuitable for A and B composites.

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## Glossary

- $A_0$ : dimensionless constant in the creep equation  
 $b$ : Burgers vector  
 $d$ : grain size  
 $D$ : diffusion coefficient  
 $G$ : shear modulus  
 $k$ : Boltzmann's constant  
 $K_1 = G(kT/A_0 D G b)^{1/n_1} (d/b)^{p/n_1}$   
 $n$ : stress exponent  
 $p$ : inverse grain size exponent  
 $T$ : temperature  
 $V_I$ : volume fraction of rigid phase ( $\text{Al}_2\text{O}_3$  or  $\text{MgAl}_2\text{O}_4$ )  
 $\gamma$ :  $\sigma/\sqrt{\dot{\epsilon}}$   
 $\dot{\epsilon}$ :  $d\epsilon/dt$  – strain rate  
 $\sigma$ : applied stress